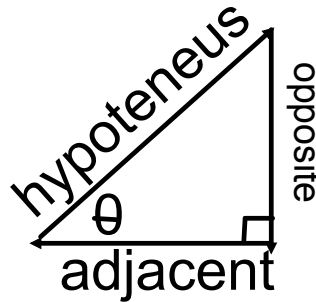
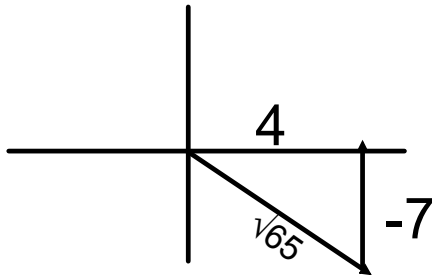


Finding values of trigonometric functions given information about an angle: Problem type 1

Let $(4, -7)$ be a point on the terminal side of θ .

Find the exact values of $\sin\theta$, $\sec\theta$, and $\tan\theta$.



$$4^2 + 7^2 = h^2$$

$$16 + 49 = 65 = h^2$$

$$\text{soh} = \frac{\text{opp}}{\text{hyp}} = \frac{-7}{\sqrt{65}}$$

$$\sec\theta = 1/\cos\theta = \text{hyp}/\text{adj} = \sqrt{65} / 4$$

Values of inverse trigonometric functions

Find the exact value of $\tan^{-1}\left(-\frac{\sqrt{3}}{3}\right) = \theta$

Write your answer in radians in terms of π .

| X | tan X |
|-----|-------|
| 0 | 0 |
| 45° | 1 |
| 90° | und. |

| X | tan ⁻¹ |
|---|-------------------|
| 0 | 0° |
| 1 | 45° |

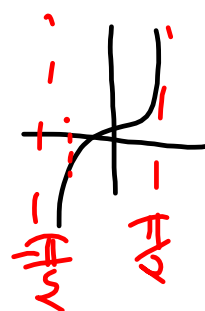
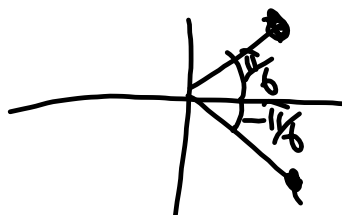


$$-30^\circ \cdot \frac{\pi}{180} = -\frac{\pi}{6}$$

$$\tan\theta = -\frac{\sqrt{3}}{3}$$

| | 0 | $\pi/6$ | $\pi/4$ | $\pi/3$ | $\pi/2$ |
|-----|---|--------------|--------------|--------------|--------------|
| sin | 0 | $\sqrt{1}/2$ | $\sqrt{2}/2$ | $\sqrt{3}/2$ | $\sqrt{4}/2$ |
| cos | 1 | $\sqrt{3}/2$ | $\sqrt{2}/2$ | $1/2$ | 0 |
| tan | 0 | $1/\sqrt{3}$ | 1 | $\sqrt{3}$ | ∞ |

$$\tan \frac{\pi}{6} = \frac{\sqrt{3}}{3}$$



Simplifying trigonometric expressions

Simplify.

$$\tan x \csc x$$

Convert to $\sin x, \cos x$

Use algebra and the fundamental trigonometric identities.

Your answer should be a number or use a single trigonometric function.

$$\tan x = \frac{\sin x}{\cos x}$$

$$\csc x = \frac{1}{\sin x}$$

$$\tan x \csc x = \frac{\sin x}{\cos x} \cdot \frac{1}{\sin x} = \frac{1}{\cos x} = \sec x$$

Equations have equal signs

3 possibilities:

age = 45 True on the Condition

age = age + 1 Never! Contradiction

age = age Always! Identity

$$\tan x = \sin x / \cos x$$

$$1 = \cot x * \tan x$$

Reciprocal identities:

$$\sin u = \frac{1}{\csc u} \quad \cos u = \frac{1}{\sec u} \quad \tan u = \frac{1}{\cot u}$$

$$\csc u = \frac{1}{\sin u} \quad \sec u = \frac{1}{\cos u} \quad \cot u = \frac{1}{\tan u}$$

Quotient identities:

$$\tan u = \frac{\sin u}{\cos u} \quad \cot u = \frac{\cos u}{\sin u}$$

Pythagorean identities:

$$\sin^2 u + \cos^2 u = 1$$

$$\tan^2 u + 1 = \sec^2 u$$

$$\cot^2 u + 1 = \csc^2 u$$

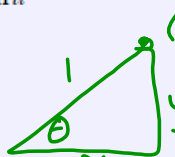
Handwritten notes:

Know (x, y) exist

$$\div \cos^2 u \rightarrow \tan^2 u + 1 = \sec^2 u$$

$$\div \sin^2 u \rightarrow 1 + \cot^2 u = \csc^2 u$$

PROOF



$x^2 + y^2 = 1$

$\sin^2 \theta + \cos^2 \theta = 1$

$$(\sin \theta)^2 = \sin^2 \theta$$

$$\sin(\theta^2) = \sin \theta^2$$

| Statement |
|------------------------------------------------------------------------|
| $(1 + \cot^2 x) \tan x$ |
| $= (\csc^2 x) \tan x$ |
| $= \left(\frac{1}{\sin^2 x}\right) \tan x$ |
| $= \left(\frac{1}{\sin^2 x}\right) \left(\frac{\sin x}{\cos x}\right)$ |
| $= \left(\frac{1}{\sin x}\right) \left(\frac{1}{\cos x}\right)$ |
| $= \csc x \sec x$ |

$$1 + \cot^2 x = \csc^2 x$$

Pythagorean Id.

$$\csc^2 x = \frac{1}{\sin^2 x}$$

Reciprocal

$$\tan x = \frac{\sin x}{\cos x}$$

Quotient

Algebra

Reciprocals

Day 19 - Question #4;
Verifying a trigonometric identity

Complete the proof of the identity by choosing the Rule that justifies each step.

$$(1 - \cos^2 x) \sec x = \sin x \tan x$$

| Statement | Rule |
|-----------------------------------------------|--------------------|
| $(1 - \cos^2 x) \sec x$ | |
| $= \sin^2 x \sec x$ | <u>Pythagorean</u> |
| $= \sin^2 x \left(\frac{1}{\cos x}\right)$ | <u>Reciprocal</u> |
| $= \sin x \left(\frac{\sin x}{\cos x}\right)$ | <u>Algebra</u> |
| $= \sin x \tan x$ | <u>Quotient</u> |

Prove the identity.

$$\cot x (\sec^2 x - 1) = \tan x$$

| Statement | Rule |
|------------------------------------------------|-------------|
| $\cot x (\sec^2 x - 1)$ | |
| $= \cot x (\tan^2 x)$ | Pythagorean |
| $= \left(\frac{1}{\tan x} \right) (\tan^2 x)$ | Reciprocal |
| $= \tan x$ | Algebra |

Thank you, your proof is complete; Click on **Done** below to submit your answer.

Day 19 - Question #7;
Proving trigonometric identities: Problem type 2

Prove the identity.

$$\sec x - \sin x \tan x = \cos x$$

| Statement | Rule |
|-----------------------------------------------------|-------------|
| $\sec x - \sin x \tan x$ | |
| $= \frac{1}{\cos x} - \sin x \tan x$ | Reciprocal |
| $= \frac{1}{\cos x} - \sin x \frac{\sin x}{\cos x}$ | Quotient |
| $= \frac{1 - \sin^2 x}{\cos x}$ | Algebra |
| $= \frac{\cos^2 x}{\cos x}$ | Pythagorean |
| $= \cos x$ | Algebra |

Day 19 - Question #8;
Proving trigonometric identities: Problem type 3

Prove the identity.

$$\frac{\cos x}{1 + \sin x} = \frac{1 - \sin x}{\cos x}$$

| Statement | Rule |
|-------------------------------------------------------------|-------------|
| $\frac{\cos x}{1 + \sin x}$ | |
| $= \frac{\cos x}{1 + \sin x} \frac{1 - \sin x}{1 - \sin x}$ | Algebra |
| $= \frac{\cos x}{1 - \sin^2 x} \frac{1 - \sin x}{1}$ | Algebra |
| $= \frac{\cos x}{\cos^2 x} \frac{1 - \sin x}{1}$ | Pythagorean |
| $= \frac{1 - \sin x}{\cos x}$ | Algebra |