

Agenda

Review Quiz 4- Discuss Test 2

Lecture Newton's Method

Lecture Differentials/ Error

Project: Error

Review Quiz #4

Write your answer in radical form.

Find a value of c satisfying the conclusion of the Mean Value Theorem.

$$f(x) = x^3 + 8x^2, [0, 3]$$

$$c = \input{width=1.5cm,height=1.2cm}$$

Write your answer in radical form.

Find a value of c satisfying the conclusion of the Mean Value Theorem.

$$f(x) = x^3 + 8x^2, [0, 3]$$

$c =$

MVT

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

$$f'(x) = 3x^2 + 16x$$

$$f(3) = 27 + 72 = 99$$

$$3x^2 + 16x = \frac{f(3) - f(0)}{3 - 0}$$

$$3x^2 + 16x = 99$$

$$3x^2 + 16x - 99 = 0$$

$$x = \frac{-16 \pm \sqrt{16^2 - 4 \cdot 3 \cdot (-99)}}{3 \cdot 3}$$

Find the linear approximation at $x = 0$ to show that the valid for "small" x . Compare the approximate and exact calculations to seven decimal places if needed.

$$5 \tan(x) \approx 5x$$

	$L(x)$	$f(x)$
$x = 0.01$		
$x = 0.1$		
$x = 1$		

Note: $f(x) = 5 \tan(x)$

Find the linear approximation at $x = 0$ to show that the valid for "small" x . Compare the approximate and exact your calculations to seven decimal places if needed.

$5 \tan(x) \approx 5x$

	$L(x)$	$f(x)$
$x = 0.01$.05	.05
$x = 0.1$.5	.50167
$x = 1$	5	7.787

Note: $f(x) = 5 \tan(x)$

X	Y1	Y2
.01	.05	.05
.1	.5	.50167
1	5	7.787

NORMAL FLOAT AUTO REAL RADIAN CL

Plot1 Plot2 Plot3

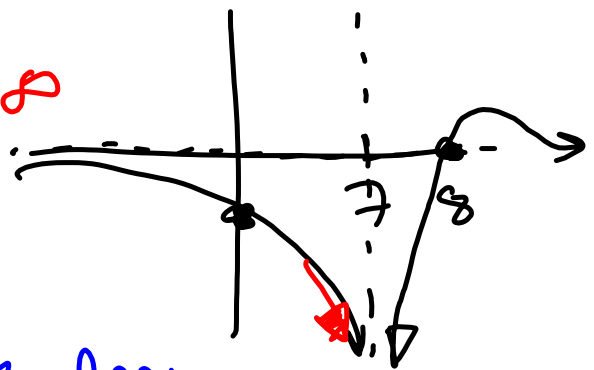
X=.01

- Y1 = 5X
- Y2 = 5tan(X)
- Y3 =
- Y4 =
- Y5 =
- Y6 =
- Y7 =
- Y8 =
- Y9 =

Test 2 Review

$$\lim_{x \rightarrow 7^-} \frac{x - 8}{x^2 - 14x + 49}$$

$$\lim_{x \rightarrow 7^-} \frac{x - 8}{x^2 - 14x + 49} = -\infty$$



$$\frac{x - (6.9999) - 8}{(6.9999^2 - 14(6.9999) + 49)} = -7002000$$

$$\lim_{x \rightarrow 7^-} \frac{x-8}{\underbrace{x^2 - 14x + 49}_{<49 \quad -98 \quad +49}} = -\infty = \frac{1}{+0}$$

$$y_1 = (x-8)/(x^2 - 14x + 49)$$

Table

$$x = 6.999$$

$$6.9999$$

$$y = -1 \text{ E } 6 = -1 \times 10^6$$

$$-1.0 \text{ E } 10 = -1,000,000$$

#1

Compute the derivative of $f(x) = \sinh^2(9x)$.

#1

Compute the derivative of $f(x) = \sinh^2(9x)$.

chain rule
twice

$$\frac{d}{dx} (\sinh(9x))^2$$

$$2(\sinh(9x))' \cdot \frac{d}{dx} \sinh(9x)$$

$$2 \sinh(9x) \cosh(9x) \cdot \frac{d}{dx}(9x)$$

$$18 \sinh(9x) \cosh(9x)$$

Find a value of c satisfying the conclusion of the Mean Value Theorem.

Write your answer in radical form.

$$f(x) = x^3 + 4x^2, [0, 3]$$

$$27 + 36 = 63$$

$f(3) =$

$$\text{Avg Rate of Change} = \frac{63 - 0}{3 - 0} = 21$$

$$f'(x) = 3x^2 + 8x$$

MVT. $21 = 3x^2 + 8x$

$$0 = 3x^2 + 8x - 21$$

$$x = \frac{-8 \pm \sqrt{64 - 4(3)(-21)}}{6}$$

Not between $(0, 3)$

#2

Find a value of c satisfying the conclusion of the Mean Value Theorem.

Write your answer in radical form.

$$f(x) = x^3 + 4x^2, [0, 3]$$

Ave Rate

$$\frac{f(3) - f(0)}{3 - 0} = \frac{27 + 36 - 0}{3} = \frac{63}{3} = 21$$

Instantaneous $f'(x) = 3x^2 + 8x$

$$3x^2 + 8x = 21$$

$$3x^2 + 8x - 21 = 0$$

$$x = \frac{-8 \pm \sqrt{64 - 4(3)(-21)}}{6} \quad \text{on } [0, 3]$$

$$\frac{-8 + 2\sqrt{79}}{6}$$

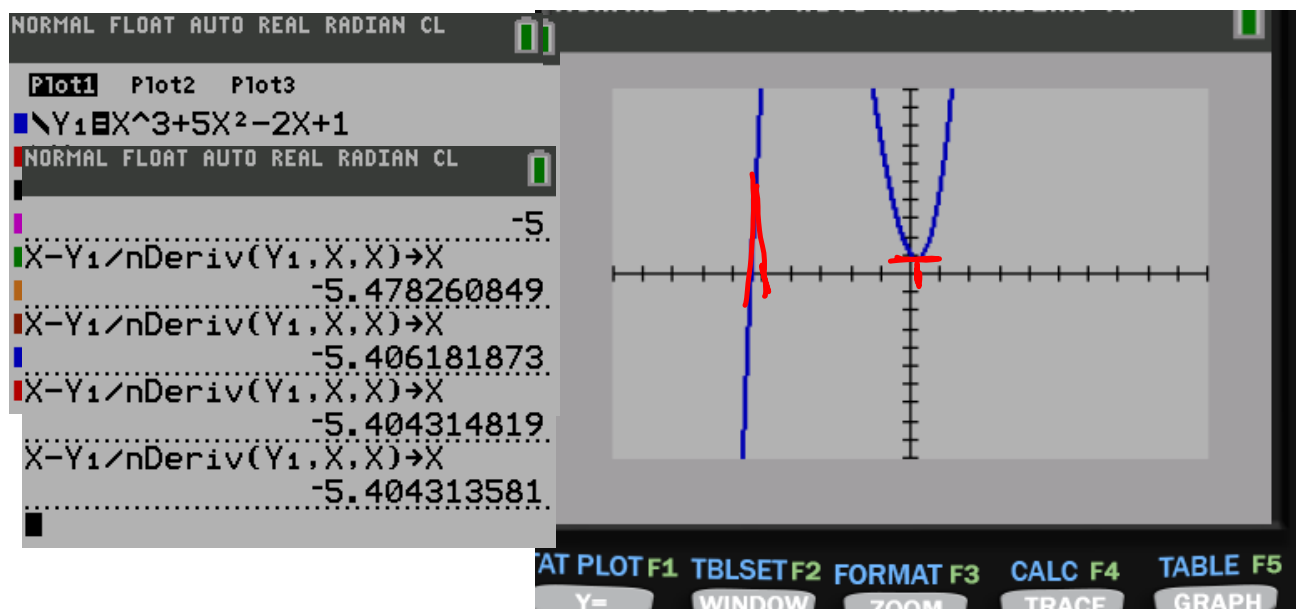
$$\frac{-4 + \sqrt{79}}{3}$$

Use Newton's method to find an approximate root (accurate to six decimal places).

$$x^3 + 5x^2 - 2x + 1 = 0$$

Use Newton's method to find an approximate root (accurate to six decimal places).

$$x^3 + 5x^2 - 2x + 1 = 0$$



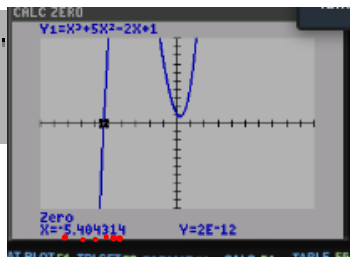
#5

Use Newton's method to find an approximate root (accurate to six decimal places).

$$x^3 + 5x^2 - 2x + 1 = 0$$

Calc 2: zero
Left: -6
Right: 0
Cross: 0

Y1 = X³ + 5X² - 2X + 1



$X - \frac{Y_1}{\frac{d}{dX}(Y_1)} \Big|_{X=X} \rightarrow X$
1.781818204
5 → X

-5.404313581
 $X - \frac{Y_1}{\frac{d}{dX}(Y_1)} \Big|_{X=X} \rightarrow X$
-5.404313581
 $X - \frac{Y_1}{\frac{d}{dX}(Y_1)} \Big|_{X=X} \rightarrow X$
-5.404313581
 $X - \frac{Y_1}{\frac{d}{dX}(Y_1)} \Big|_{X=X} \rightarrow X$
-5.404313581

Use the position function $s(t) = \frac{98t}{\sqrt{t^2 + 1}}$ to find the velocity at time $t = 2$.

(Assume units of meters and seconds.)

$$v(2) = \boxed{} \text{ m/s}$$

Use the position function $s(t) = \frac{98t}{\sqrt{t^2 + 1}}$ to find the velocity at time $t = 2$.

(Assume units of meters and seconds.)

$v(2) = \boxed{}$ m/s

$$s' = \frac{\sqrt{t^2+1} \cdot 98 - 98t \cdot \frac{d}{dt}(t^2+1)^{1/2}}{(\sqrt{t^2+1})^2}$$

$$s'(t) = \frac{\sqrt{t^2+1} \cdot 98 - 98t \cdot \frac{1}{2}(t^2+1)^{-1/2} \cdot 2t}{t^2+1}$$

$$s'(2) = \frac{\sqrt{5} \cdot 98 - 98(2) \left(\frac{1}{2} \sqrt{\frac{1}{5}} \right) \cdot 2}{5} = \frac{98 \left(\sqrt{5} - \frac{4}{\sqrt{5}} \right)}{5} = \frac{98}{5\sqrt{5}}$$

Use the position function $s(t) = \frac{98t}{\sqrt{t^2 + 1}}$ to find the velocity at time $t = 2$.

(Assume units of meters and seconds.)

$v(2) =$ m/s

$$s'(t) = \frac{\sqrt{t^2 + 1} \cdot 98 - 98t \cdot \frac{1}{2} (t^2 + 1)^{-1/2} \cdot (2t)}{t^2 + 1}$$

$$\frac{d}{dX}(Y_1) \Big|_{X=2}$$

NORMAL FLOAT AUTO REAL RADIAN CL

nDeriv(Y1,X,2)

8.7653891

$$\sqrt{xy} - 7y^2 = 33$$

Implicit-

$$\sqrt{xy} - 7y^2 = 33$$

$$\frac{d}{dx} (xy)^{1/2} - \frac{d}{dx} 7y^2 = 0$$

$$\frac{1}{2} (xy)^{-1/2} [xy' + y] - 14yy' = 0$$

$$xy' + y - 28\sqrt{xy} yy' = 0$$

$$y'(x - 28\sqrt{xy} \cdot y) = -y$$

$$y' = \frac{-y}{x - 28y\sqrt{xy}}$$

$$\frac{d}{dx} \left(\sqrt{xy} - 7y^2 \right) = 33$$

$$\frac{1}{2} (xy)^{-1/2} \cdot \frac{d}{dx} (xy) - 14y' \frac{dy}{dx} = 0$$

$$\frac{1}{2} (xy)^{-1/2} \left(x \frac{dy}{dx} + y \right) - 14y \frac{dy}{dx} = 0$$

$$\frac{1}{2} x (xy)^{-1/2} \frac{dy}{dx} + \frac{1}{2} y (xy)^{-1/2} - 14y \frac{dy}{dx} = 0$$

$$\frac{d}{dx} \left(\frac{1}{2} x (xy)^{-1/2} - 14y \right) = \frac{1}{2} y (xy)^{-1/2}$$

Symbolically find a $\delta > 0$ in terms of ε for

$$\lim_{x \rightarrow 4} (1 + x/2) = 3.$$

- A. $4\varepsilon = \delta$
- B. $2\varepsilon = \delta$
- C. $\varepsilon/4 = \delta$
- D. $-2\varepsilon = \delta$

Symbolically find a $\delta > 0$ in terms of ε for

$$\lim_{x \rightarrow 4} (1 + x/2) = 3.$$

- A. $4\varepsilon = \delta$
- B. $2\varepsilon = \delta$
- C. $\varepsilon/4 = \delta$
- D. $-2\varepsilon = \delta$

$$|f(x) - L| < \varepsilon$$

$$\left| \begin{array}{l} 1 + x/2 - 3 \\ -2 + x/2 \end{array} \right|$$

$$\left(\frac{1}{2} \right)$$

$$|x - 4| < \varepsilon$$

$$|x - 4| < 2\varepsilon = \delta$$

Symbolically find a $\delta > 0$ in terms of ε for

$$\lim_{x \rightarrow 4} (1 + x/2) = 3.$$

- A. $4\varepsilon = \delta$
- B. $2\varepsilon = \delta$
- C. $\varepsilon/4 = \delta$
- D. $-2\varepsilon = \delta$

$$|f(x) - \overset{\text{Limit}}{\boxed{3}}| < \varepsilon$$

$$|1 + \frac{x}{2} - \boxed{3}| < \varepsilon$$

$$|2 + x - 6| < 2\varepsilon$$

$$|x - \boxed{4}| < 2\varepsilon = \delta$$

$$-2\varepsilon < x - 4 < 2\varepsilon$$

$$4 - 2\varepsilon < x < 4 + 2\varepsilon$$

Symbolically find a $\delta > 0$ in terms of ε for

$\lim_{x \rightarrow 4} (1 + x/2) = 3.$

- A. $4\varepsilon = \delta$
- B. $2\varepsilon = \delta$
- C. $\varepsilon/4 = \delta$
- D. $-2\varepsilon = \delta$

$$\left| 1 + \frac{x}{2} - 3 \right| < \varepsilon$$

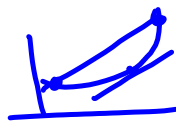
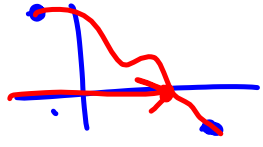

$$\left| \frac{x}{2} - 2 \right| < \varepsilon$$

$$\frac{1}{2} |x - 4| < \varepsilon$$

$$|x - 4| < 2\varepsilon = \delta$$

$$x - \delta$$

Calculus Overview

- ✓ Mean Value 
- ✓ Intermediate Value 
- ✓ Squeeze Limits Theorem 

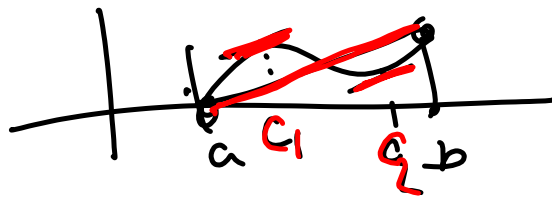
Fundamental Theorems
of Calc.

Apps of Derivative



$$f'(c) = \underline{\text{Instant}}$$

$$= \underline{\text{Ave. rate.}}$$



$$y = x^3 + 3x^2 \quad \text{on } [0, 4]$$

→ M.V.T.

A.R.C.

$$\frac{f(4) - f(0)}{4 - 0} = \frac{1(2) - 0}{4 - 0} = 28$$

I.R.C.

$$y' = 3x^2 + 6x$$

$$3x^2 + 6x = 28$$

$$3x^2 + 6x - 28 = 0$$

$$x = \frac{-6 \pm \sqrt{6^2 - 4(3)(-28)}}{2(3)}$$

$$\frac{-6 \pm \sqrt{36 + 336}}{6}$$

$$\frac{-6 \pm \sqrt{372}}{6}$$

$$\frac{-6 \pm \sqrt{4} \sqrt{93}}{6}$$

$$\frac{2(-3 + \sqrt{93})}{2 \cdot 3} = \frac{-6 \pm 2\sqrt{93}}{6} = \frac{-3 \pm \sqrt{93}}{3}$$

on $[0, 4]$ $\frac{-3 + \sqrt{93}}{3}$

Check the Mean Value Theorem and find a value of c that makes the appropriate conclusion true. Round your answer to two decimal places.

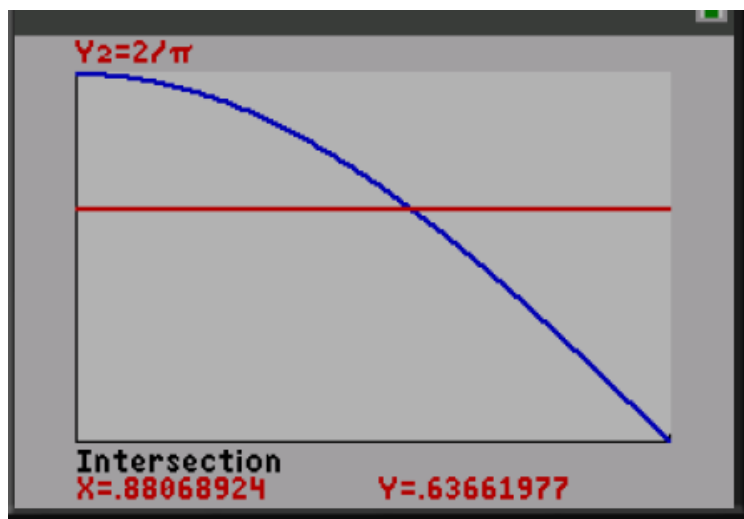
$$f(x) = \sin x + 97, \left[0, \frac{\pi}{2} \right]$$

Check the Mean Value Theorem and find a value of c that makes the appropriate conclusion true. Round your answer to two decimal places.

$$f(x) = \sin x + 97, \left[0, \frac{\pi}{2}\right]$$

$$\frac{\sin 0 + 97 - \left(\sin \frac{\pi}{2} + 97\right)}{0 - \pi/2} = \frac{-1}{-\pi/2}$$

$$f'(x) = \cos x = \frac{2}{\pi}$$



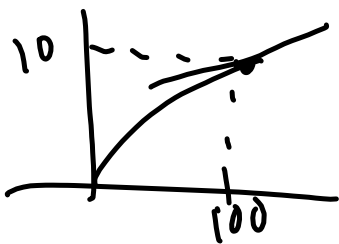
Local
Linear
Approx.

$$\sqrt{101} \approx f(x) = \sqrt{x}$$

$(100, 10)$ $x_0 = 100$
 $y_0 = 10$

$$f(x) \approx f(x_0) + f'(x_0)(x - x_0)$$

$$y = \frac{1}{0} + m(x - x_0)$$



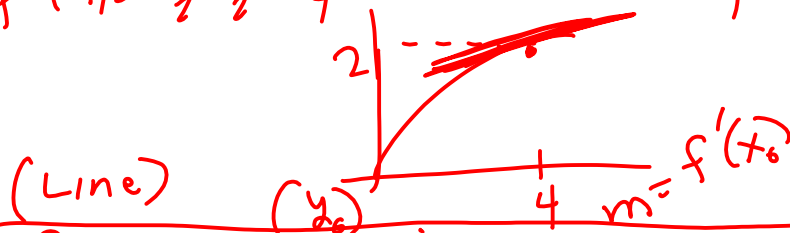
Point (x_0, y_0)
Slope m

$\sqrt{5} \approx 2.236$
around $\sqrt{4} = 2$

$f(x) = \sqrt{x}$ Center $x=4, y=2$

$f'(x) = \frac{1}{2}x^{-1/2}$ $(4, 2)$

$f'(4) = \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$ Slope = $\frac{1}{4}$



$$f(x) \approx f(x_0) + f'(x_0)(x - x_0)$$

$$\sqrt{x} \approx 2 + \frac{1}{4}(x - 4)$$

X	Y1	Y2
4	2	2
5	2.2361	2.25
6	2.4495	2.5
7	2.6458	2.75
8	2.8284	3
9	3	3.25

$$\frac{1}{4}(5 - 4)$$

$$\approx 2\frac{1}{4}$$

$$\frac{1}{4}(6 - 4)$$

$$\approx 2\frac{1}{2}$$

$$\frac{1}{4}(7 - 4)$$

$$\sqrt{7} \approx 2 +$$

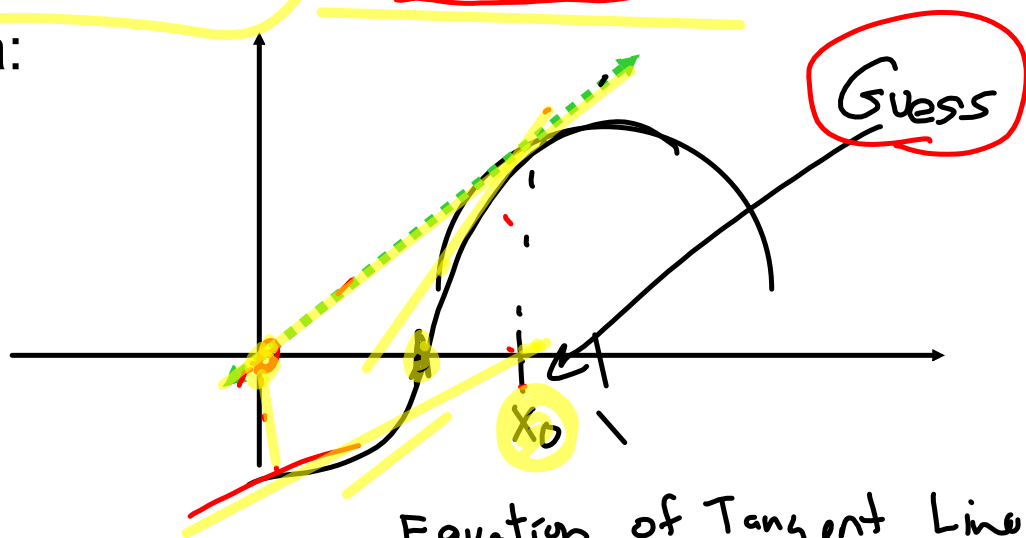
$$\sqrt{8} \approx 2 + \frac{1}{4}(8 - 4)$$

$$\approx 3$$

!

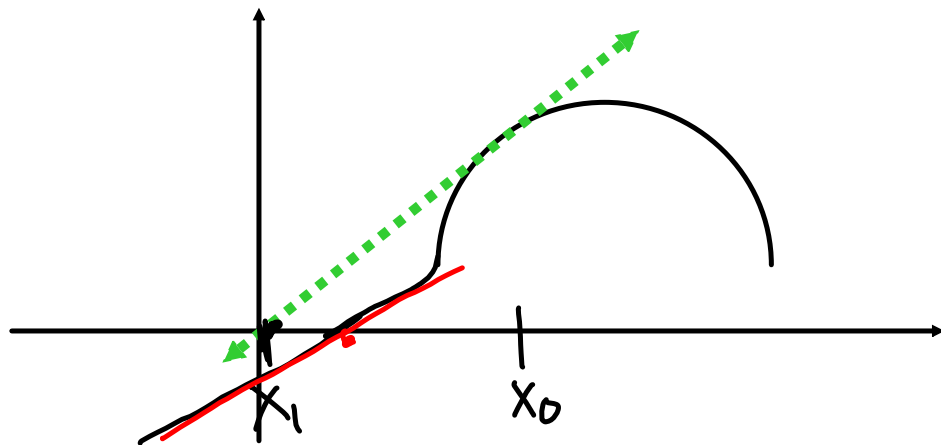
Newton's Method (for finding zeros)

Idea:



Equation of Tangent Line
$$y = y_0 + f'(x_0)(x - x_0)$$

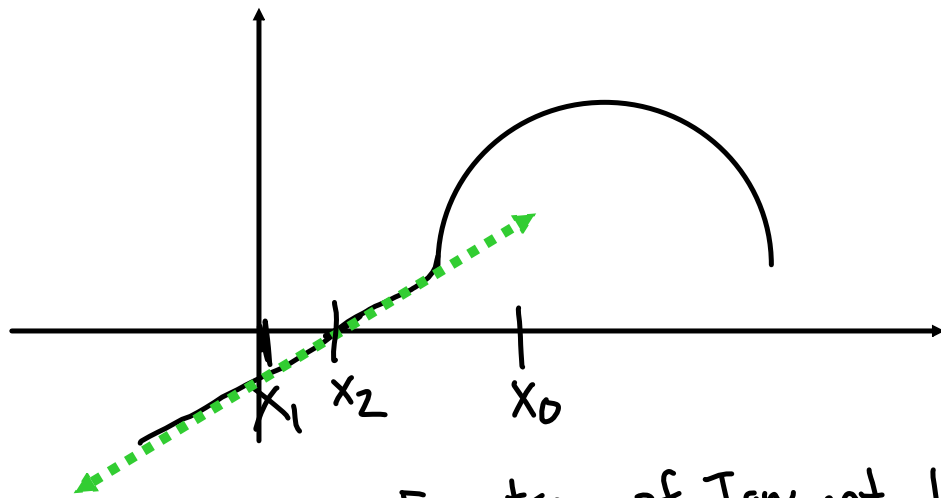
Newtons Method



$$0 = y_0 + f'(x_0)(x - x_0)$$

Equation of Tangent Line
 $y = y_0 + f'(x_0)(x - x_0)$

$$x = x_0 - \frac{y_0}{f'(x_0)} \Rightarrow x_1$$



$$0 = y_1 + f'(x_1)(x - x_1)$$

$$x = x_1 - \frac{y_1}{f'(x_1)} \Rightarrow x_2$$

Equation of Tangent Line
 $y = y_1 + f'(x_1)(x - x_1)$

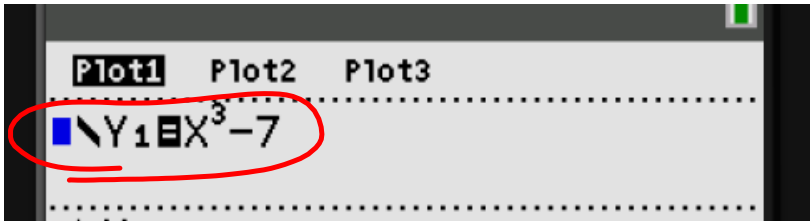
Repeat

$$\underline{x_{n+1}} = \underline{x_n} - \frac{f(x_n)}{f'(x_n)}$$

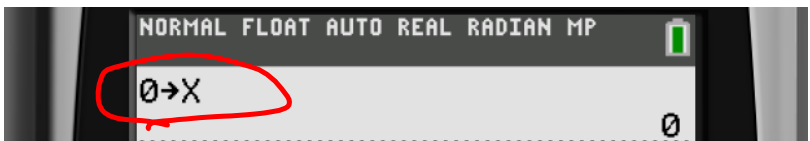
New Old — Function at old value.
Derivative -

Eventually settles on answer.

Ex Solve $y = X^3 - 7 = 0$ $X^3 = 7$

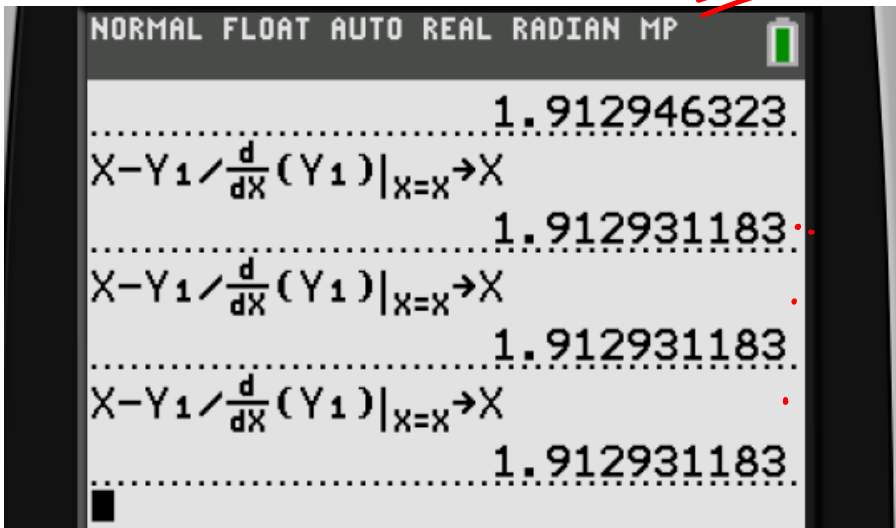
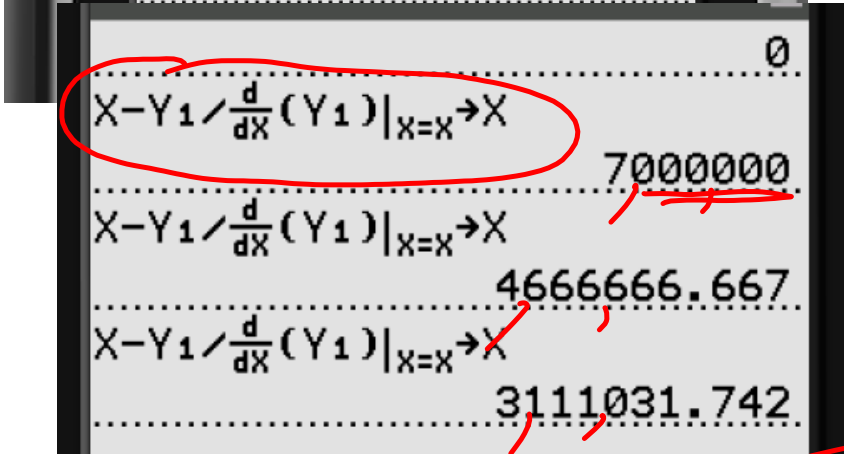


Guess ≈ 0



$$X^3 = 7$$

$$X^3 - 7 = 0$$



$$X^3 - 7 = 0$$

$$X^3 = 7$$

$$X = \underline{1.91\dots}$$

A certain parasite is an enemy of a specific type of tree. In one model of the interaction between these organisms, possible long-term populations of the parasite are the solutions of the equation $r(1 - x/k) = 5x/(1 + x^2)$, for constants r and k . Find all possible solutions of the equation with $r = 2.5$ and $k = 7$.

Your Answer:

A certain parasite is an enemy of a specific type of tree. In one model of the interaction between these organisms, possible long-term populations of the parasite are the solution of the equation $r(1 - x/k) = 5x/(1 + x^2)$, for constants r and k . Find all possible solutions of the equation with $r = 2.5$ and $k = 7$.

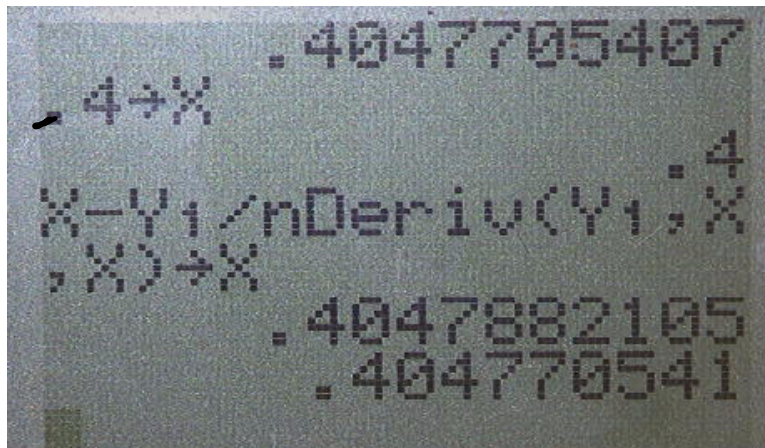
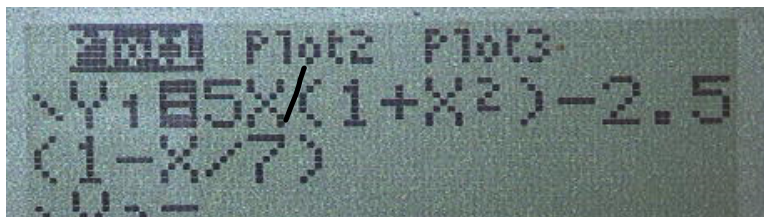
Your Answer:

$$2.5(1 - x/7) = 5x/(1 + x^2)$$

$$5x/(1 + x^2) - 2.5(1 - x/7) = 0 \quad \text{Solve for } x?$$

Newton's,

$y_1 = \dots$



1. Solver

2. Intersect

3. Newton's

4. Graph. Find zeros

A certain parasite is an enemy of a specific type of tree. In one model of the interaction between these organisms, possible long-term populations of the parasite are the solution of the equation $r(1 - x/k) = 5x/(1 + x^2)$, for constants r and k . Find all possible solutions of the equation with $r = 2.5$ and $k = 7$.

Your Answer:

Solu

$$2.5\left(1 - \frac{x}{7}\right) = \frac{5x}{1+x^2}$$

$$0 = 5x / (1+x^2) - 2.5(1-x/7)$$

Plot2 Plot3
 $Y_1 = 5X(1+X^2) - 2.5(1-X/7)$
 0.4047705407

$.4047705407$
 $.4 \rightarrow X$
 $X - Y_1 / nDeriv(Y_1, X, X) \rightarrow X$
 $.4047882105$
 $.404770541$

Give your final answers as reduced improper fractions.

Use Newton's method with the given x_0 to compute x_1 and x_2 by hand.

$$x^3 + 5x^2 - 7 = 0, x_0 = 1$$

Give your final answers as reduced improper fractions.

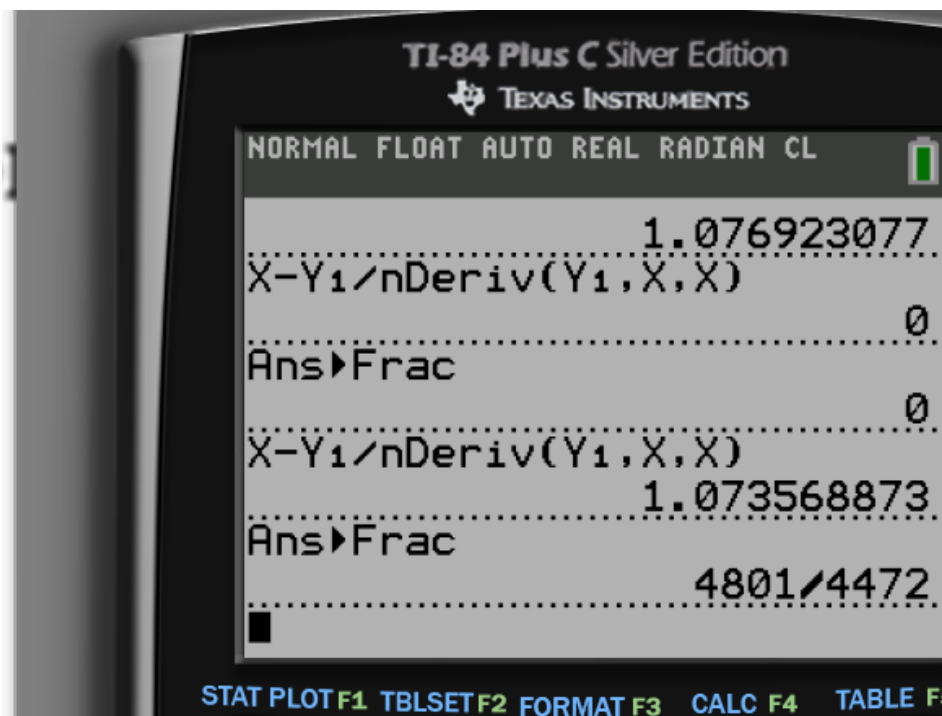
Use Newton's method with the given x_0 to compute x_1 and x_2 by hand.

$$x^3 + 5x^2 - 7 = 0, x_0 = 1$$

$$x_0 = 1$$

$$x_1 = 1 - \frac{1^3 + 5(1)^2 - 7}{3(1)^2 + 10(1)} = 1 - \frac{-1}{13} = \frac{14}{13}$$

$$x_2 = \frac{14}{13} - \frac{\left(\frac{14}{13}\right)^3 + 5\left(\frac{14}{13}\right)^2 - 7}{3\left(\frac{14}{13}\right)^2 + 10\left(\frac{14}{13}\right)} =$$



Give your final answers as reduced improper fractions.

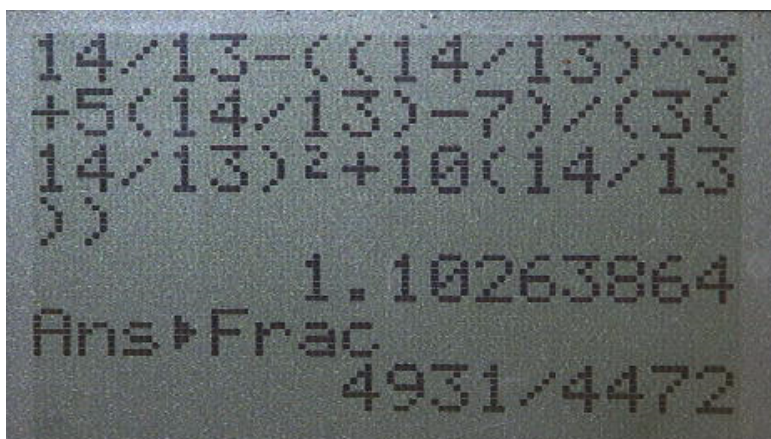
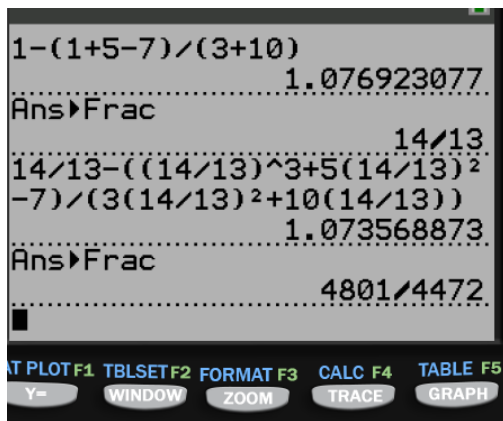
Use Newton's method with the given x_0 to compute x_1 and x_2 by hand.

$$x^3 + 5x^2 - 7 = 0, x_0 = 1$$

$$X - \frac{X^3 + 5X^2 - 7}{3X^2 + 10X}$$

$$1 - \frac{1 + 5 - 7}{3 + 10} = \frac{14}{13}$$

$$\frac{14}{13} - \frac{\left(\frac{14}{13}\right)^3 + 5\left(\frac{14}{13}\right)^2 - 7}{3\left(\frac{14}{13}\right)^2 + 10\left(\frac{14}{13}\right)}$$



Give your final answers as reduced improper fractions.

Use Newton's method with the given x_0 to compute x_1 and x_2 by hand.

$$x^3 + 5x^2 - 7 = 0, x_0 = 1$$

$$y = x^3 + 5x^2 - 7$$

$$y' = 3x^2 + 10x$$

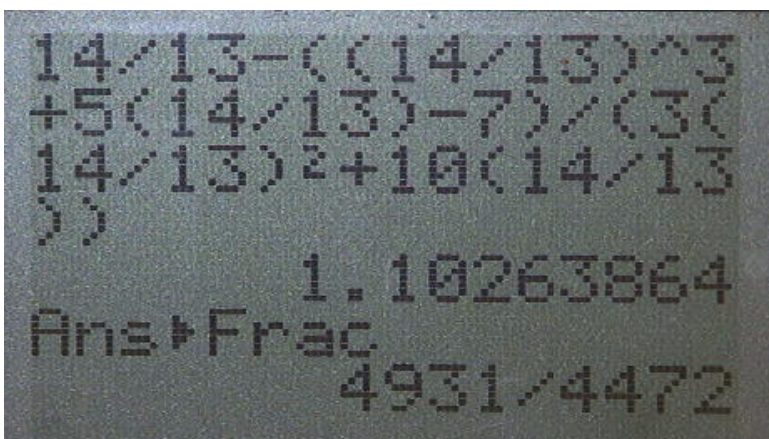
$$x_1 = \frac{y_0(x_0)}{y_0'(x_0)}$$

$$1 - \frac{1}{13} = \frac{14}{13}$$

$$y\left(\frac{14}{13}\right) = \left(\frac{14}{13}\right)^3 + 5\left(\frac{14}{13}\right)^2 - 7$$

$$y'\left(\frac{14}{13}\right) = 3\left(\frac{14}{13}\right)^2 + 10\left(\frac{14}{13}\right)$$

$\frac{14}{13} - \frac{0}{\square} = \text{NASTY}$



Ans: $Y = (Ans) \times 100$
 $100Y = X, Ans) \blacksquare$

Use Newton's method to approximate $\sqrt[3]{16}$.

Round your final answer to nine decimal places.

Your Answer:

$$\begin{aligned}\sqrt[3]{16} &= x \\ x - \sqrt[3]{16} &= 0 \\ x^3 - 16 &= 0\end{aligned}$$

Use Newton's method to approximate $\sqrt[3]{16}$.

Round your final answer to nine decimal places.

Your Answer:

$$y_1 = x^3 - 16$$

$$x_0 = 2$$

$$x = \sqrt[3]{16}$$

$$x^3 = 16$$

$$2 \rightarrow x$$
$$x - y_1 / \text{deriv.}(y_1, x, x) \rightarrow x$$

$$x^3 - 16 = 0$$

$$x_1 = 2 - \frac{2^3 - 16}{3 \cdot 2^2} =$$

⋮

Use Newton's method to approximate $\sqrt[3]{16}$.

Round your final answer to nine decimal places.

Your Answer:

$$\begin{aligned} (X)^3 &= (\sqrt[3]{16})^3 \\ 0 &= X^3 - 16 \quad X^3 = 16 \end{aligned}$$

Differentials

$$dx \longrightarrow \frac{d}{dx}$$

$$\frac{d}{dx} y^2 = 2y \quad d(y^2)$$

$$\frac{d}{dx} y^2 = 2y \frac{dy}{dx}$$

$$\frac{d}{dx} x^2 = 2x$$

$$\frac{d}{dt} x^2 = 2x \frac{dx}{dt}$$

$$d(x^2) = 2x \frac{dx}{dt}$$

Differential

$$f'(x) \equiv \frac{d}{dx} f(x)$$

$$\frac{d}{dt} f(x) = f'(x) \cdot \frac{dx}{dt}$$
$$\underline{d f(x) = f'(x) \cdot dx}$$

Differential

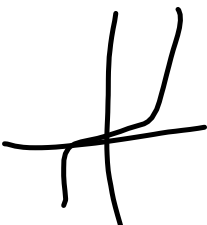
$$\underline{d f(x) = f'(x) dx}$$

1

Take derivative w.r.t Nothing

4

$$y = x^3$$



$$\frac{dy}{dx} = 3x^2$$

$$dy = 3x^2 dx$$

$$\Delta y \approx$$

exact
change
in y

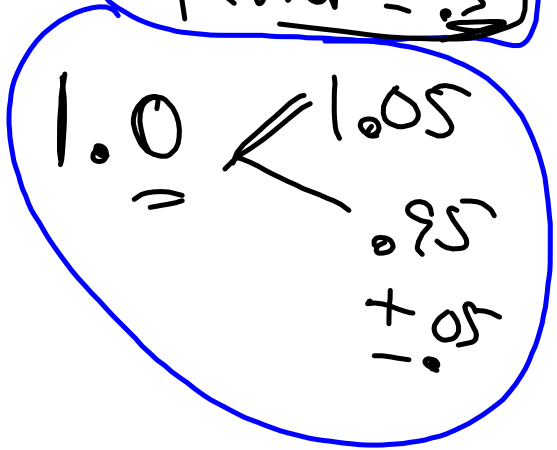
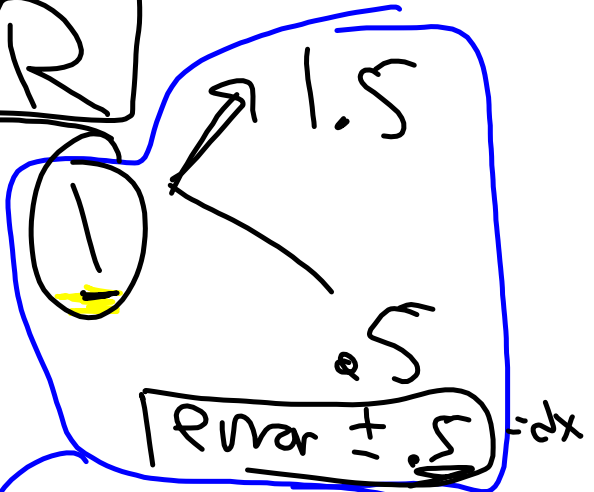
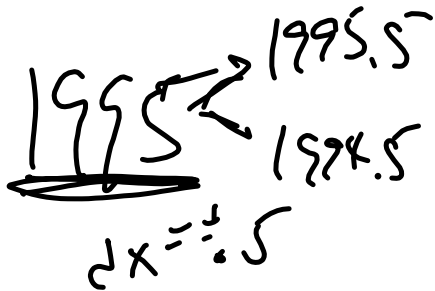
$$dy = f'(x) dx$$

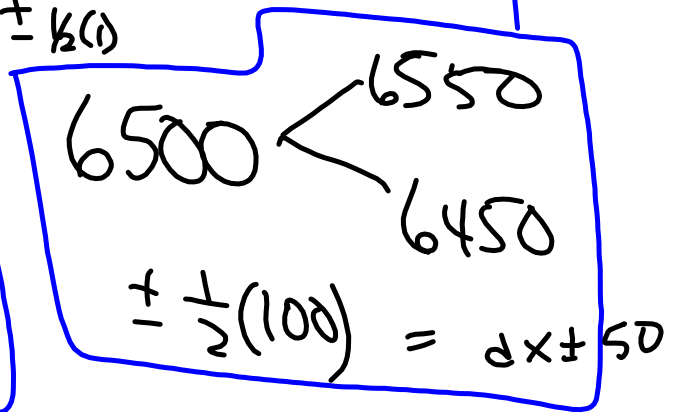
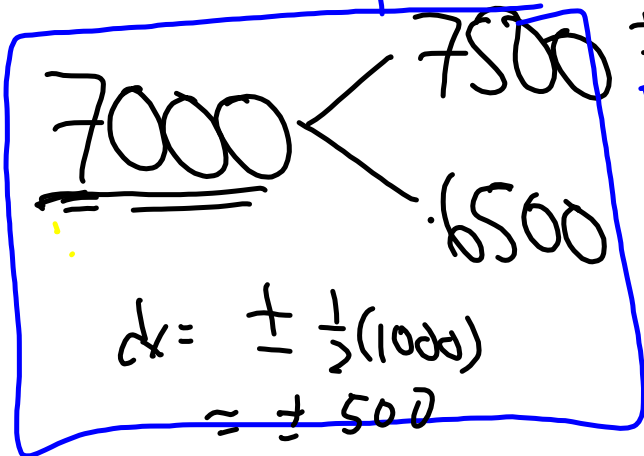
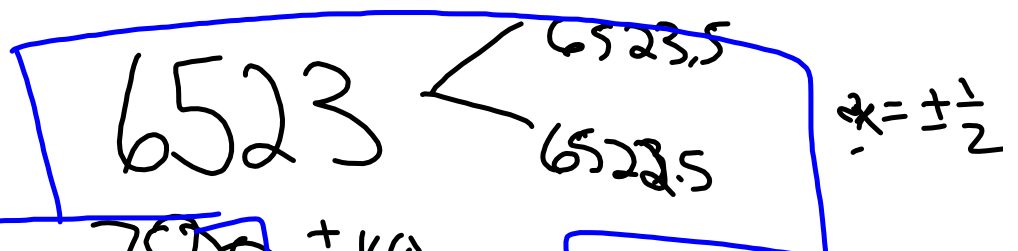
$$\Delta y = y_2 - y_1$$

$$dy =$$

ERROR

X - Number (Δx)





6.500 $\times 10^3$

Project: Error

y1=regression

y2=nderiv(y1, x, x) * 0.5 error

y3= y2 / y1 * 100 % error

$$y = f(x)$$

$$dy = f'(x) \cdot dx$$
$$= f'(x) dx$$

error in
derivative number

$y = y_1 = \text{regression}$ $f'(x) \Delta x = \Delta y$

$\Delta y = y_2 = \text{nderiv}(y_1, x, x) * \underline{0.5}$ error

$y_3 = y_2 / y_1 * 100$ % error

X	Y1	Y2	Y3
11.8	7.9015	6.0107	7.607

Plot1 Plot2 Plot3
 ■ \Y1 ■ .3123426473315*1.1643221776647^X (exp res)
 ■ \Y2 ■ 1.3123426473315*1.1643221776647^X*ln(1.1643221776647)*.5 ← y'
 ■ \Y3 ■ Y2/Y1*100

7.9 ± .6
% error 7.6

write $r(95) = 10$
 $r'(95) * .5 = .5$ $r(95) / r'(95) * 100 = .005$

(95)

y1=regress	y2=error	y3=%error
10	±.5	.005

speaker

In 95, LG is worth 10mil +/- .5mil with an error of .005%

Accordy to — regress

$Y_1 =$ regression

X	Y	Error	% error
1995	Worth y	Error dy	.005

$$f'(x_{1995}) \cdot dx$$

$$Y_2 = \text{ndert}(Y_1, X, X) \cdot \underline{.5}$$

$$Y_3 = Y_2 / Y_1 \times 100 = \text{percent}$$

In 95, LG is worth 10mil +/- .5mil with an error of .005%

Conclusion in words:

With 50k cases there are 1181.3 earthquakes plus and minus 117 with an error of 10%.

TI-84 Plus CE

NORMAL FLOAT AUTO REAL Radian CL

X	Y1	Y2	Y3
50	1181.3	117.05	9.9083

Conclusion in words:

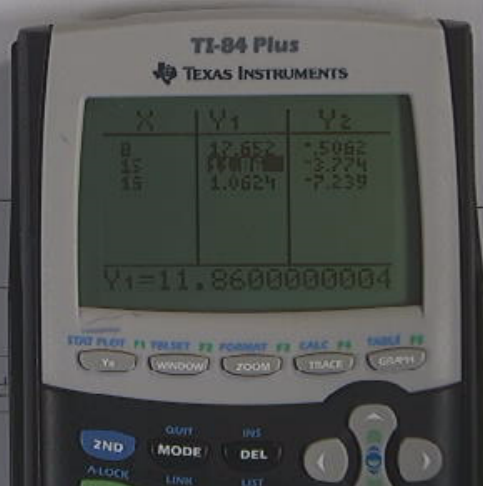
In year 2015, the radio industry is worth
 $\$1.86$ billion dollars with a ± 3.774 error
and a $\pm 31.83\%$ error.

13. Error: Find the error in your x-values:

Now find $f'(a)$:

Multiply them:

y_1
Quadratic
17.652



y-axis (dependent variable): Kg waste

Conclusion in words:

X	Y ₁	Y ₂	Y ₃
90	22588	291.25	1.5
100	32615	335.91	1.02

In 2000 there was 32615 Kg garbage with an error of ± 335.91 with % error of 1.02% according to the cubic regression.

13. Error: Find the error
Now find $f'(a)$:
Multiply them:

TEXAS INSTRUMENTS TI-83 Plus

X	Y ₁	Y ₂
70	117438	834.32
80	16004	688.22
90	25582	391.25
100	32615	335.91
110	39981	424.69

$Y_1 = 993.55714000$

Conclusion in words:

At \$0mil spent they will win 51 games
with an error of ± 1 game with a
percent error of 1.5.

Error: Find the error in your x-values:

Now find $f(a)$:

$$y = f(x)$$

$$\Delta x = 0.5$$

$$y(x, x) \cdot 0.5 = 1.72$$

$$y_1 \times 100 = 1.5$$
$$= 1.$$

X	Y2	Y3
65	.50262	1.556
80	.72709	1.67038

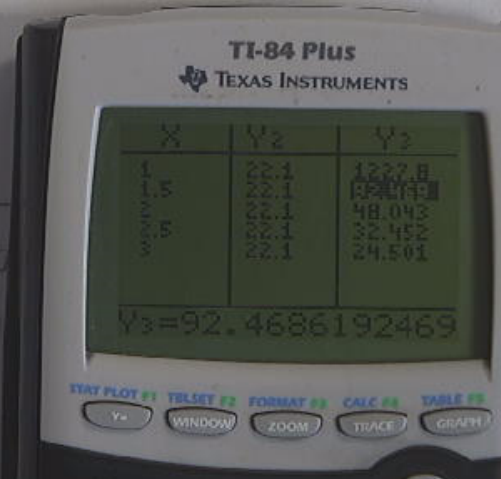
riable): _____

Conclusion in words: After 1 year of being legal, the
weed revenue in taxes is \$22.1 million per
year \pm , 5 years with an error of 1227.8%.

Error: Find the error in your x-values: .5 years

Now find $f'(a)$: \$22.1 million per year

Multiply them:
11.05 million per year



DATE: 3/1/16

Writer: Natna Colombo

x-axis (independent variable): Years

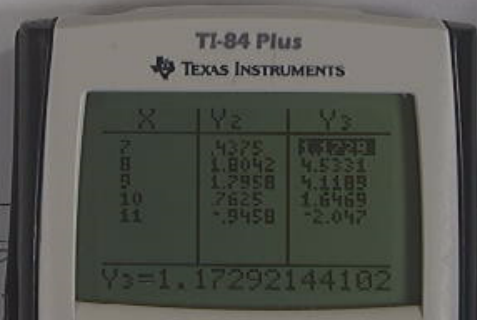
Team Leader: Bill Burrows

y-axis (dependent variable): # of people

Rankita Singha

Conclusion in words:

In 2007, there was 37.3 million people in poverty $\pm 437,500$ with a percent error of 1.17%



13. Error: Find the error in your x-values

$\frac{1}{2}$ Now find f'(a): $\text{nderiv}(Y_1, X_1, X)$

Group Name: Team Xiao

Speaker: 1

DATE: 3/1/16

Writer: Mariam Shah

x-axis (independent variable): years $dx = 0.5 \text{ yr}$

Team Leader: Yvette

y-axis (dependent variable): people

Conclusion in words:

In 2016 according to the exponential regression the population of NJ will be 1.1×10^7 people with an error of ± 62344 & a percent error of 0.57%

13. Error: Find the error in your x-values:

$dx = 0.5 \text{ years}$

Now find $f(a)$:

exponential regression

Multiply them:

$y = a \cdot b^x$