



$$\int_1^{27} \frac{X^{4/3} - X^{-2}}{f(x)} dx$$
$$\frac{X^{4/3}}{4/3} - \frac{X^{-1}}{-1} \Big|_1^{27} = F(27) - F(1)$$

$$\left(\frac{3}{4} (27)^{4/3} + 27^{-1} \right) - \left(\frac{3}{4} + 1 \right)$$

$F(27) \qquad \qquad \qquad F(1)$

$$\frac{3}{4} \cdot 81 + \frac{1}{27} - \frac{7}{4} = \frac{1594}{27}$$

$59 \frac{1}{27}$

Position, $S(t)$

$$\text{Velocity } v(t) = \frac{d}{dt} S(t) = S'(t)$$

$$\text{Acceleration } a(t) = \frac{d}{dt} \frac{d}{dt} S(t) = S''(t)$$

$$\frac{d}{dt} v(t).$$

Initial Value Problem

$$\text{Velocity} = 20 - \cos t$$

$$S(0) = 2$$

$$s'(t) = 20 - \cos t$$

$$\int s'(t) dt = \int 20 - \cos t dt$$

$$s(t) = 20t - \sin t + C$$

$$S(0) = 20(0) - \sin(0) + C = 2$$

$$0 - 0 + C = 2$$

$$C = 2$$

$$S(t) = 20t - \sin t + 2$$

$$a(t) = 8 - t \quad v(0) = 9 \quad s(0) = 0$$

$$\int a(t) dt = 8t - \frac{t^2}{2} + C_1$$

$$v(t) = 8t - \frac{t^2}{2} + C_1$$

$$v(0) = 0 - 0 + C_1 = 9$$

$$v(t) = 8t - \frac{t^2}{2} + 9$$

$$\int v(t) dt = \frac{8t^2}{2} - \frac{t^3}{6} + 9t + C_2$$

$$s(t) = 0 - 0 + 0 + C_2 = 0$$
$$C_2 = 0$$

$$s(t) = 4t^2 - \frac{t^3}{6} + 9t$$

$\Delta X = \text{error in } x$

\approx differential dx

$\Delta y = \text{exact error in } y$

$\approx dy$

$$dx \frac{dy}{dx} = f'(x) \cdot dx$$

$$dy = f'(x) dx$$

$$\frac{d}{dx} x^2 = 2x$$

$$\frac{d}{dt} x^2 = 2x \cdot \frac{dx}{dt}$$

$$\frac{d}{dx} \ln y = \frac{1}{y} \frac{dy}{dx}$$

$$\frac{d}{dt} x^2 + y^2 = 2x \frac{dx}{dt} + 2y \frac{dy}{dt}$$

differential

$$d x^2 = 2x dx$$

$$d \ln y = \frac{1}{y} dy$$

$$d(x^2 + y^2) = 2x dx + 2y dy$$

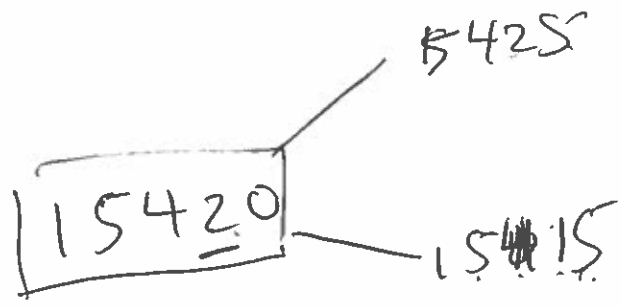
Error.

$$\frac{15500}{15499} \approx 15500$$

15000 people at Mercer.

~~14500~~

15000 ± 500



15420 ± 5

43 yrs. ± .5

Really

43 ± 1

43 ± 10

43.5 ± .5

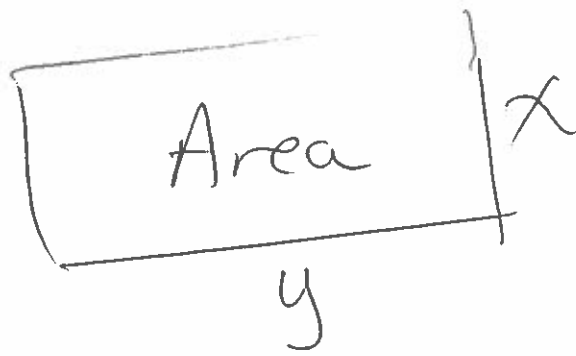
x dx

1970 ± 5

1970.0 ± .05

Given

1970 ± .5



$$A = xy$$

$$x = 2.05 \quad y = 1.7$$

Error! $dx = \pm 0.005 \quad dy = 0.05$

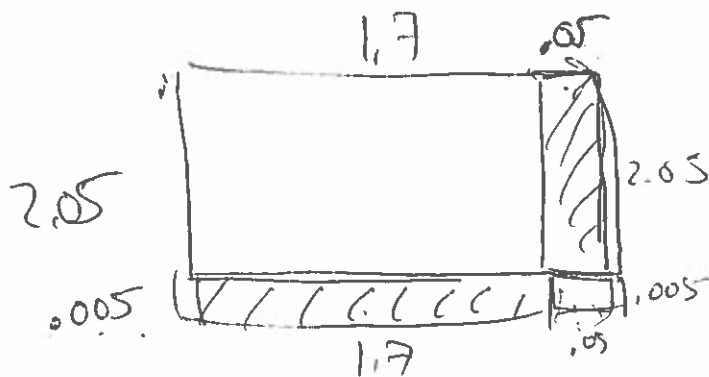
$$\begin{aligned} \text{Area} &= 2.05 \times 1.7 = \\ &= 3.485 \end{aligned}$$

Evaluate Area

Error? $dA = x dy + y dx$

$$= (2.05)(\pm 0.05) + (1.7)(\pm 0.05)$$

$$= .111$$



$$3.485 \pm .111$$

$dA =$ % error

$$\frac{.111}{3.485} \times 100 = 3.18\%$$

$$y = f(x) \text{ at } x = a$$

$$dy = f'(x) \cdot dx$$

$Y_1 =$ Quad Reg.

TABLE

Predict: $X = 2015$ $Y = 23.167$
Error?

Find $\frac{dy}{dx}$ $X = 2015$

$$\frac{dy}{dx} = 22.79 \text{ m}$$

nderiv($Y_1, X, 15$)

$$\text{Error} = f'(15) \times dx$$
$$22.79 \times 0.5 = 11.396$$

~~2015.5 ± 0.5~~
2015 \rightarrow 2016

2015 ± 0.5
2014.5 \rightarrow 2015.5

In 2015 Lady G is

$$\text{Wart} \quad \underline{22.79 \text{ ml}} \pm 11.2$$

$$23. \text{ ml} \pm 11 \text{ ml}$$

90 error 50%

$$11 \frac{\cancel{dx}}{y} \times 100 = 50\%$$

23.

$$23 \text{ ml} \pm 50\%$$

1. evaluate y at $x=a$

2. evaluate y' at $x=a$

3. Evaluate $dx = \pm \frac{1}{2}$ (last digit)

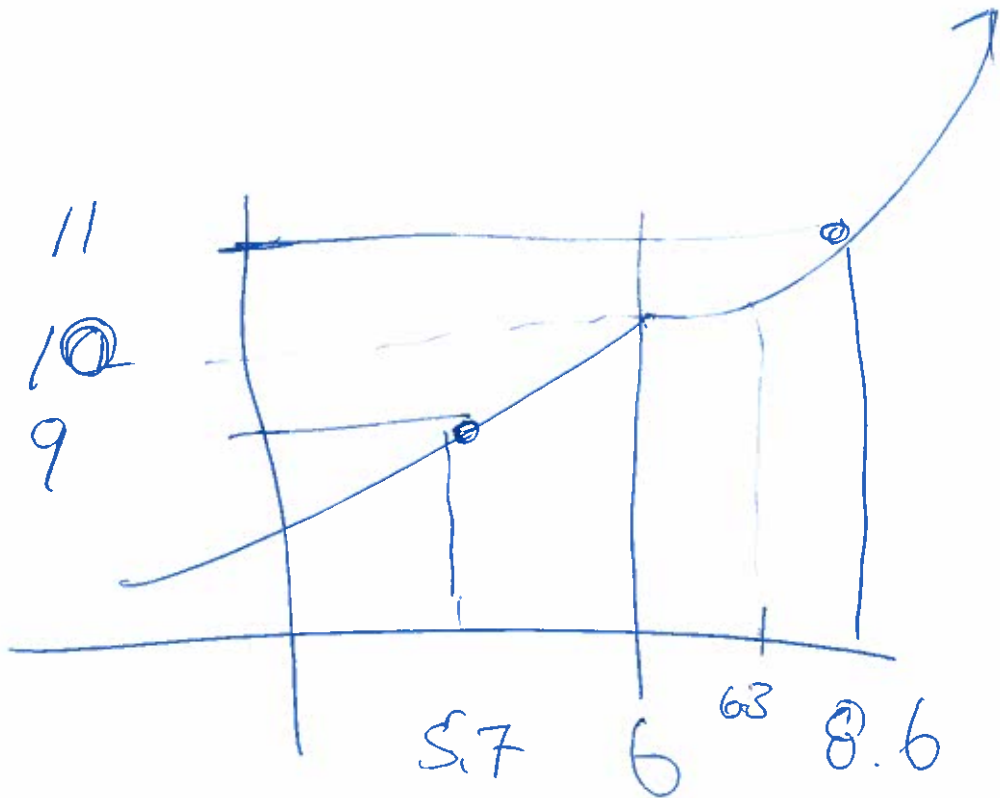
$$4. \quad dy = y'(a) \cdot dx$$

$$3 \text{ say } y(a) \pm dy$$

or

$$y(a) \pm \% \text{ error}$$

$$\rightarrow 2.8 \text{ ml} \pm .96 \text{ } \cancel{.5} .48 \quad 17\%$$



$$E = 1$$

$$\underbrace{5.7 \quad 6 \quad 6.3 \quad 8.6}_{.3 \quad 2.6}$$

$$\delta = .3$$

GROUP NAME: Cha-Ching

Date: 4/21/14

Student Names (First and Last)

Speaker/Presenter: Sheila Mae Gan

Writer/Prep: Freniwot Bekele
~~Sheila Mae Gan~~

Independent Variable (x-axis): Years

Dependant Variable (y-axis): Revenue

Leader/Collaborator: Tatiana Calderon
Trey Murrill

Conclusion (in words):

In 2015 we're expecting to make 289.41669 million \pm 144.708345 million or an error of 50%

Supporting Work:

DATA	
X	Y
13	35
12	27
11	26
10	17
9	16

$Y_1 = \text{Quart Reg}$
 $x = 15 \quad y = 287$

$\frac{dy}{dx} = 289.41669$ $dx = \del{.000005}$

Error of $f'(15) \times dx$
 $289.41669 \times .5$

Error = 289.41669 ± 144.708345

% error $\frac{144.708345}{289.41669} = 50\%$

GROUP NAME:	Student Names (First and Last)
Date: <u>04/21</u>	Speaker/Presenter: <u>Nader Shenouda</u>
Independent Variable (x-axis): <u>time (hours)</u>	Writer/Prep: <u>Karol Zariski</u>
Dependant Variable (y-axis): <u>memory usage (MB)</u>	Leader/Collaborator: _____

Conclusion (in words):

During the 4th hour of use, the memory usage will be 2166.6678752 MB with a % error of 42%.

Supporting Work:

Quartic Regression

Prediction: $x = 4$ $y = 2600$

$y'(4) = 2166.6678752$
~~2600~~

Error = $y'(4) \cdot .5$

$= \frac{1083.333938}{2600} \cdot 100 = 42\%$

$y(4) = 2600 \pm 1080$

$\pm 42\%$ error

GROUP NAME:

Date: _____

Illuminatti

Student Names (First and Last)

Speaker/Presenter: Ryan Piotrowski

Independent Variable (x-axis): _____

Dependant Variable (y-axis): _____

Writer/Prep: _____

Leader/Collaborator: Danyan Zhou

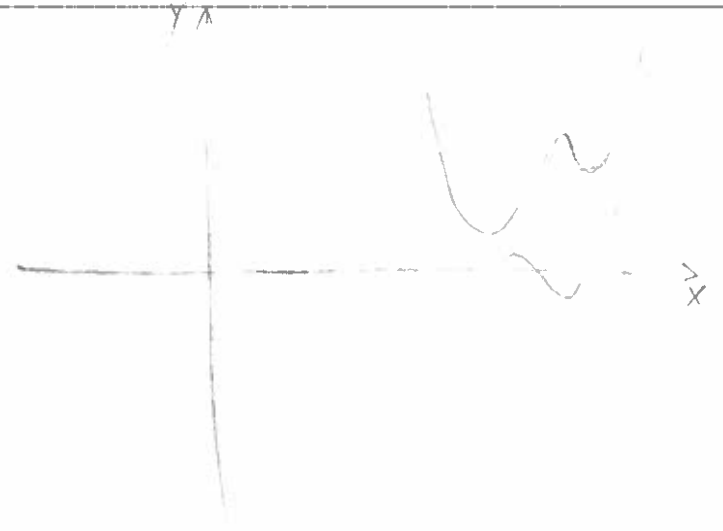
Conclusion (in words):

Gas price in 2008 was \$2.9, the error was 0.2%

Supporting Work:

Year	Price
1999	1
2000	1.54
2001	2.18
2002	3.5
2003	3.2

Quantity



$$x = 108$$

$$y(108) = 3$$

$$y'(108) = 0.0187$$

$$\Delta x = \pm \frac{1}{2} = \pm 0.5 \text{ years}$$

$$dy = y'(a) \cdot dx = 0.0187 \times (\pm 0.5) = \pm 0.00935$$

Error

$$y(108) = 3 \pm 0.00935$$

$$0.24\%$$

GROUP NAME: <u>T rates</u>	Student Names (First and Last)
Date: <u>04/21/2014</u>	Speaker/Presenter: <u>Shanon Tsue</u>
Independent Variable (x-axis): <u>time</u>	Writer/Prep: <u>Onur Turkay</u>
Dependant Variable (y-axis): <u>Guys</u>	Leader/Collaborator: _____

Conclusion (in words): At 7:45pm there will be a 50% chance of no hot guys in the bar between 6:15pm to 8:00pm.

Supporting Work:

Quart Reg:

$$y_1 = \text{Quart reg.}$$

and calc predict at 7:45pm

$$= 4.2196 \longrightarrow 0 \text{ guys}$$

$$n \text{ Deriv } (y_1, x, 19.45)$$

$$- 4.2196 \quad \pm 2 \text{ guys}$$

$$\text{Ans } \times .5$$

$$- 2.10973$$

$$\text{Ans } / - 4.2196$$

$$\cdot 5 \cdot 100$$

$$= 50$$

50% erra.

GROUP NAME: Winnifred
 Date: 4/21/14
 Independent Variable (x-axis): YEARS
 Dependant Variable (y-axis): # of children

Student Names (First and Last)
 Speaker/Presenter: Christina Trujillo
 Writer/Prep: Yamin Silverio
 Leader/Collaborator: _____


Conclusion (in words):

Supporting Work:

X	Y
2004	20771
2005	20734
2006	20580
2007	19602
2008	2662
2009	2319
2010	11058
2011	12744
2012	17466

Quadratic Regression * 2015 = -4.29651406Eai
 $n(x,y) = -1.05247444E15 x .5$
 $= -5.262372E11$

$$\frac{-1.05247444E15 \times 100}{-5.262372E11} = 200\%$$

<p>GROUP NAME: <u>3 + friends</u></p> <p>Date: _____</p> 	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Vince</u></p> <p>Writer/Prep: <u>Vince</u></p> <p>Leader/Collaborator: <u>Vince</u></p>
<p>Independent Variable (x-axis): _____</p> <p>Dependant Variable (y-axis): _____</p>	

Conclusion (in words):

Supporting Work:

$100 = 1.653$
 Prediction = $x = 0.20 \quad y = 7.6 = 3$
 $\frac{dy}{dx} = 0.6$
 $\frac{dy}{dx} = 0.6$
 $100 = 50(2.00) \times 100$
 $69.80(0.5) = 34.90$
 $\frac{34.90}{1.653} (100) = 2109\%$
 7600 ± 30
 $0.1100 \approx 0.11\%$

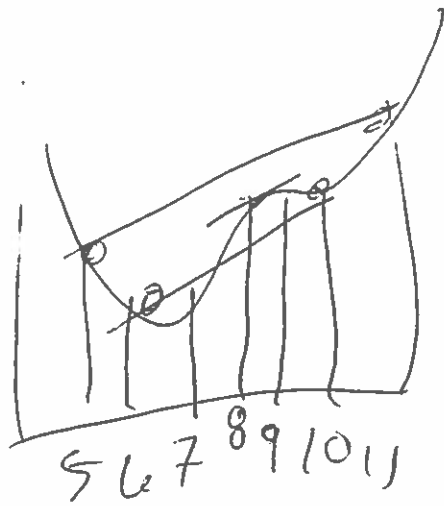
$$\text{Ex } \int_{-1}^3 \sinh(x) dx = \cosh(x) \Big|_{-1}^3$$

$$= \cosh(3) - \cosh(-1)$$

$$\int_1^{27} x^{1/3} - x^{-2} dx = \frac{x^{4/3}}{4/3} - \frac{x^{-1}}{-1} \Big|_1^{27}$$

$$= \left(\frac{27^{4/3}}{4/3} - \frac{27^{-1}}{-1} \right) = \left(\frac{1}{4/3} - \frac{1}{-1} \right)$$

Initial
Value
Problems.



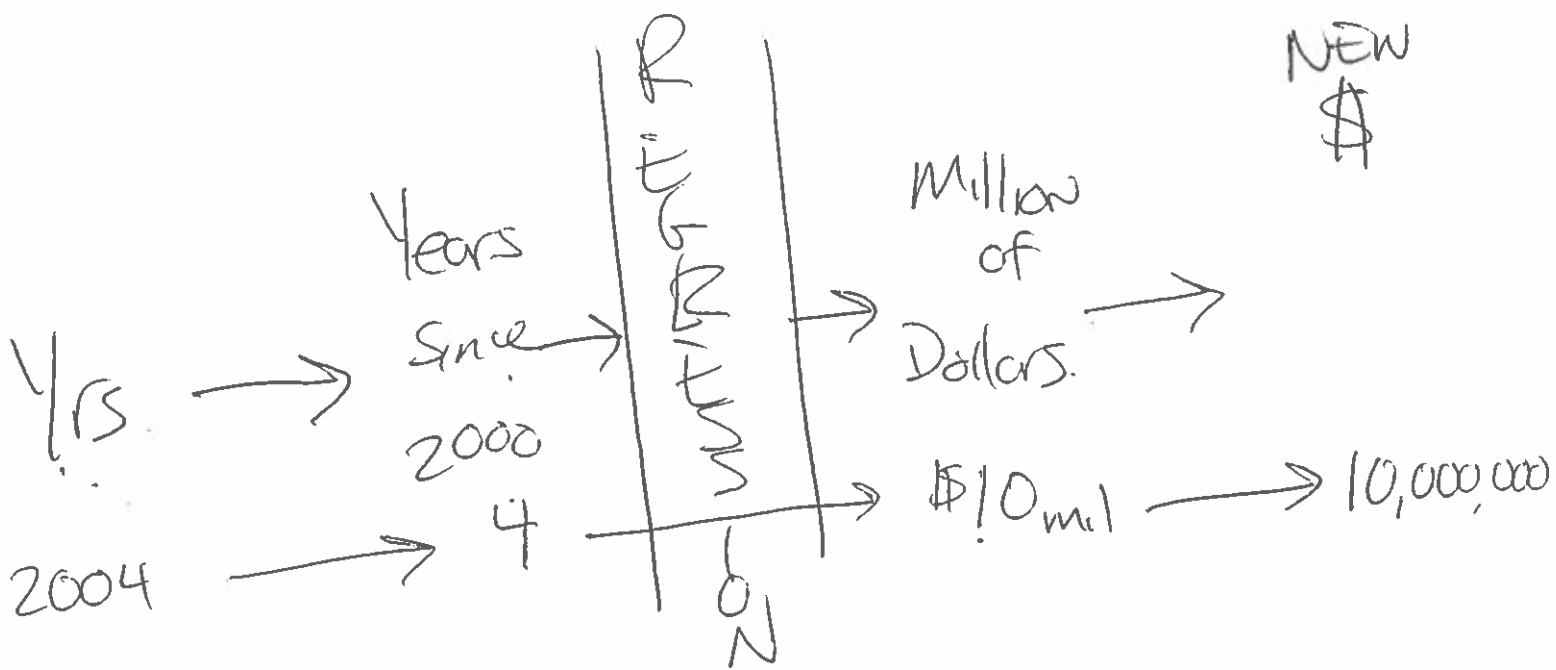
s	$y(s)$
6	
7	
8	
9	
10	
11	$y(11)$

1.24

1.163

1.113

Calc: \downarrow
1.0967



$$Y_1 = X - 2000$$

$$Y_2 = \text{reg}$$

$$Y_3 = X * 1,000,000$$

Yrs

Yrs since 2000

Mil of \$

Yrs since 2000

Mil of \$

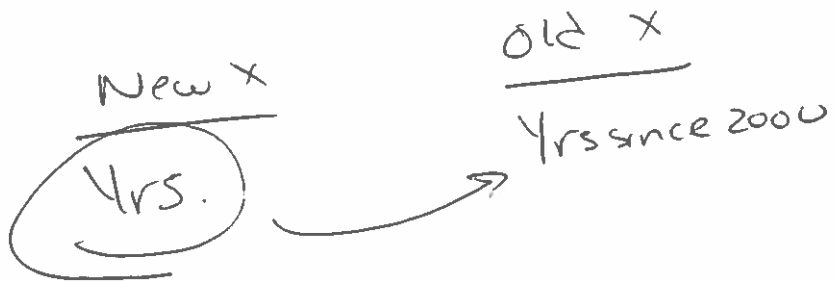
\$

X - 2000

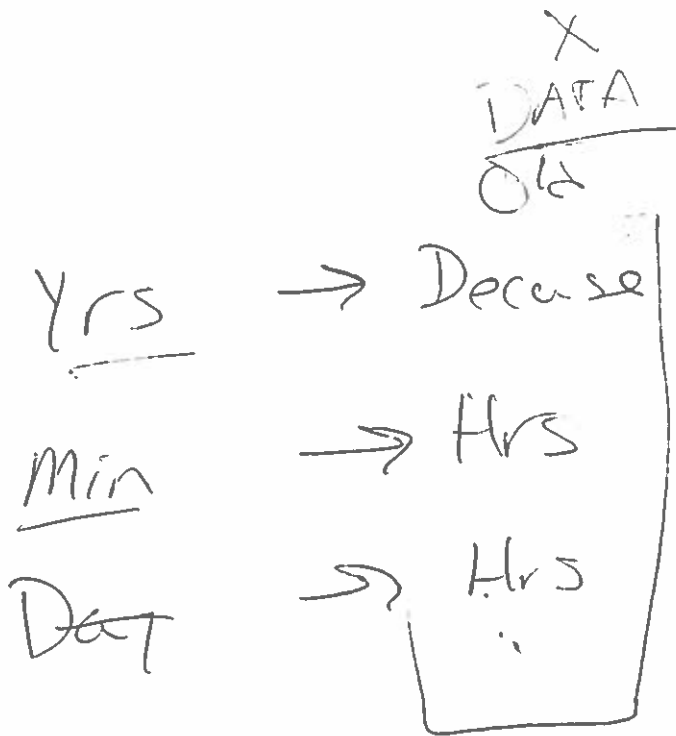
reg

X * 1,000,000

New X	Yrs since ²⁰⁰⁰	Q in Millions
2005	→ 5	10
2006	→ 6	



$$Y_i = X - 2000$$



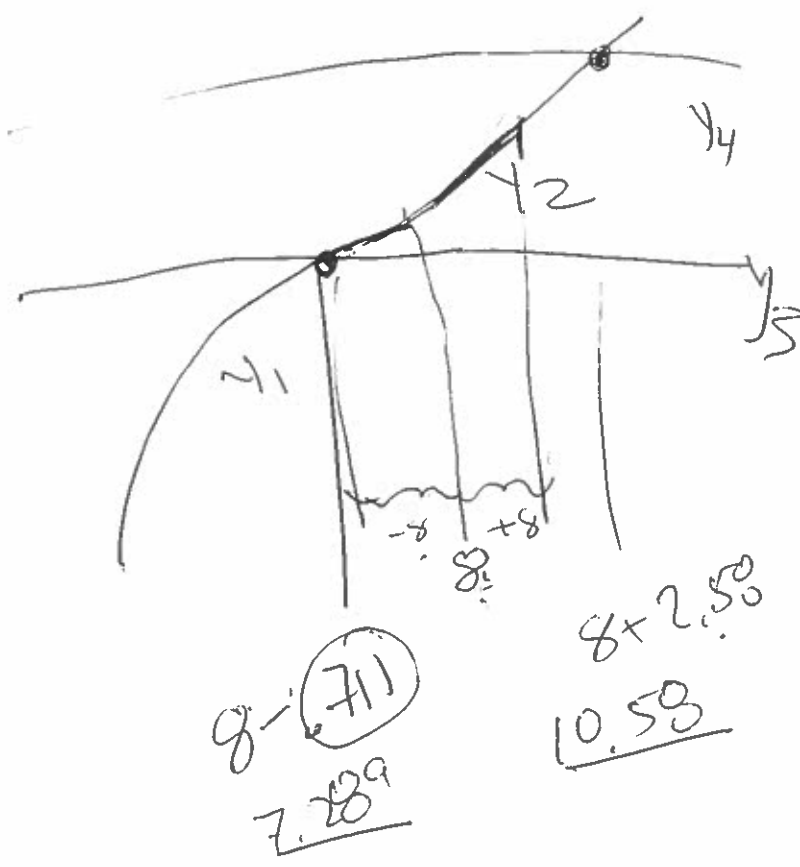
$$X/10$$

$$X/60$$

$$X \times 24$$

$\frac{\text{Days since.}}{\text{min.}}$ → Yrs since 2000

$$X \neq 365$$



$$= 13.212$$

$$y(2008) \rightarrow$$

$$y_2(2008) - y_1(2008)$$

$$=$$

$$\lim_{x \rightarrow 2008} C(x) = \boxed{13.212}$$

$$\epsilon = 1$$

Intere-

$$\underbrace{7.289 \quad 8}_{-0.711} \quad \underbrace{10.58}_{+2.58}$$

$$\boxed{\delta = -0.711}$$

before

7 2 9

Ave. Rad

2.02

USCG Survey

$$y = A \sin(Bx + c) + D$$

$$y' = A \cos(Bx + c) \cdot B$$

Differential

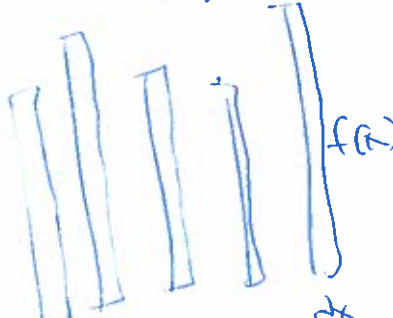
$$\frac{d}{dx} x^2 = 2x$$

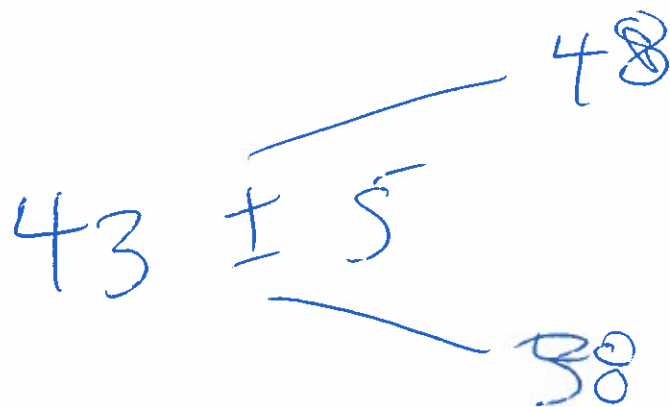
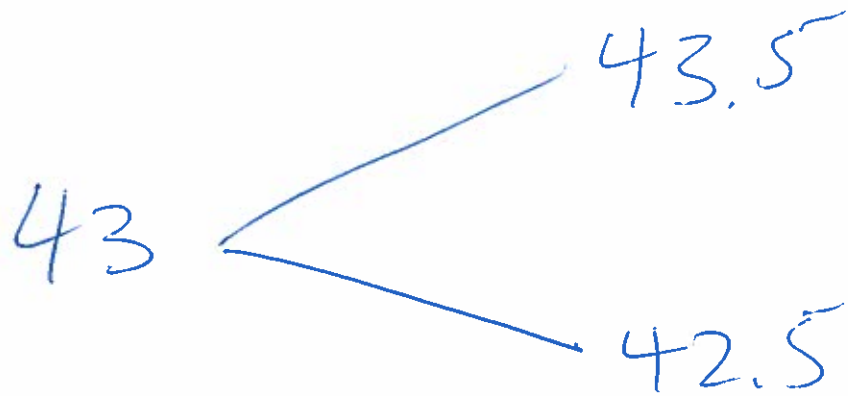
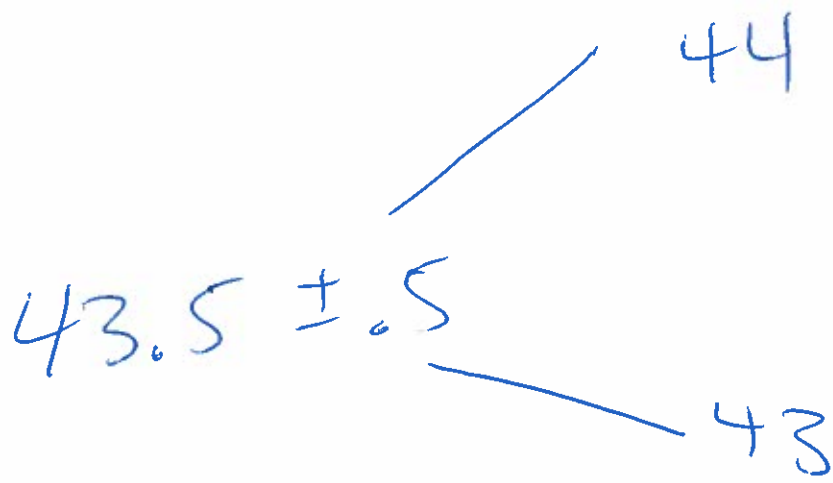
$$\frac{d}{dx} y^2 = 2y \frac{dy}{dx} \quad \text{chain rule.}$$

$$\frac{d}{dt} x^2 = 2x \frac{dx}{dt} \quad \text{Related Rate}$$

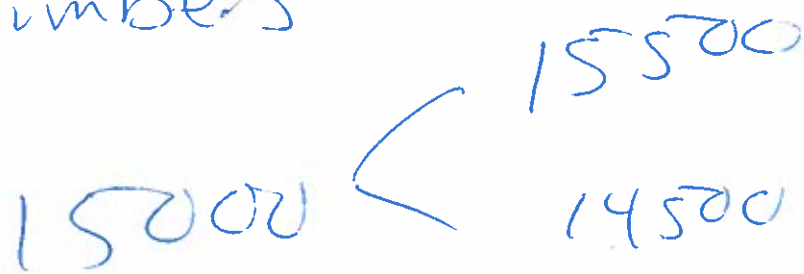
Differentials (derivative w.r.t. nothing)

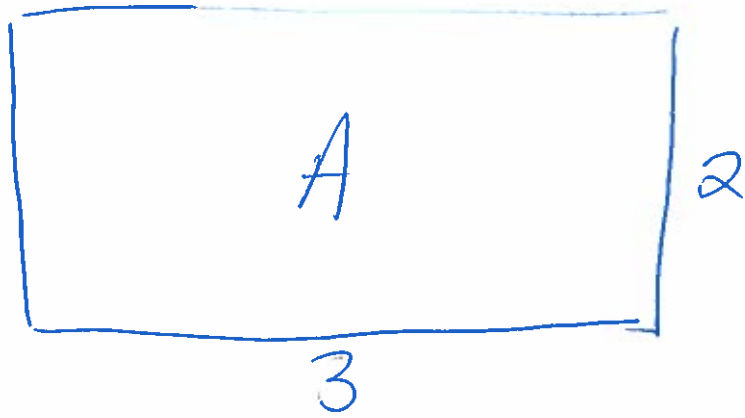
$$d(x^2) = 2x dx$$

$$\int_a^b f(x) dx = \text{Area under } f(x) \text{ between } a \text{ \& } b$$
A diagram illustrating the Riemann sum approximation of an integral. It shows four vertical rectangles of varying heights, representing the area under a curve. The x-axis is labeled with 'x' and the y-axis with 'f(x)'. The rectangles are drawn between two points on the x-axis, 'a' and 'b', which are indicated by a large integral symbol.



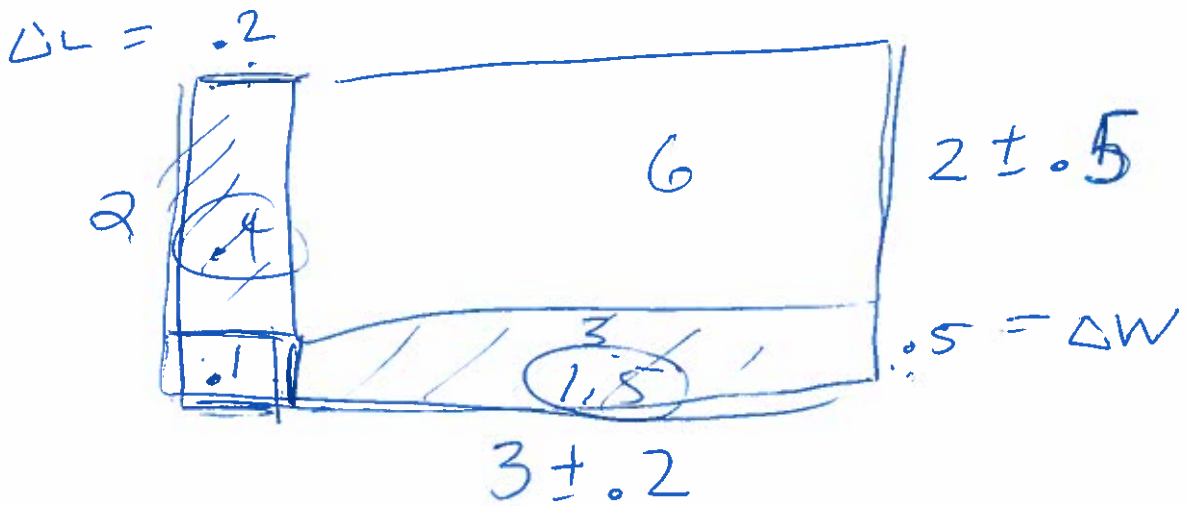
Error in
Numbers





$$A = L \times W$$

$$A = 3 \cdot 2 = 6$$



$$\Delta A = (3.2)(2.5) - 6 = 8 - 6 = 2$$

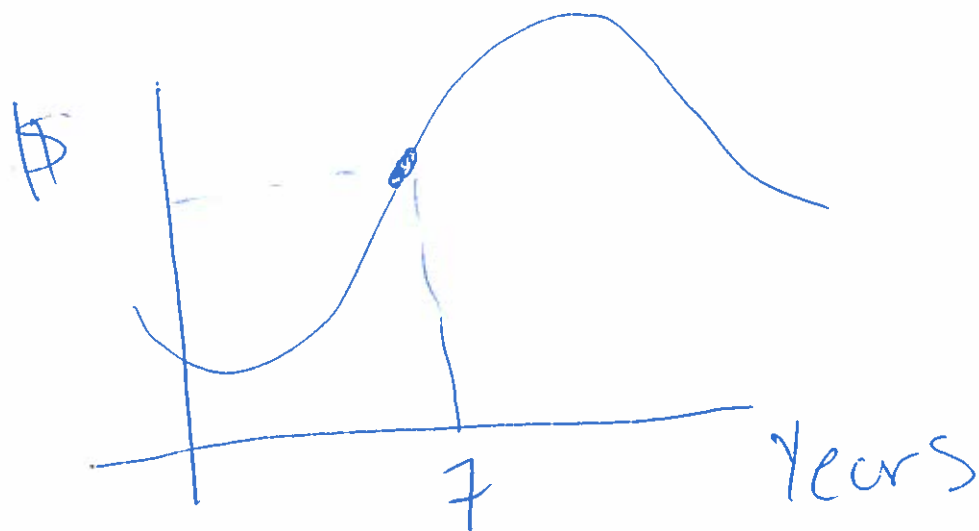
Exact change in area

$$6 \pm 2$$

$$\frac{dy}{dx} = f'(x)$$

$$dy = f'(x) \cdot dx$$

$$10 < \begin{matrix} 10.5 \\ 9.5 \end{matrix} \pm .5$$



In Year 7 Lady G was worth 10.9 mil

$$3.46 \cdot .5 \rightarrow \pm \boxed{1.7} \text{ error}$$

$$\Delta y \approx dy = f'(7) \cdot \frac{dx}{dx = \Delta x} =$$

$$\pm .5$$

% error

$$\frac{1.7}{10.9} \times 100$$

15% error

$$500 \text{ ml} \pm 100$$

$$\frac{100}{500} \times 100 = 20\%$$

20

30

40

$$dx = \pm 5$$

200

300

400

$$dx = \pm 50$$

Yrs

2000 $\xrightarrow{X-2000}$

Yrs after 2000	
X	Y
5	
6	
7	
8	

new X
Years

old
Yrs after 2000

Fun
X-2000

old X
Yrs

old Y
\$ in Mil.

Quant

old Y
\$ in Mil.

New Y
\$

~~X~~ \$ 1000000

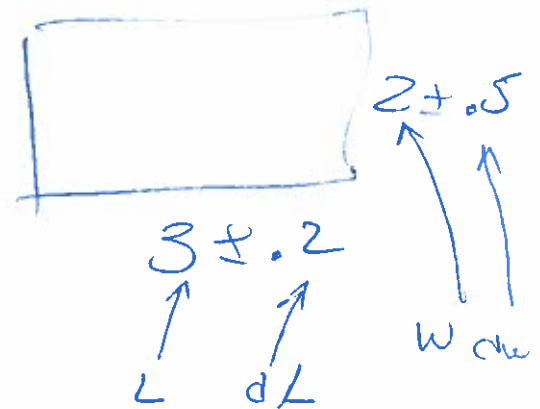
$$y = 1000000 \text{ Reg}(X - 2000)$$

$$y' =$$

$$A = l \cdot w$$

$$dA = l \cdot dw + w \cdot dl$$

$$= 3(\pm .5) + 2(\pm .2)$$
$$1.5 \pm .4$$
$$\pm 1.9$$

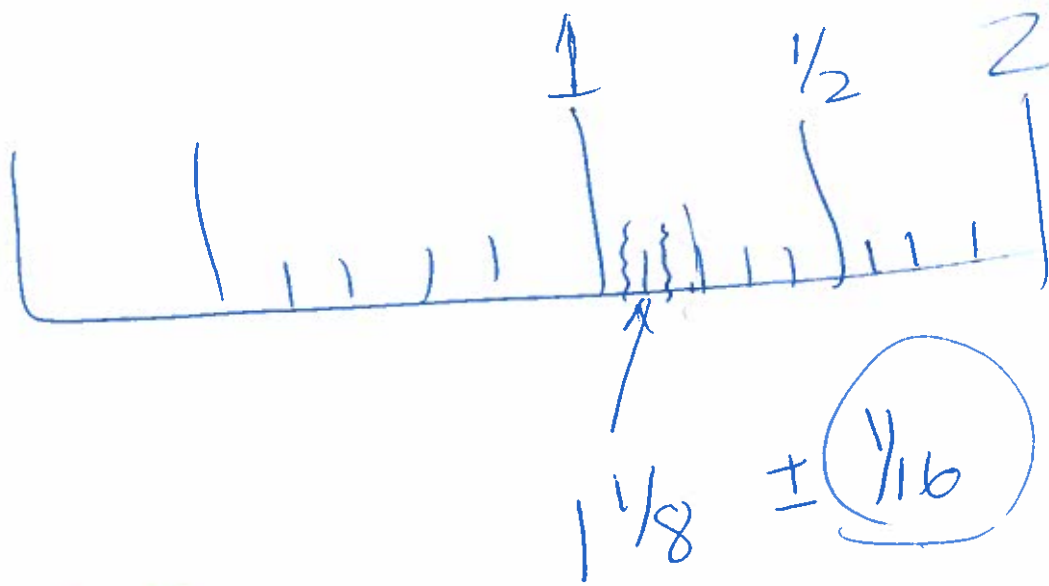


Ex $E = M \cdot C^2$

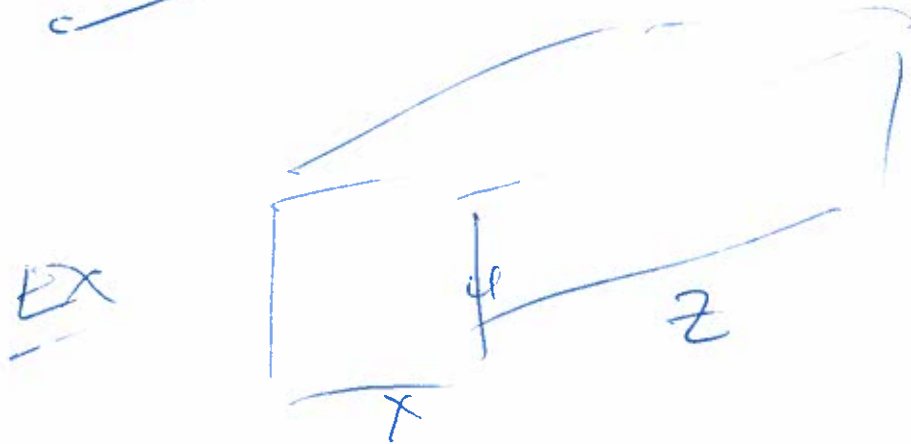
Given. $M = 6 \pm .01$ $C = 2 \pm .05$ $\leftarrow dw$

Find error in E ?

$$dE = M \cdot 2C \cdot dC + C^2 \cdot dM$$
$$= 6 \cdot 2 \cdot 2 \cdot .05 + 2^2 \cdot .01$$
$$= 1.2 \pm .04 = 1.24$$



Error



$$V = xyz$$

$$dV = xydz + xzdy + yzdx$$