

## Agenda

Quiz 8 Reveiw

Review for Midterm

Lecture Trig Functions and Graphs

Project Sine regression

Quiz 9 Preview

## Review Quiz #8

If  $\theta = \frac{5\pi}{6}$ , find the exact value of each expression below.

(a)  $\cos^2\theta = \square$

(b)  $\cos(-\theta) = \square$

(c)  $\cos 2\theta = \square$

NORMAL FLOAT AUTO REAL RADIAN CL

$(\cos(5\pi/6))^2$	.75
$\cos(-5\pi/6)$	-.8660254038
$\sqrt{3}/2$	.8660254038
$\cos(2*5\pi/6)$	.5

If  $\theta = \frac{5\pi}{6}$ , find the exact value of each expression

$\cos(5\pi/6)$	- .8660254038	✓
$\sqrt{3}/2$	- .8660254038	✓

(a)  $\cos^2\theta = \square \rightarrow \left(\cos \frac{5\pi}{6}\right)^2 \rightarrow \left(-\frac{\sqrt{3}}{2}\right)^2 = \frac{3}{4}$

(b)  $\cos(-\theta) = \square$

(c)  $\cos 2\theta = \square$

$\cos\left(-\frac{5\pi}{6}\right) = -\frac{\sqrt{3}}{2}$

$\cos\left(\frac{10\pi}{6}\right) = \frac{1}{2}$

~~$\frac{2\sqrt{3}}{2}$~~

- .707... =  $\frac{\sqrt{2}}{2}$
- 1.414... =  $\sqrt{2}$
- .866... =  $\frac{\sqrt{3}}{2}$
- 1.732... =  $\sqrt{3}$

### Trigonometric functions and special angles: Problem type 3

Find the exact values below. If applicable, tap on "Undefined."

$$\cos \frac{14\pi}{3}$$

cos(14π/3)

-.5

$$\csc(-225^\circ)$$

1/sin(-225°)

1.414213562

√2

1.414213562

## Reciprocal Identities

$$\cos(x) = \frac{1}{\sec(x)}$$



$$\sec(x) = \frac{1}{\cos(x)}$$



$$\csc(x) = \frac{1}{\sin(x)}$$

$$\sin(x) = \frac{1}{\csc(x)}$$



$$\cot(x) = \frac{1}{\tan(x)}$$

$$\tan(x) = \frac{1}{\cot(x)}$$

## Quotient Identities

$y/x$

$$\tan \theta =$$

$$\frac{\sin \theta}{\cos \theta} \quad \begin{array}{l} = y \\ = x \end{array}$$

$$\cot \theta =$$

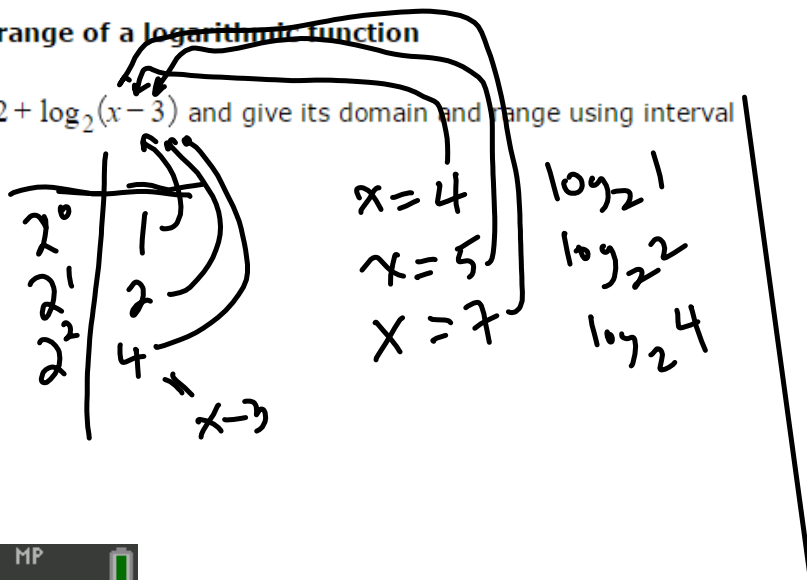
$$\frac{\cos \theta}{\sin \theta}$$

# Review Practice Test



The graph, domain, and range of a logarithmic function

Graph the function  $g(x) = 2 + \log_2(x-3)$  and give its domain and range using interval notation.



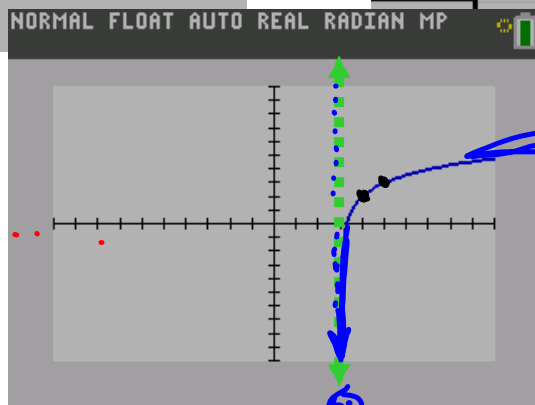
```

NORMAL FLOAT AUTO REAL RADIAN MP
Plot1 Plot2 Plot3
Y1=2+log(X-3)/log(2)
Y2=2+log2(X-3)
Y3=
Y4=
Y5=
Y6=
Y7=
Y8=
Y9=
    
```

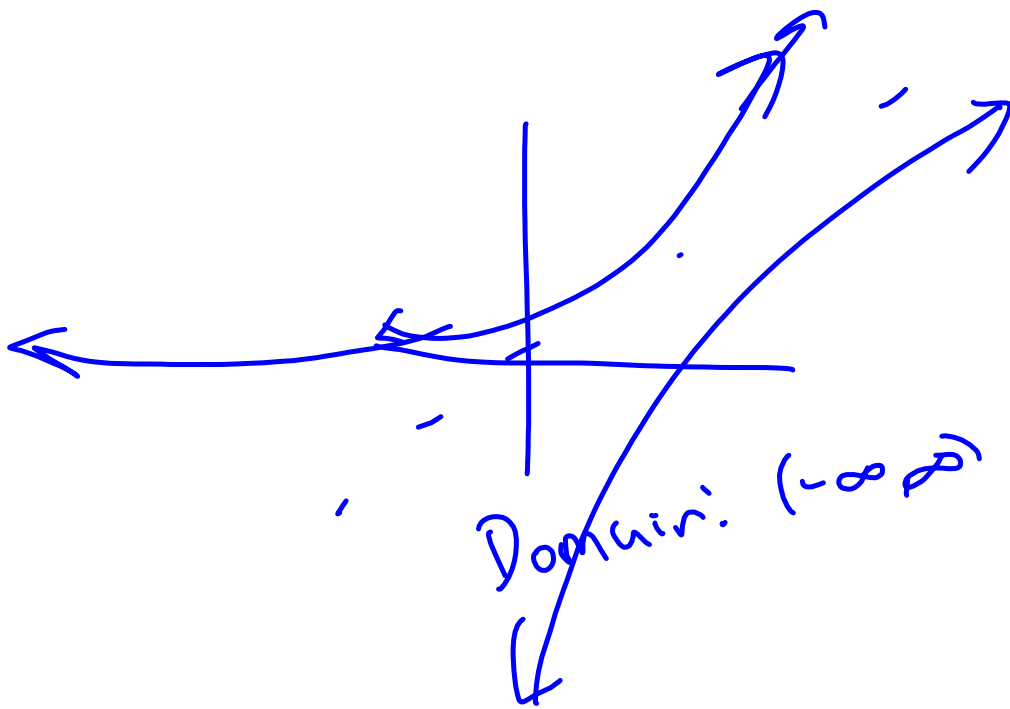
$x-3=0$

X	Y1	Y2
4	2	2
5	3	3
6	3.585	3.585
7	4	4

$x=7$



Domain  $(3, \infty)$   
 Range  $(-\infty, \infty)$



### The graph, domain, and range of a logarithmic function

Graph the function  $g(x) = 2 + \log_2(x-3)$  and give its domain and range using interval notation.

PARENT: log base 2

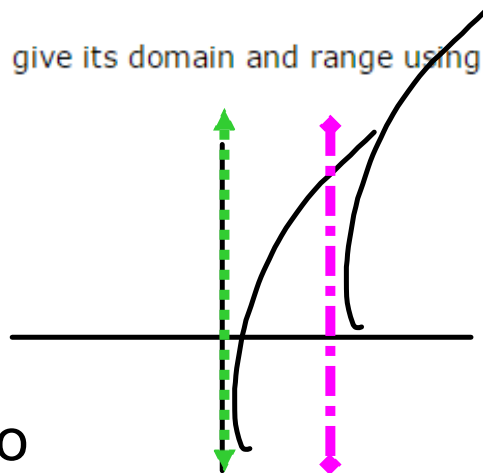
Transformations:

Parenthesis 1st: 3 to the right (move VA 3 to the right)

Addition 2nd: 2 up

calculator:

$$y1=2+\log(x-3)/\log(2)$$

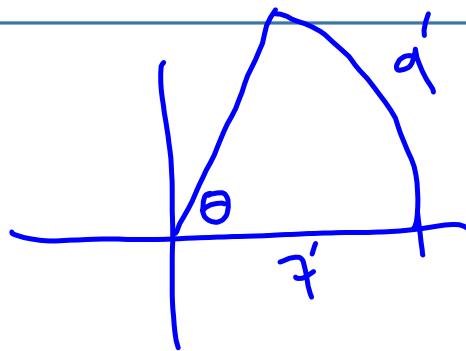


x	y
4	2
5	3
7	4
11	5

### Arc length and central angle measure

A circle has a radius of 7 ft. Find the degree measure of the central angle  $\theta$  that intercepts an arc of length 9 ft.

Do not round any intermediate computations, and round your answer to the nearest tenth.



$$s = r\theta$$
$$9 = 7\theta$$

$$\theta = \frac{9}{7} \text{ radians}$$

$$\frac{9}{7} \cdot \frac{180^\circ}{\pi} = 73.7^\circ$$

### Arc length and central angle measure

A circle has a radius of 7 ft. Find the degree measure of the central angle  $\theta$  that intercepts an arc of length 9 ft.

Do not round any intermediate computations, and round your answer to the nearest tenth.

---

$$S = r \theta$$

$$9 = 7 \theta$$

$$9/7 = \theta$$

To degrees  $\rightarrow$

$$\frac{9}{7} \cdot \frac{180^\circ}{\pi} = \circ$$



9\*180/7/pi  
73.66600223

$$9 \cdot 180 / (7\pi)$$

$$\frac{9 \cdot 180}{7\pi}$$

**Using a calculator to approximate cosecant, secant, and cotangent values**

Use the ALEKS calculator to evaluate each expression.  
Round your answers to the nearest hundredth.

For each expression, make sure you are in the correct calculator mode.

$\cot\left(-\frac{\pi}{8}\right) = \square$	$\rightarrow$	$1/\tan(-\pi/8)$
$\csc(-180^\circ) = \square$	$\rightarrow$	$1/\sin(-180^\circ)$
$\sec 315^\circ = \square$	$\rightarrow$	$1/\cos(315^\circ)$

C S

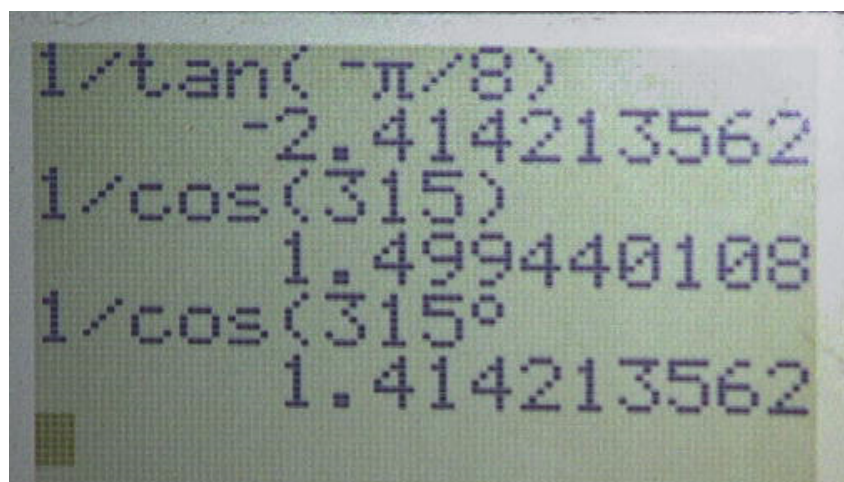
**Using a calculator to approximate cosecant, secant, and cotangent values**

Use the ALEKS calculator to evaluate each expression.  
Round your answers to the nearest hundredth.  
For each expression, make sure you are in the correct calculator mode.

$$\cot\left(-\frac{\pi}{8}\right) = \square$$

$$\csc(-180^\circ) = \square$$

$$\sec 315^\circ = \square$$



## Lecture: Trig Functions and Graphs

$$\begin{aligned}x &= \pi \\ \text{Identity } x &= x \\ x &= x + 1\end{aligned}$$

$$f(x) = \frac{\sin x}{\cos x}$$

Polynomial  $\rightarrow$  Disco/Parab  
Zero/Intercept

Rational  $\rightarrow$  Asymptotes

Exponential

Logarithmic

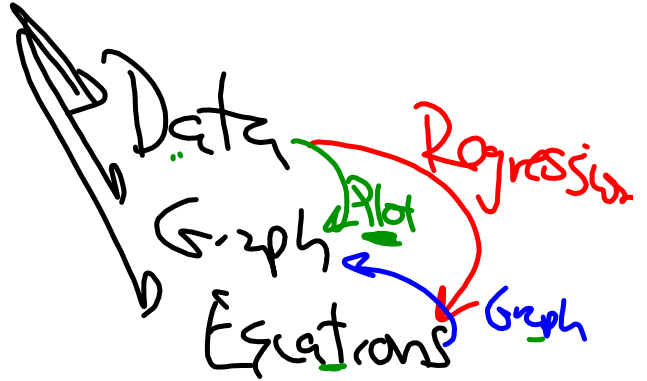
Trig sine, cosine, TANGENT  
csc, sec, cot

compose, Translation, Inverse  
Identities



# Functions\*

Job →  
In → Domain  
Out → Range



→ Transformations

→ Inverses

solve for x  
switch x & y  
 $(f \circ f^{-1})(x) = x$

→ Properties

- Polynomials  $\left\{ \begin{array}{l} \text{Zeros} \\ \text{End Beh} \end{array} \right.$
- Ration  $\left\{ \begin{array}{l} \text{Zeros} \\ \text{HA, SA} \\ \text{VA} \end{array} \right.$
- Exp  $\left\{ \begin{array}{l} \text{HA} \\ \text{Exp graph} \\ \text{Formulas} \end{array} \right.$
- Log  $\rightarrow$  5  $\left\{ \begin{array}{l} 1. \text{ Def} \\ 2. \text{ Sum/Prod} \\ 3. \text{ Ladder} \\ 4. \text{ COB} \\ 5. \text{ LOBS} \end{array} \right.$

# Polynomials

Domain:  $(-\infty, \infty)$

Range: Graph

Transformation  $y = \frac{1}{2}(x+3)^{-2}$

Parent:  $x^2$       Left 3  
Stretch  $1/2$   
Down 2

Inverse: solve for  $x$   
with  $x$  &  $y$

Data  $\rightarrow$   
Line  
Parabola  
Cubic  
Quartic

Props

Zeros = Degree

Faces  $\leq$  Degree

Max/Min

Increase/Decrease

END Diso/Points.

# Rational

Domain: Can't Divid by 0

Range: Graph (or Domain of Inverse)

Transfer.  $Y = \frac{1}{x+2} + 3$

Parent:  $1/x$

Left 2

Up 3

Inverse: Solve for  $x$   
swik  $x$  &  $y$

## Properties

- Zeros (Touch/Pass)
- V.A (Asint/Volc)
- End Behvi
- HA, O, SA

# Trig Functions SINE

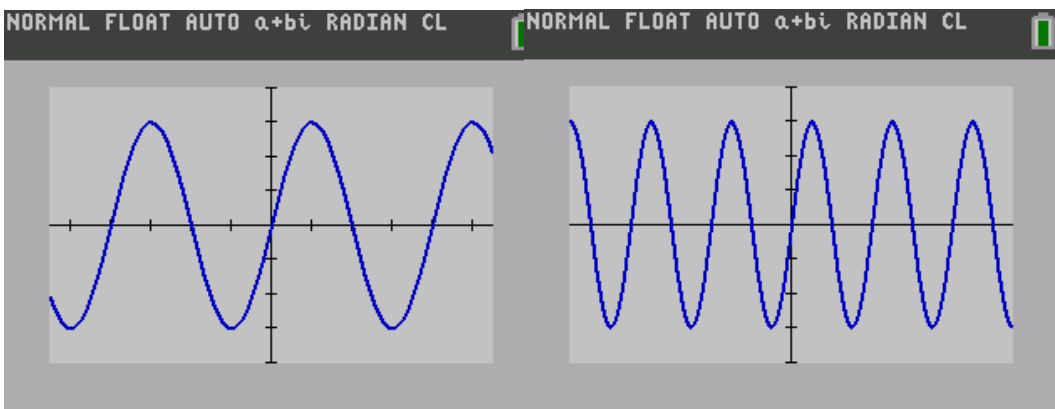
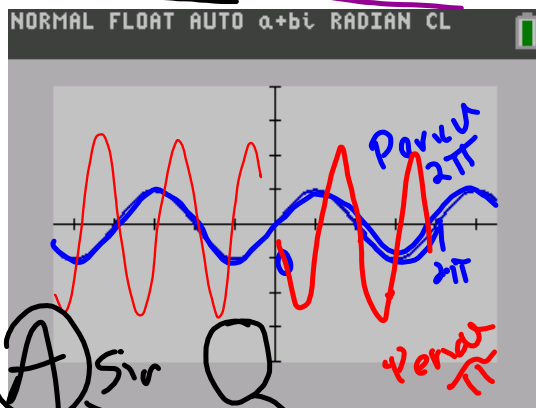
Domain: All Real

Range:  $[-1, 1]$

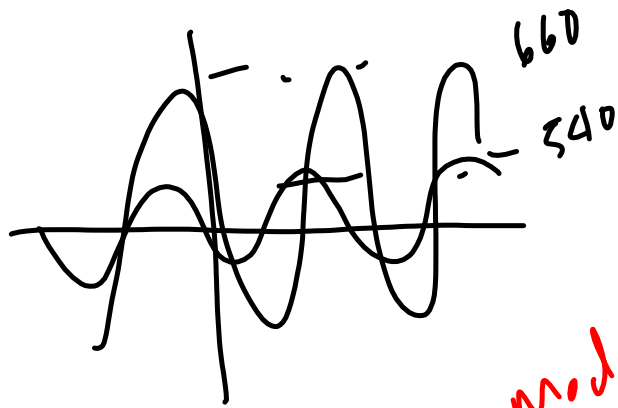
Transformations

$$y = A \sin(Bx + C)$$

$A$  → Amplitude: (stretch)  $|A|$  always +  
 $B$  → Period  $|2\pi/B|$  (Squish/Pull)  
 $C$  → Phase Shift:  $-C/B$  (Left/Right)

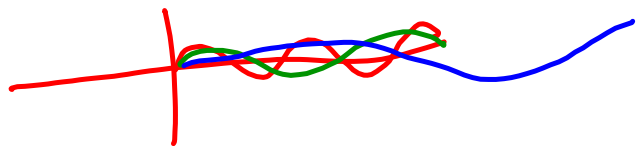


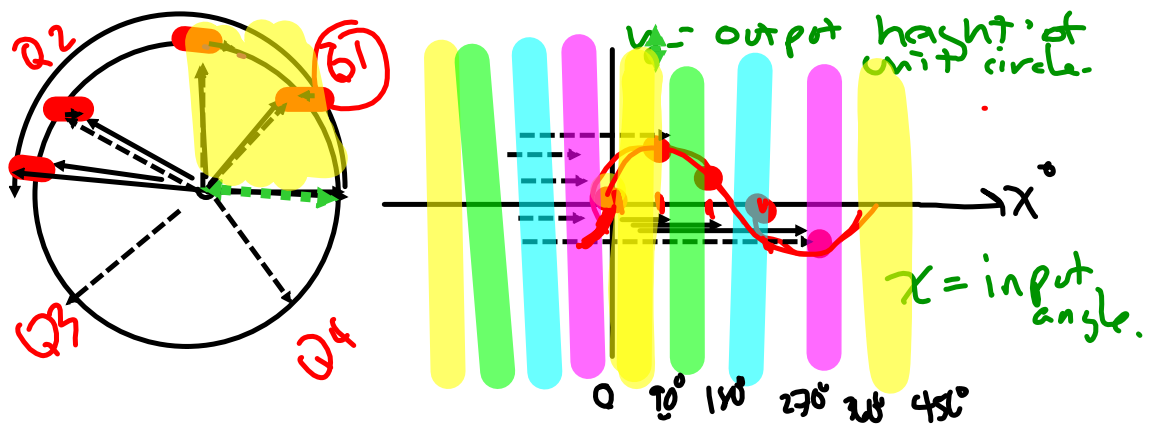
AM  
Amplitude Modulation



FM

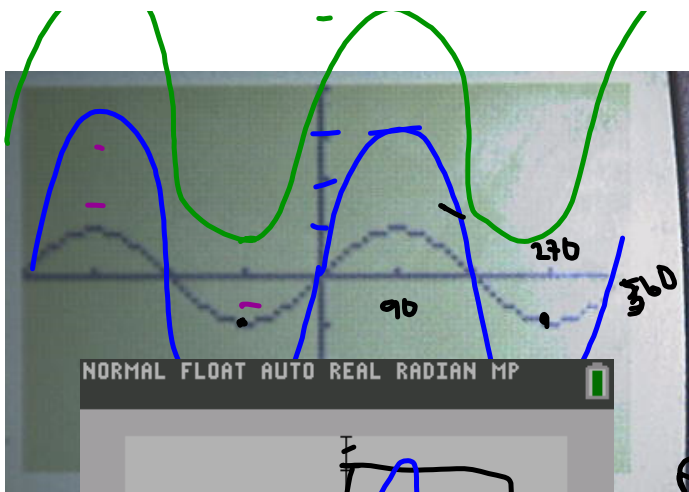
Frequency Modulation  
(Periodic modulation)





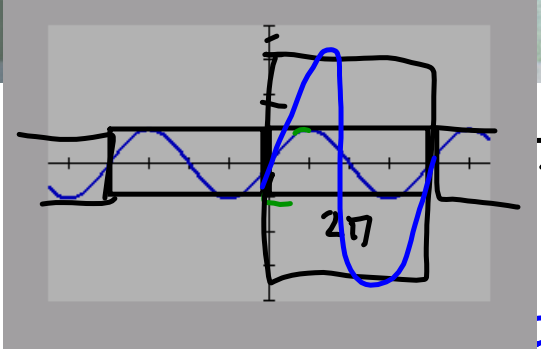
$$y = (\text{x-value on unit circle}) = \cos(t)$$





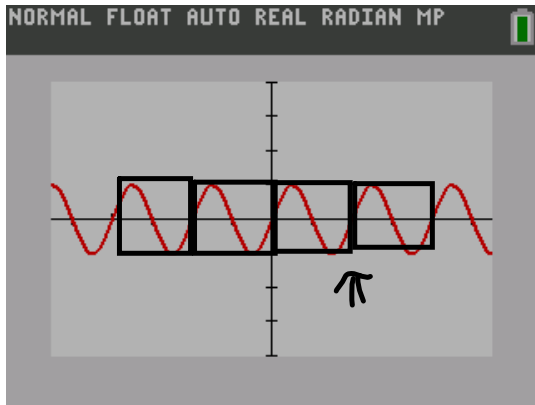
u.p.i.g

Sine  
 period =  $360^\circ$   
 degrees or  $2\pi$   
 or  $2\pi$  radians



$= \sin x$

$d = 3 \sin x + 3$



Period

$$2 \cdot \frac{\pi}{2} = \underline{\underline{\pi}}$$

$$\frac{2\pi}{B} = \pi$$

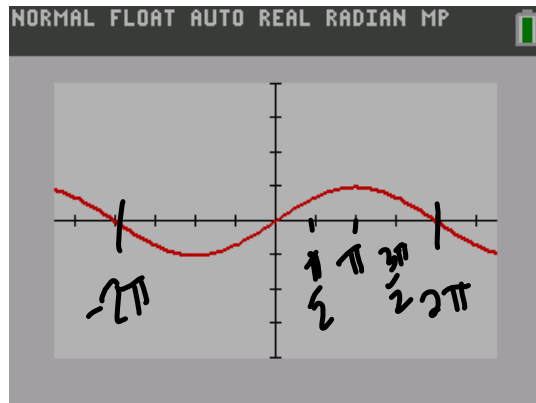
$$B = 2$$

$$\sin(Bx)$$

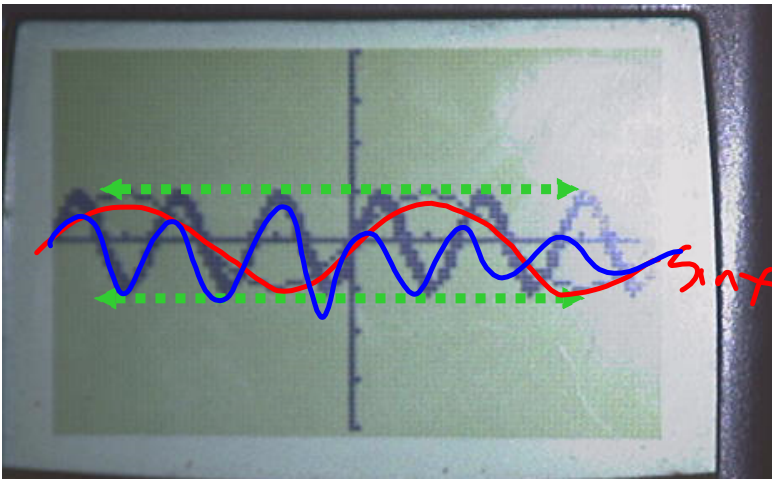
Period:  $2\pi/B$

B	Period
1	$2\pi$
2	$\pi$
4	$\pi/2$

If  $B = 1/2$  Period  $\frac{2\pi}{1/2}$   
 $4\pi$







$$\sin(3x)$$

"smushed"  
busier

$$y = x^2$$

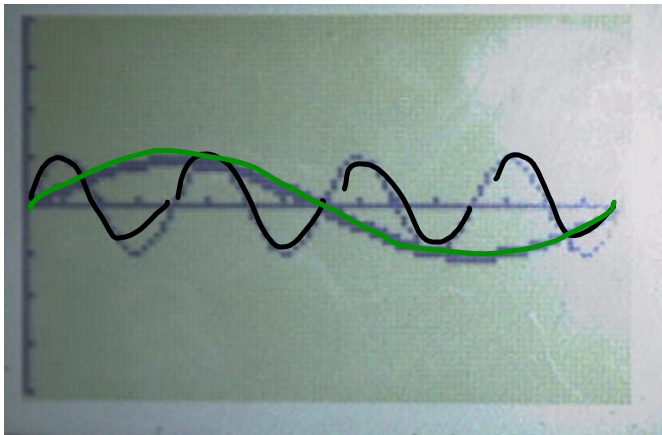
$$y = (3x)^2$$

smushed

$$= 9x^2$$

stretche

$$\sin(.25x)$$



period  $2\pi/B$

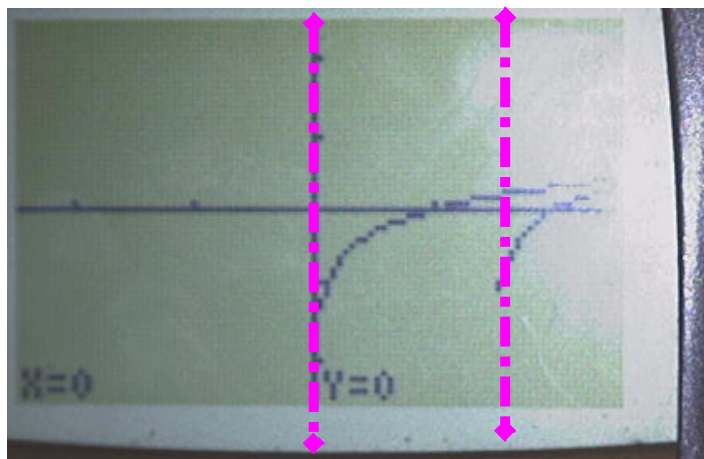
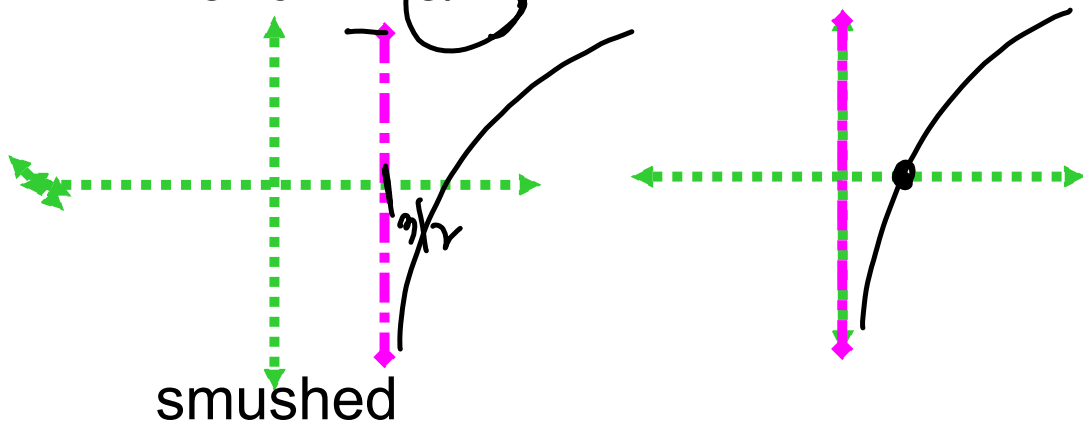
$$2\pi/.25 = 8\pi$$

4 times bigger than  
regular sine

"Lazier"

$y = \log(2x-3)$  has VA at  $\underline{2x-3=0}$   $\log(x)$  has VA at  $x=0$

$2x-3=0 \quad x = \frac{3}{2}$



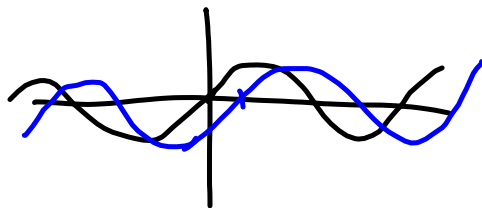
$$\sin(4x - 3)$$

Phase shift

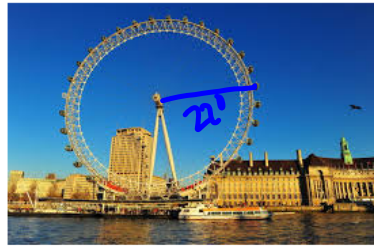
$$4x - 3 = 0$$

$$4x = 3$$

$$x = \frac{3}{4}$$

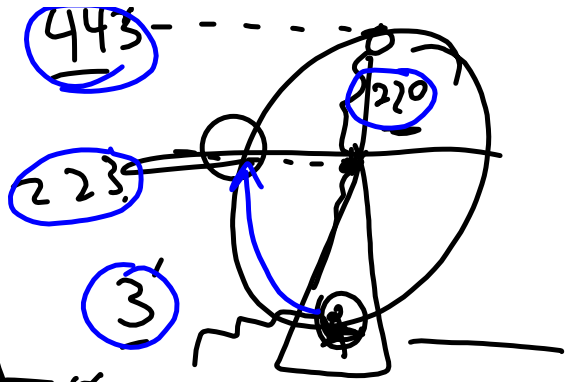
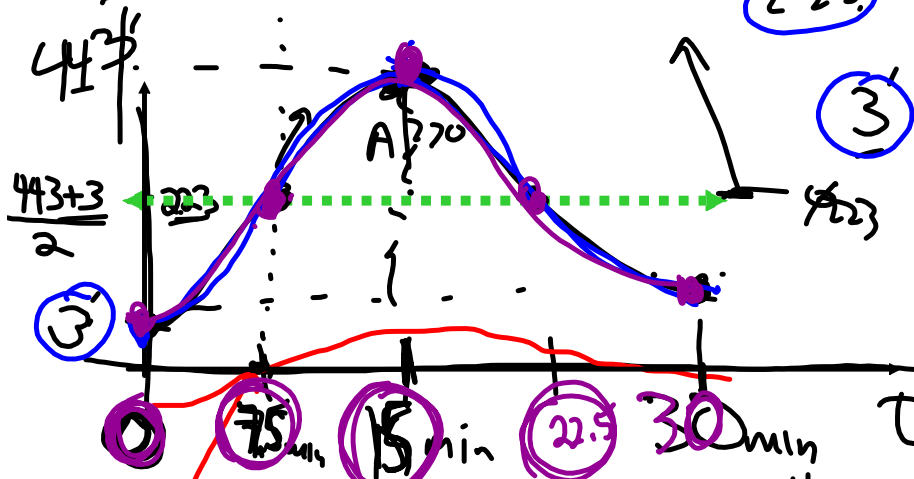


# London Eye



9:08 PM

# London Eye



$$y = A \sin(Bx + C) + D$$

Phase shift

Amplitude:  $\frac{\text{MAX} - \text{MIN}}{2} = \frac{443 - 23}{2} = 220 = A$

Period:  $30 \text{ mins.} = \frac{2\pi}{B}$

Vertical shift:  $223 = D$

Phase Shift:  $7.5 = \frac{C}{B}$

$$C = -7.5B$$

$$C = -7.5(2\pi) = -15\pi \dots$$

$$\begin{aligned} \sin(x) &= \sin(x + 2\pi) \leftarrow \\ &= \sin(x - 2\pi) \leftarrow \\ &= \sin(x - 8\pi) \leftarrow \end{aligned}$$

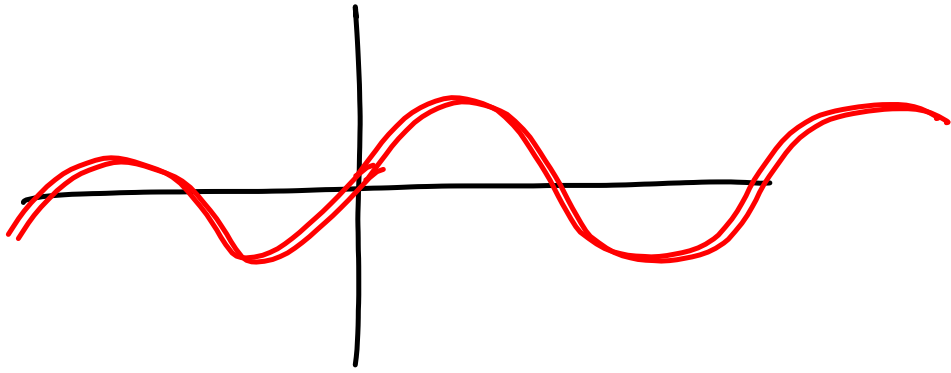
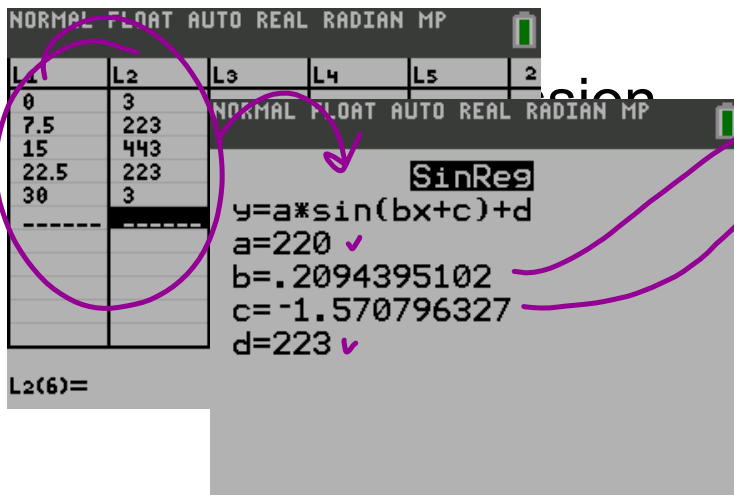


Table → Data 

time	height
0	3
7.5	223
15	443
22.5	223
30	3

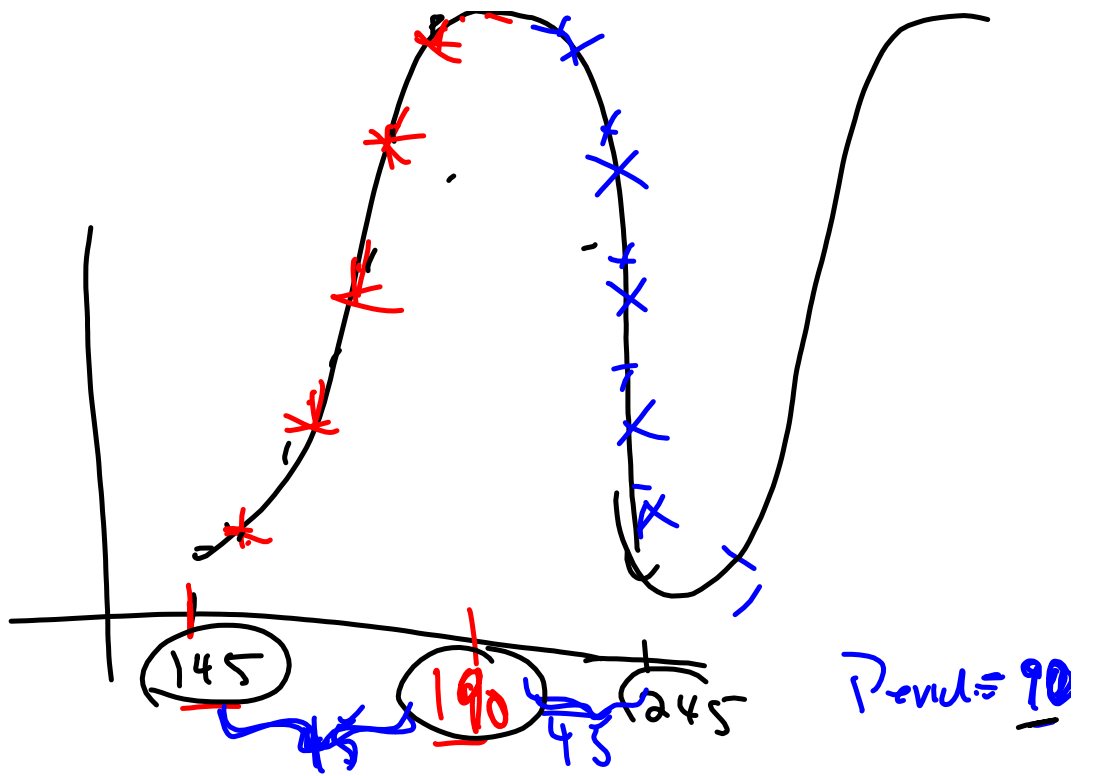


The image shows a TI-84 Plus calculator screen. On the left, a table is displayed with two columns: L1 and L2. The data points are: (0, 3), (7.5, 223), (15, 443), (22.5, 223), and (30, 3). The table is circled in purple. To the right of the table, the SinReg function is shown with the following results:  $y = a \sin(bx + c) + d$ ,  $a = 220$  ✓,  $b = .2094395102$ ,  $c = -1.570796327$ , and  $d = 223$  ✓. Handwritten purple arrows point from the SinReg results to the table and to the handwritten equations on the right.

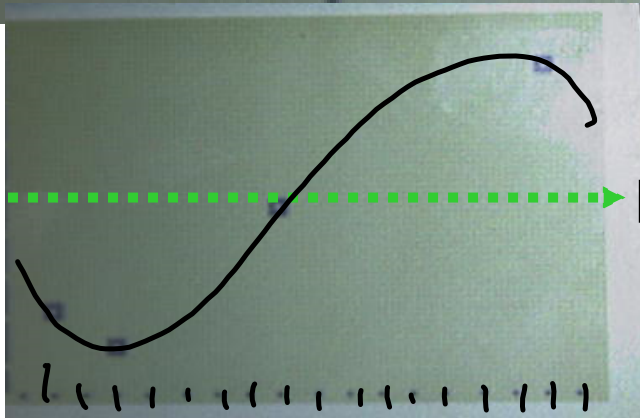
$\cdot 2044 = \frac{1}{15} \pi$

$\rightarrow 1.57 = \frac{\pi}{2}$

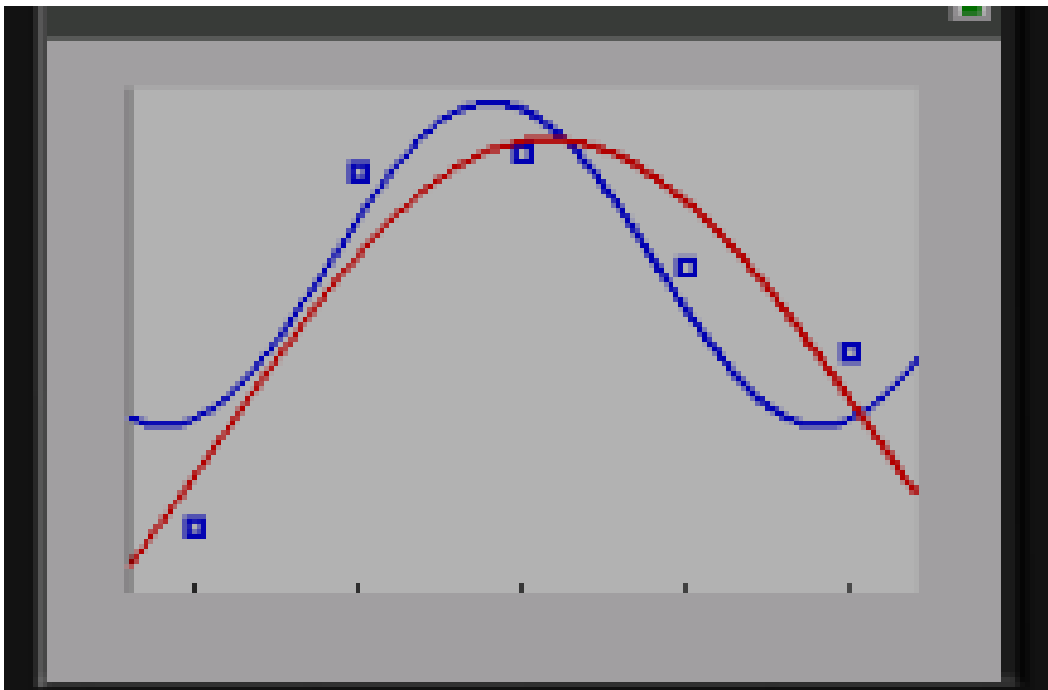


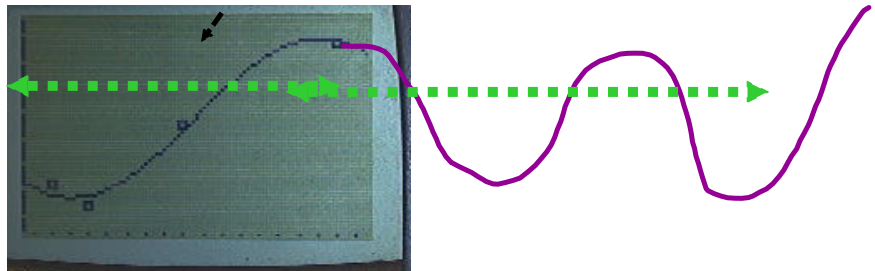
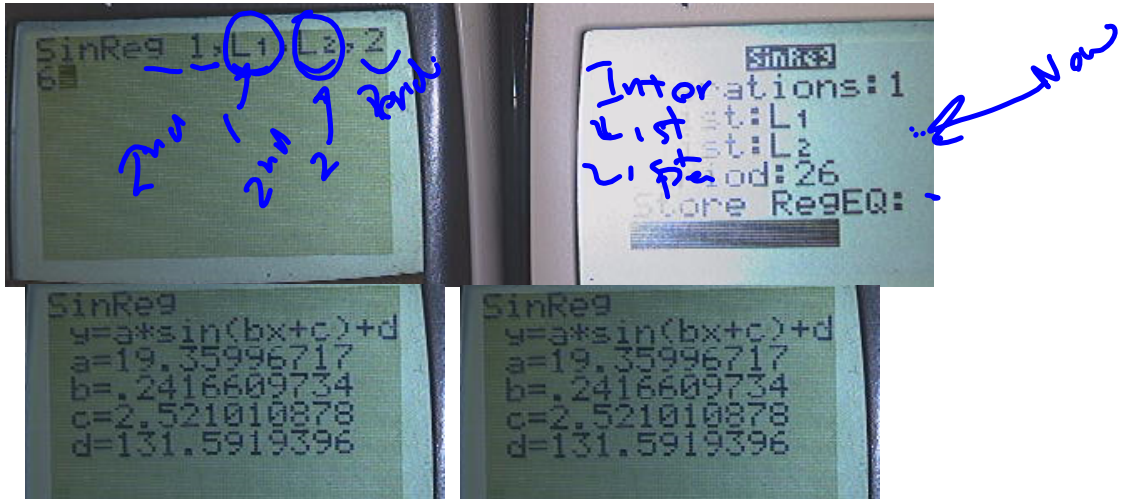


75	1450
60	115
62	110
67	130



Period??? = 7





math 0: solver

0= var 5: >> 1:

minus y (alpha 1)

## Project: Sine Regression

## Ideas for individual Project (9 data points)

Interesting

Relevant

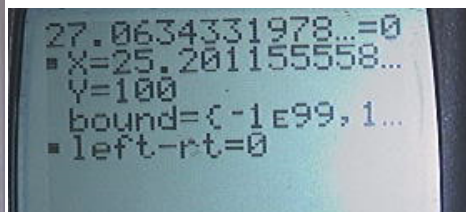
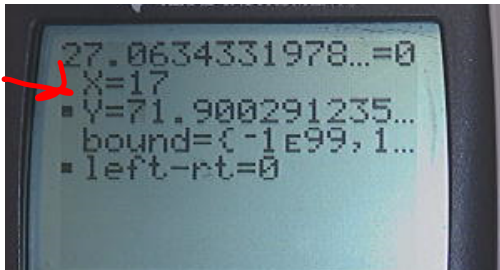
Informative



font  
44 | 50 |

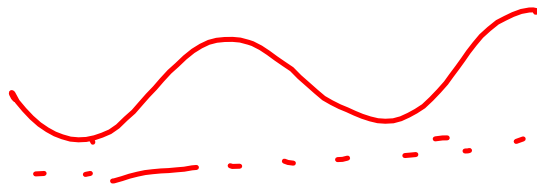
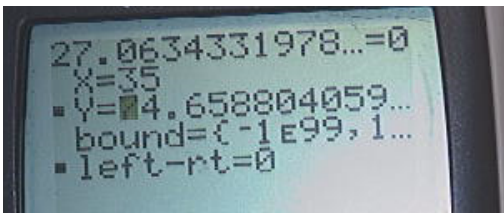
According to the sine regression, <sup>W of 4P of 80</sup>  
Apple stock will cost \$72 August 2017.

Conner



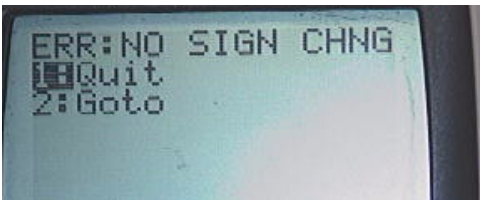
Daisy

The stock will be 100 in 2025.



Hope says in 2035 stock will be worth \$74.65

Maddie says the price of apple stock is \$55 in NEVER





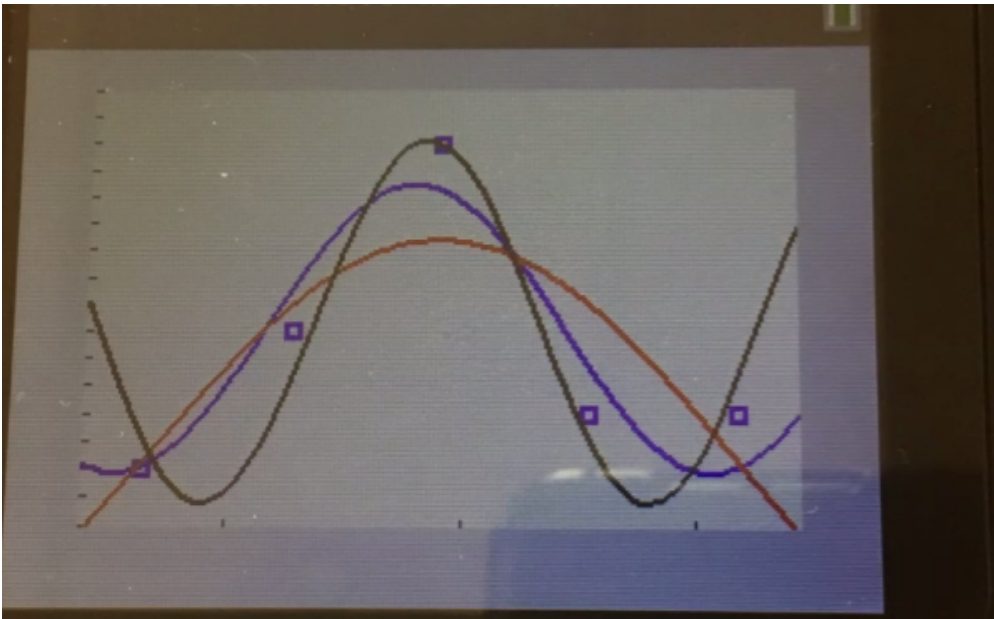
According to the sine regression with period of 7,

6.6 drinks gets 5.6 encounters according to Sine regression with period of 7, to get 3 encounters, I can only drink 2.8 drinks

```
SOLUTION IS MARKED *  
4.3422872756748*sin(0.897▶  
X=0  
▪ Y=■.0580156715537  
bound={ -1E99, 1E99}  
▪ E1-E2=0
```

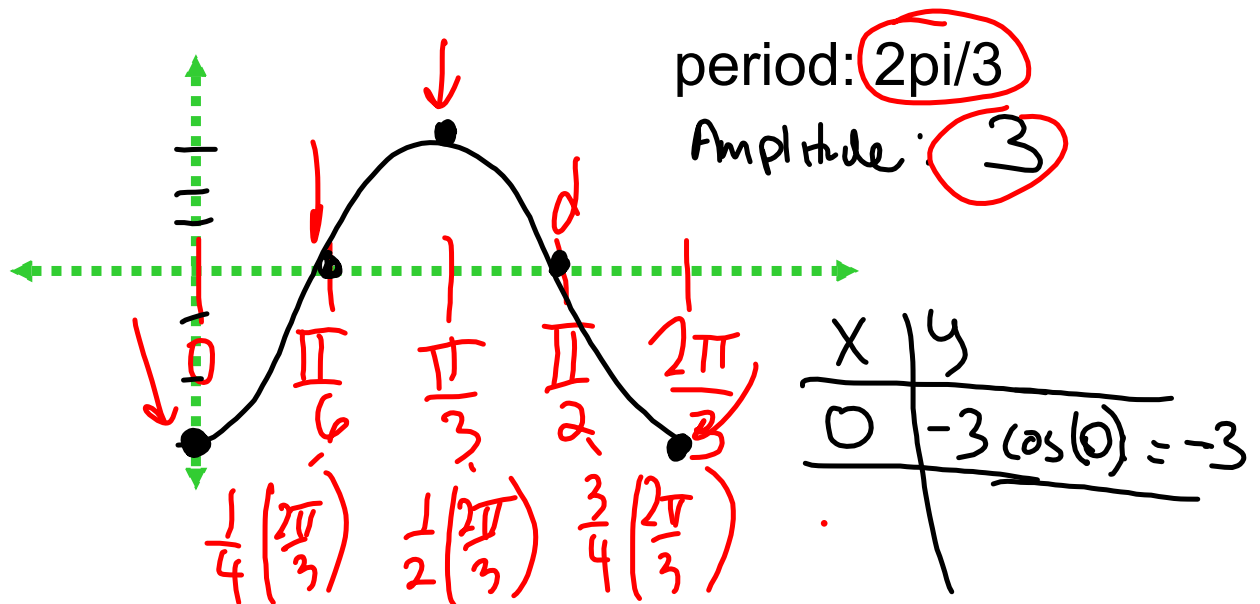
according to the sine regression with a period of 7, a person who does not drink can expect 4 encounters

## Quiz 9 : Preview



Sketching the graph of a sine or cosine function: Problem type 2

Graph the function  $y = 3 \cos 3x$ .



**Matching graphs and equations for secant, cosecant, tangent, and cotangent functions**

Three graphs are given below.  
For each, choose its equation from the following.

$y = 2 \csc x$

$y = 2 \sec \frac{x}{2}$

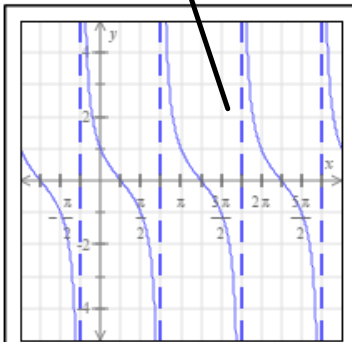
$y = 2 \sec x$

$y = \cot \left( x + \frac{\pi}{4} \right)$

$y = \cot \frac{x}{2}$

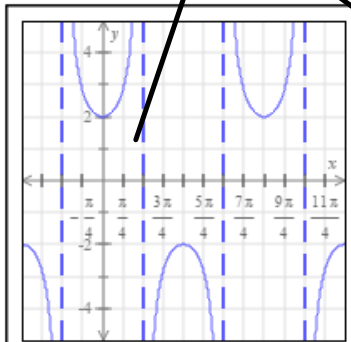
$y = \tan \frac{x}{2}$

*Handwritten notes:*  
 $\frac{1}{\sin}$   
 $\frac{1}{\cos}$



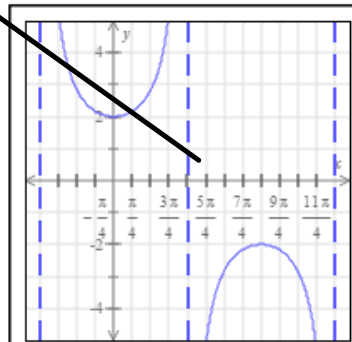
Equation:

(choose one) ▼



Equation:

(choose one) ▼



Equation:

(choose one) ▼

**Matching graphs and equations for secant, cosecant, tangent, and cotangent functions**

Three graphs are given below. For each, choose its equation from the following.

*sin(x)*  
 $y = 2 \csc x$

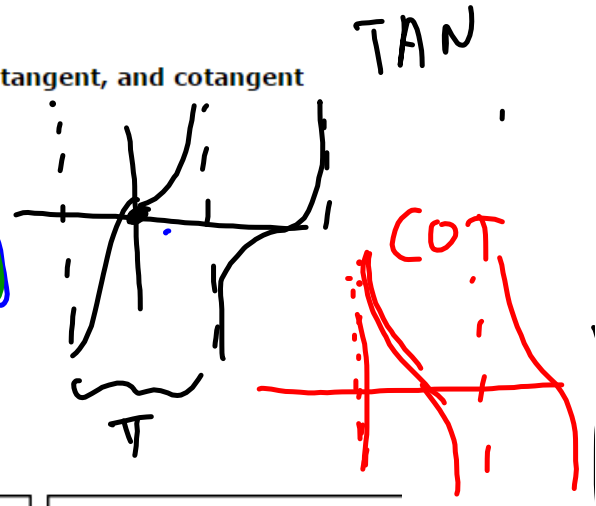
$y = 2 \sec \frac{x}{2}$

$y = 2 \sec x$

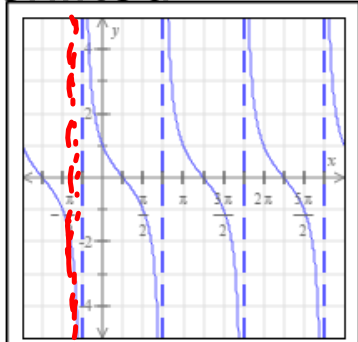
$y = \cot \left( x + \frac{\pi}{4} \right)$

$y = \cot \frac{x}{2}$

~~$y = \tan \frac{x}{2}$~~

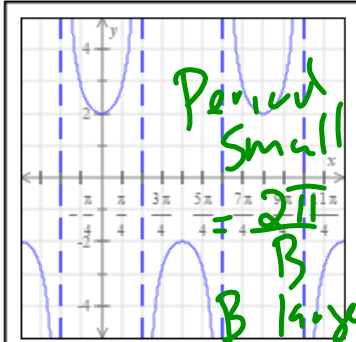


shifted



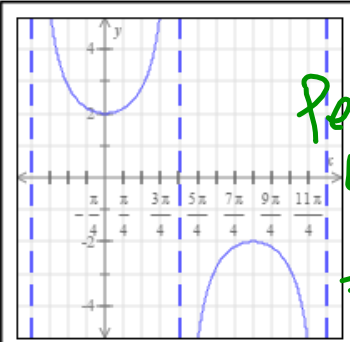
$y = 1/\tan(x + \pi/4)$

Equation:



$y = 2/\cos(x)$

Equation:



$y = 2/\cos(x/2)$

Equation:

Plot1 Plot2 Plot3  
  $y_1 = 2/\cos(x)$   
  $y_2 = 2/\cos(x/2)$

