

TODAY:

1 Implicit Differentiation

Implied

"Heads are gonna roll"

Explicit

"I'm cutting your head off"

$$2x = y - 1$$

$$\frac{d}{dx}(2x) = \frac{d}{dy}(y-1)$$

$$2 = \frac{dy}{dx}$$

$$f(x) = 2x + 1$$

$$f'(x) = 2$$

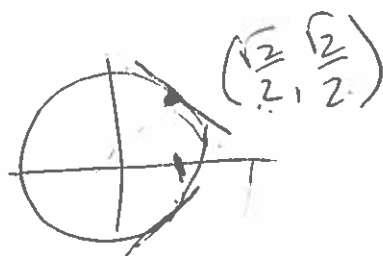
Ex $y^2 + x^2 = 1$. Circle.

$$\frac{d}{dx}(y^2 + x^2) = \frac{d}{dx} 1$$

$$2y \cdot \frac{dy}{dx} + 2x = 0$$

$$\frac{2y y'}{2y} = \frac{-2x}{2y}$$

$$y' = -\frac{x}{y}$$



$$y'(x,y) = \frac{-\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = -1$$

Ex $y^2 + \sin y - 2xy = 7$

$$\frac{d}{dx} y^2 + \frac{d}{dx} \sin y - 2 \frac{d}{dx} (xy)$$

$$2y \frac{dy}{dx} + \cos y \cdot \frac{dy}{dx} - 2 \left[x \frac{dy}{dx} + y \right] = 0$$

$$2y \frac{dy}{dx} + \cos y \frac{dy}{dx} - 2x \frac{dy}{dx} = 2y$$

$$\frac{dy}{dx} (2y + \cos y - 2x) = 2y$$

$$\frac{dy}{dx} = \frac{2y}{2y + \cos y - 2x}$$

Hyperbolic Trig Functions

Hyperbolic cosine.
 $\cosh(x) = \frac{e^x + e^{-x}}{2}$

$$\frac{d}{dx} \cosh(x) = \sinh(x)$$

Hyperbolic sine
 $\sinh(x) = \frac{e^x - e^{-x}}{2}$

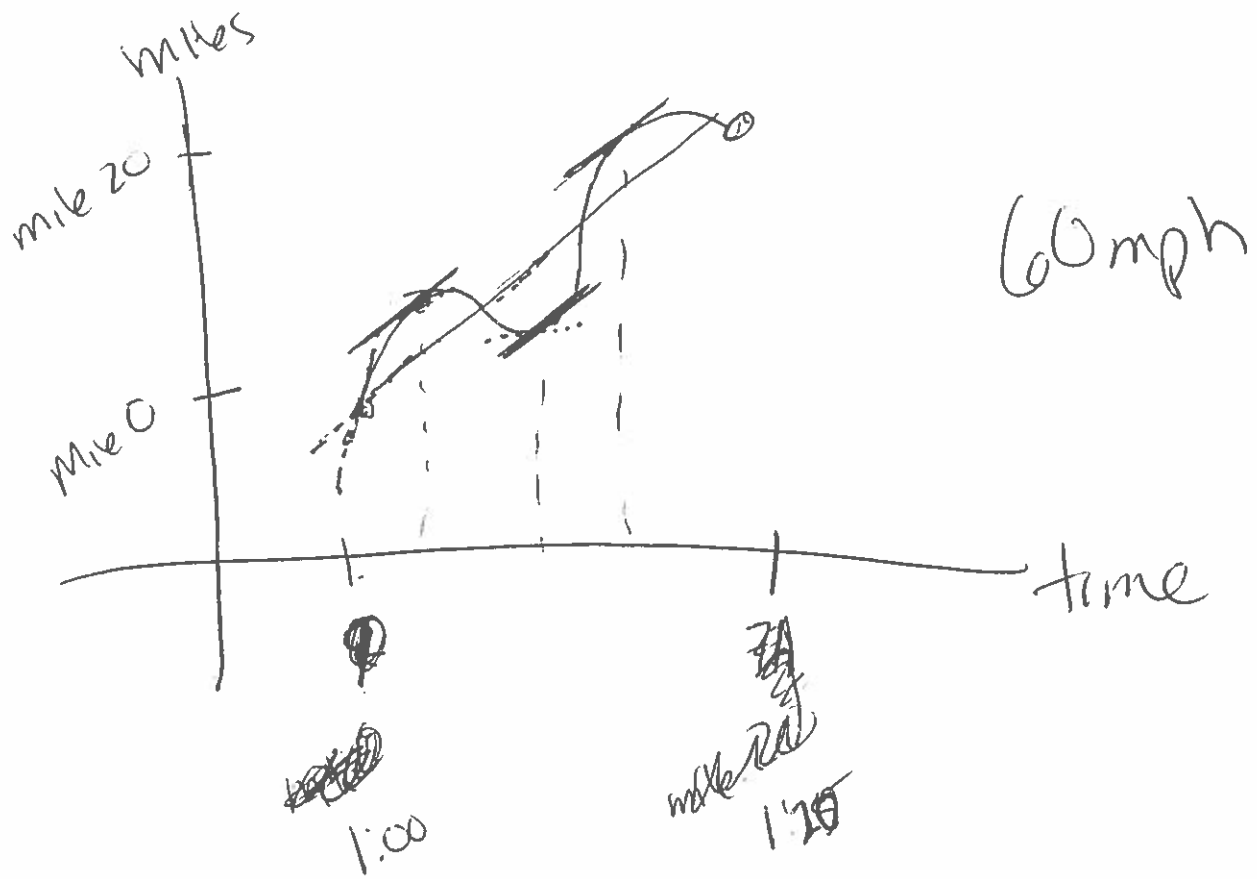
$$\frac{d}{dx} \sinh(x) = \cosh(x)$$

Hyperbolic tangent
 $\tanh = \frac{e^x - e^{-x}}{e^x + e^{-x}}$

$$\frac{d}{dx} \tanh(x) = \frac{d}{dx} \frac{\sinh(x)}{\cosh(x)}$$

sech
 csch
 coth

$$\cosh^2(x) - \sinh^2(x) = 1$$



$$\text{Average Rate} = \frac{\Delta y}{\Delta x} = \frac{20 \text{ miles}}{20 \text{ min}} = \frac{1 \text{ mile}}{\text{min}}$$

Mean Value Theorem

Average Rate of change (between a & b)

instantaneous rate of change
at some points on
interval between a & b.

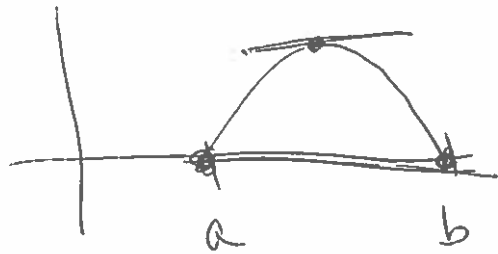
Rolle's Theorem

MVT -

except $f(a) = f(b)$

Then $a < c < b$

$$f'(c) = 0$$



$$\frac{\Delta y}{\Delta x} = \frac{f(b) - f(a)}{b - a} = 0$$

Intermediate Value Theorem

If $f(a) \leq c \leq f(b)$

and $f(x)$ is continuous

Then There is another point "d"

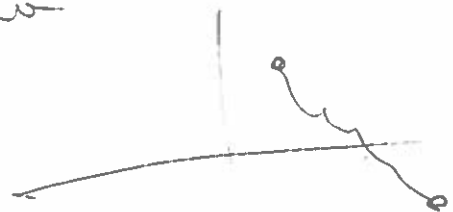
$$f(d) = c$$

If $f(x)$ is continuous

$f(a)$ is \oplus

$f(b)$ is \ominus

Then is a zero between a & b ?



Yes by IVT.

GROUP NAME:

WTH (?) (PRO-BABIES)

Student Names (First and Last)

Date: 2/25

Speaker/Presenter: JENNA

Independent Variable (x-axis): years

Writer/Prep: KATHLEEN

Dependent Variable (y-axis): steroid level in food in babies (ppm)

Leader/Collaborator: CATHRYN

Conclusion (in words):

The average rate of change is the same as the instantaneous rate of change at 2 different points. / Years
 2002 to 2010 when the steroid level in food in babies is increasing at 3.68 ppm and 8.3 ppm respectively.

Supporting Work:

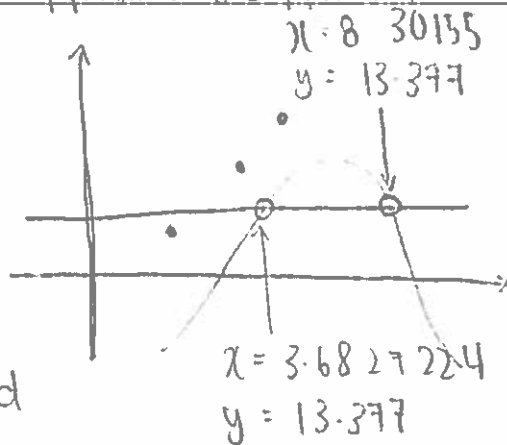
L_1	L_2
.01	122
3	100
6	143
9	200
12	170

Picking two x's

$x = 2$
 $x = 10$

Cubic Reg

$y_i = ax^3 + bx^2 + cx + d$
 $a = -.4701035709$
 $b = 8.4507738409$
 $c = -29.73944721$
 $d = 123.0101337$



At $x = 2, y = 93.574$

At $x = 10, y = 200.59$

Ave rate of change $\frac{200.59 - 93.574}{8}$
 $= \frac{107.016}{8} (y_2)$

$y_3 = \text{deriv}(y, x, x)$

① $Y_1 =$ regression equation.
↑ Turn this off.

② Calculate Average Rate of Change between a & b :

$$Y_2 = (Y_1(b) - Y_1(a)) / (b - a)$$

③ $Y_3 = \text{nderiv}(Y_1, X, X)$

④ calc 5: Intersection
<enter> <enter> <enter>

⑤ " $X = \frac{c}{}$ " is when
the rate at " c " is equal
to the average rate of Y_2
over the region b to a "

GROUP NAME: WHO

Student Names (First and Last)

Date: 7/25/14

Speaker/Presenter: Michael

Independent Variable (x-axis): Time

Writer/Prep: Charlie

Dependent Variable (y-axis): Steady Increase in Price

Leader/Collaborator: Caitlin

Conclusion (in words):

Take the value of $c = 1$ (2007), the value of $d = 11$ (2008) and the value of $b = 4$ (ppm per year). In June of 2007, the index of 4 ppm is 1. In June of 2008, the index of 4 ppm is 11.

Supporting Work:

D.1

$$\frac{x}{0.6} = \frac{y}{1.2}$$

1000

Re: Curve

vertex: (2, 1)

$$a = 4^2 \cdot 1 = 16$$

$$b = 2 \cdot 4 \cdot 1 = 8$$

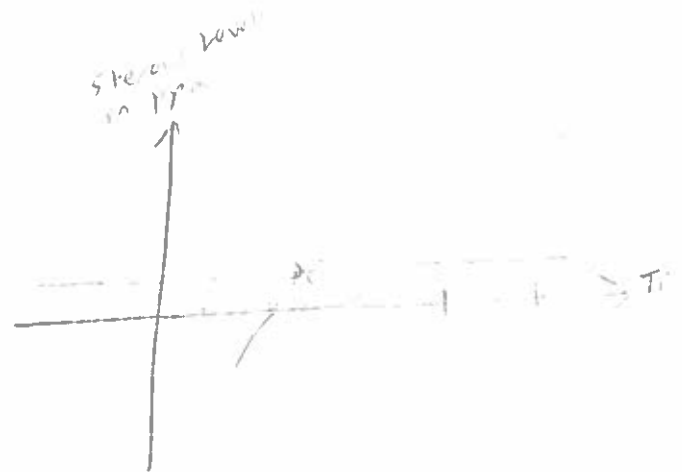
$$c = 1(2^2 + 4 \cdot 2) = 12$$

$$d = 11 \cdot 1 = 11$$

Average rate of change:

$$\begin{aligned} Y_2 &= (1)^2 (11 - 1) / (11 - 1) \\ &= (1) (11 - 1) / (11 - 1) \\ &= 10 / 10 \\ &= 1 \text{ ppm per year} \end{aligned}$$

$$Y_2 = \text{index}(Y_1, X_2)$$



Index of 4

$$x = 2.5 \cdot 5 = 12.5 \quad y = 4$$

<p>GROUP NAME: <u>The Kenkorian Team</u></p> <p>Date: <u>2/25/14</u></p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Ahmed and June</u></p>
<p>Independent Variable (x-axis): <u>income</u></p> <p>Dependant Variable (y-axis): <u>Crime rate</u></p>	<p>Writer/Prep: <u>June/Ahmed</u></p> <p>Leader/Collaborator: _____</p>

Conclusion (in words):
 Between 60K and 80K, there was a negative change for crime rate is -0.0025, which is represented at 70.823657

Supporting Work:

$$Y_1 = 4.1666... E^{-7 \times 10^3} + 1.107... E^{-11 \times 10^2} + \dots - 0.0195... + 812...$$

$Y_2 = \dots$

7	Y
00	.13
30	.5

interest rate $X = 70.823657$

crime rate $Y = -0.0025$

GROUP NAME: Porter's minions

Student Names (First and Last)

Date: Feb 25, 2017

Speaker/Presenter: Kero

Independent Variable (x-axis): years

Writer/Prep: Jenn

Dependant Variable (y-axis): price of tuition

Leader/Collaborator: Dalton

Conclusion (in words):

$x = -17.48...$ is when the rate at ^{-17.48} ~~1983~~ is equal to the average rate of 32.125 over the region b to a

Supporting Work:

$$y_1 = 2818.288... * 1.014...^x \quad (\text{exponential})$$

$$y_2 = (y_1(-15) - y_1(-20)) / (-15 - -20)$$

$$y_3 = nDeriv(y_1, x, x)$$

average rate of change = 32.125..

$$\left. \begin{array}{l} x = -17.48... \\ y = 32.125... \end{array} \right\} \text{intersection}$$

GROUP NAME: <u>Porter's minions</u> Date: <u>2/25/14</u>	Student Names (First and Last) Speaker/Presenter: <u>Jason</u>
Independent Variable (x-axis): <u>years</u> Dependant Variable (y-axis): <u>price of tuition</u>	Writer/Prep: <u>Daniella</u> Leader/Collaborator: <u>Dallon</u>

Conclusion (in words): $x = 42.5$ when the rate at 42.5 is equal to the average rate of 77.86 over the region between

Supporting Work:

$$y_1 = 2818.28... * 1.0148...^x$$

$$y_2 = (y_1(45) - y_1(40)) / (45 - 40)$$

$$y_3 = \text{nderiv}(y_1, x, x)$$

average rate of change : 77.86 $\frac{\$}{\text{year}}$

$$\left. \begin{array}{l} x = 42.5 \\ y = 77.86 \end{array} \right\} \text{Intersection}$$

GROUP NAME: <u>fluffy Ponies</u> Date: <u>2/25/14</u>	Student Names (First and Last) Speaker/Presenter: <u>MILTON</u>
Independant Variable (x-axis): <u>income</u> Dependant Variable (y-axis): <u>crime rate</u>	Writer/Prep: <u>Courtney</u> Leader/Collaborator: <u>Tyler</u>

Conclusion (in words):

Between \$20K and \$60K, the average rate of change for crime rate is $-.0085$ which is represented at \$42.177...K

Supporting Work:

$$y_1 = .3285... \ln(.0367...x + 2.3812...) + .41623...$$

x	y
20	.47
60	.13

$$\frac{.47 - .13}{20 - 60} = \frac{.34}{-40} = -.0085$$

$$y_2 = -.0085$$

$$y_3 = \text{nderviv}(y_1, x, x)$$

$$\text{Intersect} = (42.177..., -.0085)$$