

Exponential Models

"Increase at 5% a year"

INVEST \$100 w/ 5% simple interest

$$\begin{array}{r} 5\% \times 100 = \$5 \\ \hline 100\% \quad 100 \quad \frac{\$5}{\$100} \\ \hline 105\% \times 100 \quad \$105 \end{array}$$

\$100 \downarrow $(1.05)(1.05) = 110.25$ Two years.
↑
interest on interest

$$100 (1.05)^2$$

after n years.

$$100 (1.05)^n \quad \leftarrow \text{exponential}$$

Compound Interest Form

$$P = Q \left(1 + \frac{R}{N}\right)^{NT}$$

P = ENDING AMOUNT

Q = STARTING AMOUNT

R = Interest RATE

T = TIME

N = 2 (semi-annual) 4 (Quarterly) 12 (Monthly) 365,

Ex "CD" pays. 6 mos. \$10,000 1.050%

P = Compound monthly

$$Q = 10,000$$

$$R = 1.050\% = .01050 \text{ per year}$$

$$T = 6 \text{ mos} / 12 = 1/2 \text{ year}$$

$$N = 12$$

$$P = 10000 \left(1 + \frac{.0105}{12} \right)^{(12 \times 1/2)}$$
$$= 10052.61$$

Compounded.

Hourly

$$P = Q \left(1 + \frac{R}{8760} \right)^{8760 \cdot T}$$

close to zero

close to 1

Raise 8760

Compounded ↓

Continuously

$$P = Q \left(1 + \frac{R}{\infty} \right)^{\infty \cdot T}$$

↓

$$P = Q e^{RT}$$

Natural
Exponent

2.71...

Math 0:

Solver

$$0 = P - Q e^{(RT)}$$

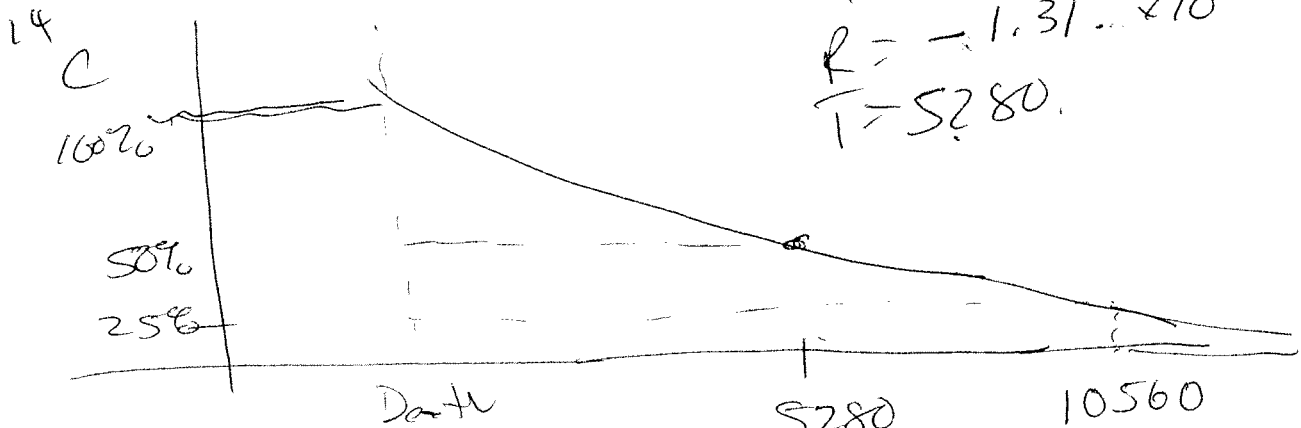
$$P = 10000$$

$$Q = 1200$$

$$R = ? \quad \langle \text{alpha} \rangle \langle \text{entor} \rangle = .0815$$

$$T = 26$$

Carbon Dating



$$P = 50 \quad \text{"Half Life"}$$
$$Q = 100$$
$$R = -1.31 \dots \times 10^{-4}$$
$$T = 5280$$

$$P = ?$$
$$Q = 100$$
$$R = -1.31 \dots$$
$$T = 10560$$

How old is ^{14}C if it is at 1%

$$P = 1$$

$$Q = 100$$

$$R = -1.31 \dots$$

$$T = ? \quad 35079.56 \dots$$

