

# Newton's Method

151 h.  
d13

use to find zeros

$$x^4 - 3x^2 - 5x + 7 = 0$$

$$y_1 = x^4 - 3x^2 - 5x + 7$$

(Guess = 3)

$$3 \xrightarrow{\text{STO}} X$$

$$X - y_1 / \text{nderv}(y_1, X, X) \xrightarrow{\text{STO}} X$$

ENTER

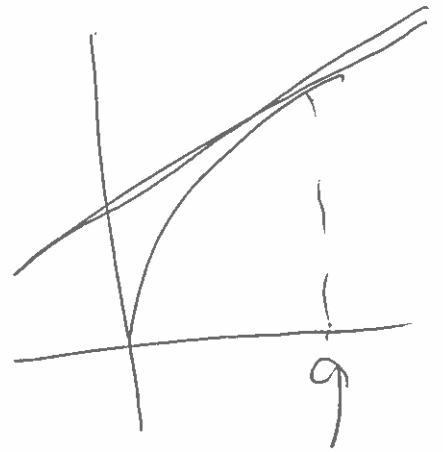
⋮



# Linearizing

$$f(x) = \sqrt{x}$$

Solve  $\sqrt{12}$



## Konnect

$$\sin\left(\frac{11}{4}\right)$$

$$\frac{11}{4} \approx \pi$$

Slope of tangent line

$$f(x) = \sin(x)$$
$$f'(x) = \cos(x)$$

Point  $(\pi, \sin \pi)$   
 $(\pi, 0)$

$$f'(\pi) = \cos(\pi)$$

$$m = -1$$

$$y - 0 = -1(x - \pi)$$

$$y = -x + \pi$$

$$\sin\left(\frac{11}{4}\right) = -\frac{11}{4} + \pi$$



# L'Hôpital Rule "LO PEE TAL"

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \frac{0}{0} \text{ or } \frac{\infty}{\infty}$$

Then.

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$$

Ex

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = \frac{0}{0} \text{ use LHR}$$

$$= \lim_{x \rightarrow 0} \frac{\cos x}{1} = \cos(0) = 1$$

Ex  $\lim_{x \rightarrow \infty} \frac{3x^2 - 5x}{4x^2 + 7} = \frac{\infty}{\infty}$  use LHR

$= \lim_{x \rightarrow \infty} \frac{6x - 5}{8x} = \frac{\infty}{\infty}$  use LHR

$= \lim_{x \rightarrow \infty} \frac{6}{8} = \frac{3}{4}$



$0 \cdot \infty =$   
 $\downarrow \quad \downarrow$

$\lim_{x \rightarrow \infty} \frac{3}{x^{23}} \cdot x^{23} = 3$

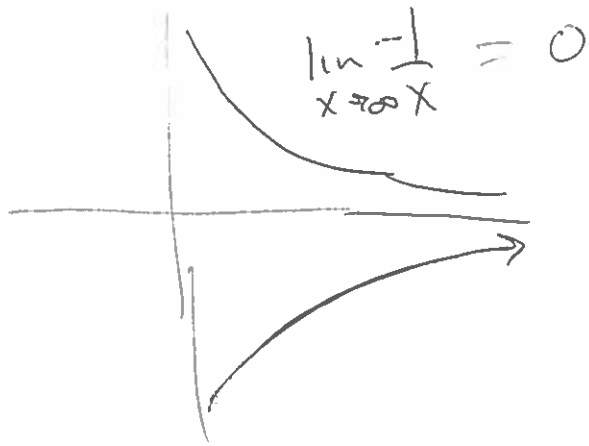
$\lim_{x \rightarrow \infty} \frac{1}{4x^2 + 7} \cdot \frac{3x^2 - 5x}{\infty} = \frac{3}{4}$

0 .  $\infty$

$0 \cdot 0 \checkmark$   
 $0 \cdot 1 \checkmark$   
 $0 \cdot \infty = \text{UNKNOWN}$   
 $1 \cdot 0 \checkmark$   
 $1 \cdot 1 \checkmark$   
 $1 \cdot \infty \checkmark$   
 $\infty \cdot \infty \checkmark$   
 $\infty \cdot 0 = \text{UNKNOWN}$   
 $\infty \cdot 1 \checkmark$

$0/0 = \text{UNKNOWN}$   
 $0/1 \checkmark$   
 $0/\infty \checkmark$   
 $1/0 = \pm \infty$   
 $1/1 \checkmark$   
 $1/\infty = 0$   
 $\infty/\infty = \text{UNKNOWN}$   
 $\infty/1 \checkmark$   
 $\infty/0 = \pm \infty$   
 ~~$\infty/\infty$~~

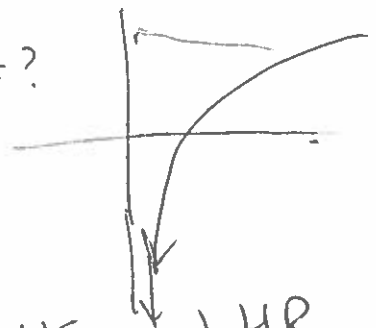
$\infty = \infty$  ??  
UN  
 $1^0 = 1$   
 $1^1 = 1$   
 $1^\infty = 1$   
 $1.99^\infty = 0$   
 $1.01^\infty = \infty$   
UNKNOWN



$$\lim_{x \rightarrow \infty} \frac{-1}{x} \cdot x^2 = -\infty$$



Ex  $\lim_{x \rightarrow 0^+} x \ln x = 0 \cdot -\infty = ?$



$$\lim_{x \rightarrow 0^+} \frac{\ln x}{x^{-1}} = \frac{-\infty}{\infty}$$

$$= \lim_{x \rightarrow 0^+} \frac{\frac{1}{x}}{-x^{-2}} = \lim_{x \rightarrow 0^+} -x = 0$$

Ex:  $\lim_{x \rightarrow \infty} \left(1 + \frac{R}{x}\right)^x = 1^\infty$  unknown

$$e^{\ln x} = x$$

$$\ln \left( \lim_{x \rightarrow \infty} \left(1 + \frac{R}{x}\right)^x \right)$$

$$e^{\lim_{x \rightarrow \infty} \ln \left(1 + \frac{R}{x}\right)^x}$$

$$e^{\lim_{x \rightarrow \infty} x \cdot \ln \left(1 + \frac{R}{x}\right)}$$

$$e^{\lim_{x \rightarrow \infty} \frac{\ln \left(1 + \frac{R}{x}\right)}{x^{-1}} = \frac{0}{0} \text{ USE LHR}}$$

$$e^{\lim_{x \rightarrow \infty} \frac{1}{\left(1 + \frac{R}{x}\right)} \cdot \frac{d}{dx} \left(\frac{R}{x}\right)}{\left(\frac{d}{dx} x^{-1}\right)}$$

$$e^{\lim_{x \rightarrow \infty} \frac{R}{1 + R/x}} = e^R$$

# Second Derivative

Formula

$$y''$$

$$\frac{d^2 y}{dx^2}$$

$D_{xx}$

$$f''(x)$$

Value

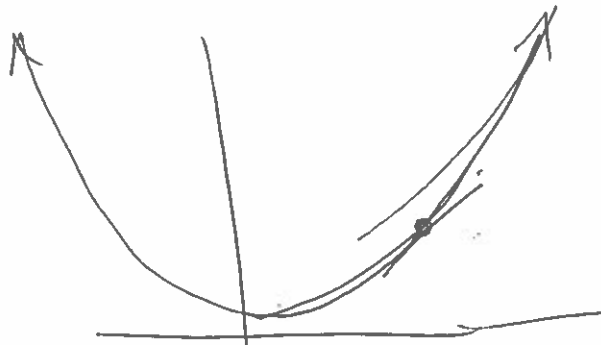
$$y''(a)$$

$$\left. \frac{d^2 y}{dx^2} \right|_{x=a}$$

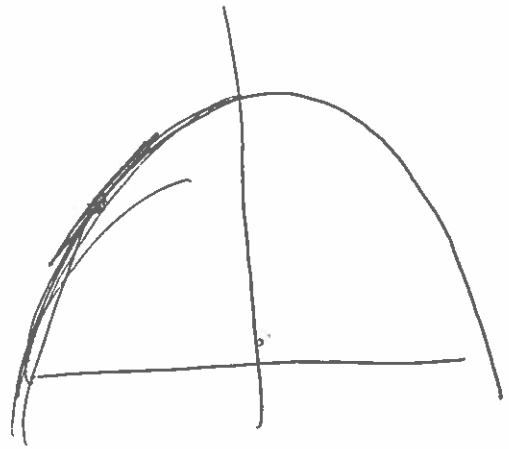
$D_{xx}(a)$

$$f''(a)$$

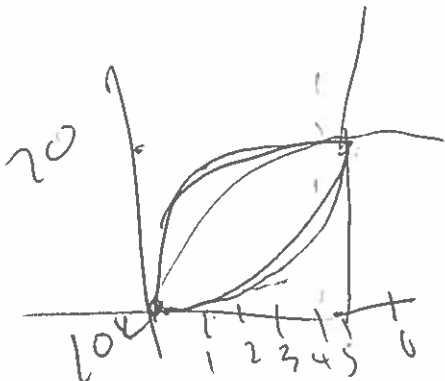
## Concavity



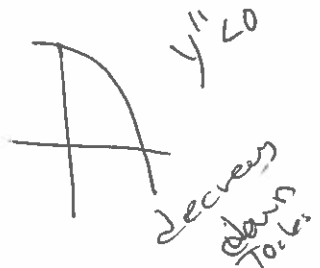
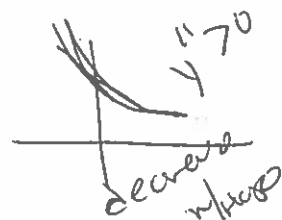
Concave  
up



Concave  
down



"Lady G is decreasing  
constantly??"



GROUP NAME: P. Minions  
 Date: 3/11

Student Names (First and Last)  
 Speaker/Presenter: Jason  
 Writer/Prep: Dallen  
 Leader/Collaborator: \_\_\_\_\_

Independent Variable (x-axis): years  
 Dependent Variable (y-axis): moneys

Conclusion (in words): In 2014 tuition prices will rise without hope!

Supporting Work:

$$Y_1 = -.0833...x^3 + 20.999...x^2 - 417.916... + 5464.199...$$

$$Y_2 = nDeriv(Y_1, x, x)$$

$$Y_3 = nDeriv(Y_2, x, x)$$

X	Y <sub>1</sub>	Y <sub>2</sub>	Y <sub>3</sub>
14	3500.7	121.08	35
	\$	\$/yr	\$/yr/yr



<p>GROUP NAME: <u>Porter's Minions</u></p> <p>Date: <u>March 11, 2014</u></p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Kero</u></p>
<p>Independent Variable (x-axis): <u>years</u></p> <p>Dependant Variable (y-axis): <u>tuition</u></p>	<p>Writer/Prep: <u>Jenn</u></p> <p>Leader/Collaborator: <u>Daniella</u></p>

Conclusion (in words):

In 2014 tuition prices will rise with hope

Supporting Work:

quartic

$$y_1 = -2.041...x^{14} + 97.916...x^{13} + -1733.958...x^{12} + 13477.083...x^{11} + -35573.999...$$

$$y_2 = nDeriv(y_1, x, x)$$

$$y_3 = nDeriv(y_2, x, x)$$

increasing  
concave  
down

x	y <sub>2</sub>	y <sub>3</sub>
14	91.97	-44.91
	\$/yr	\$/yr/yr

GROUP NAME: <u>Fluffy Ponies</u>	Student Names (First and Last)
Date: <u>3/11/14</u>	Speaker/Presenter: <u>Milton</u>
Independent Variable (x-axis): <u>Income</u>	Writer/Prep: <u>Courtney</u>
Dependant Variable (y-axis): <u>Crime rate.</u>	Leader/Collaborator: <u>Tyler</u>

Conclusion (in words):

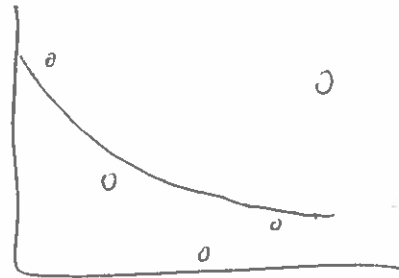
At \$70K, your chance of committing a crime is decreasing, but levels off  
(by n14)

Supporting Work:

In reg:

$$a = .6825...$$

$$b = -.1013...$$



~~$y = .6825... - .1013... \ln x$~~

$$y_1 = .6825... - .1013... \ln x$$

$$y_2 = n \text{ Deriv}(y_1, x, x)$$

$$y_3 = n \text{ Deriv}(y_2, x, x)$$

x	$y_1$	$y_2$	$y_3$
70	.25208	-.0014	$2.1 \times 10^{-5}$
	$\%0$	$\%6/41$	$\%10/41$

GROUP NAME: **INTERNATIONAL AVENGERS!!**

Date: \_\_\_\_\_

Student Names (First and Last) **Ahmed & June**

Speaker/Presenter: **Ahmed & June**

Independent Variable (x-axis): **salary per thousand**

Writer/Prep: **Ahmed & June**

Dependent Variable (y-axis): **crime rate**

Leader/Collaborator: **Tyler**

Conclusion (in words):  
 At 70K crime rate is increasing without hope because it's concave and <sup>is</sup> going up  
 ↓  
 cp

Supporting Work:

$Y_1 = \text{Quartic Reg.}$

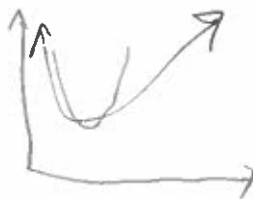
$Y_2 = \text{Deriv}(Y_1, x, x)$

$Y_3 = \text{Deriv}(Y_2, x, x)$

Quartic Reg

$Y = ax^4 + bx^3 + \dots + e$   
 $a = -1.041 \dots E^{-8}$   
 $b = 2.916 \dots 7E^{-9}$   
 $c = -9.58 \dots E^{-5}$   
 $d = -0.01266 \dots 7$   
 $e = .74$

X	Y <sub>2</sub>	Y <sub>3</sub>
70	.0025 Increases	4.2E <sup>-4</sup> With out hope



GROUP NAME: <u>W. H. O.</u> Date: <u>3/11/14</u>	Student Names (First and Last) Speaker/Presenter: <u>Michael</u>
Independant Variable (x-axis): <u>years</u>	Writer/Prep: <u>Charles</u>
Dependant Variable (y-axis): <u>steroid levels</u>	Leader/Collaborator: <u>Cathryn</u>

**Conclusion (in words):**  
 In the current year of 2014, the steroid levels in ppm of the cubic regression are decreasing at the rate of 69.54 ppm per year and will continue to decrease forever after this year.

**Supporting Work:**

Data

<u>X</u>	<u>Y</u>
0.01	122
3	100
6	143
9	200
12	170

$$y = ax^3 + bx^2 + cx + d$$

$a = -0.4701035709$   
 $b = 8.450773849$   
 $c = -29.73944721$   
 $d = 123.0101337$

$Y_2 = \text{nderiv}(y_1, x, x)$   
 $Y_3 = \text{nderiv}(y_2, x, x)$

X	Y <sub>2</sub>	Y <sub>3</sub>
14	-69.54	-22.59

$\frac{\text{ppm}}{\text{yr}}$

$\frac{\text{ppm}}{\text{yr}} / \frac{\text{yr}}{\text{yr}}$

GROUP NAME: WHO Save the babies (e)  
 Date: 3/11/14

Student Names (First and Last)

Speaker/Presenter: Kathleen

Writer/Prep: Jenna Garofalo

Leader/Collaborator: Catherine

Independent Variable (x-axis): years

Dependant Variable (y-axis): steroid in food in babies (ppm)

Conclusion (in words):

In 2014 and after this, the steroid level in food in babies is going on a constant increasing slope up.

Supporting Work:

x	y
0.01	122
3	100
6	143
9	200
12	170

Sin Reg

$$y = a * \sin(bx + c) + d$$

$$a = 51.49869637$$

$$b = 0.4431990559$$

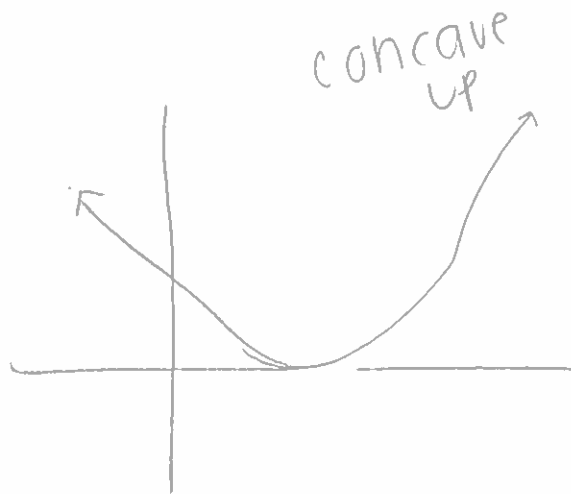
$$c = -2.666224053$$

$$d = 147.0192513$$

$$y_1 = \text{sin Reg}$$

$$y_2 = n\text{Denv}(y_1, x, x)$$

$$y_3 = n\text{Denv}(y_2, x, x)$$



x	y1	y2	y3
<del>11</del>	<del>127.1</del>	<del>-21.05</del>	<del>2.711</del>
17	96.48	3.541	9.9932