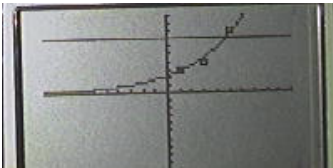
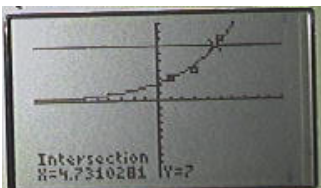


What is precalculus?
Study of Function
How does data in your field become an equation?
~~Write Data, Graph a Function~~
When you do a regression on it



CALCULATE
 1:value
 2:zero
 3:minimum
 4:maximum
 5:intersect
 6:dy/dx
 7:∫f(x)dx



Stat [Test] Stat [2nd] [0] [Enter]

Year	Sales in millions
1	3
3	4
5	8

EXPONENTIAL FUNCTION: $y = a \times b^x = 2.194 \dots (1.27920\dots)^x$

When will sales reach 7 million?

ANSW

9. Your boss gives you the following equation. Give the verti

When will sales reach 7 million?
 $Y_1 = \text{Vars } 5 \gg 2 \text{ enter}$
 $Y_2 = 7$
 Calc 5 intersect Enter/4

ANSWER: 4.7310281

#9.

Horizontal Asymptote: $y = 100$

$$S = \frac{100x(x - .01)}{(x - 100)(x + 100)}$$


DN = DD = 2 \therefore HA = $\frac{LC}{LD} \dots \boxed{y = 100}$

Vertical Asymptotes

$$\frac{100x(x - .01)}{(x - 100)(x + 100)}$$

$x = 100$
 $x = -100$

VA: 100 & -100
VA = zeros of the Denominator

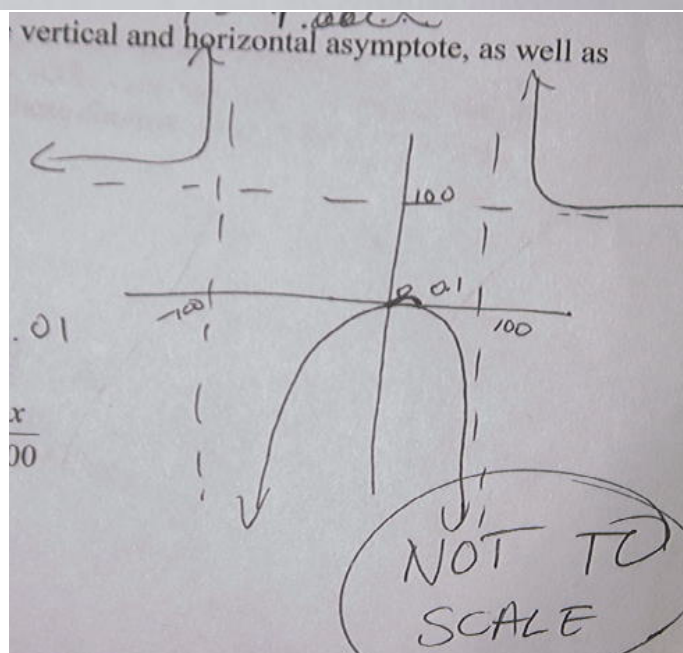
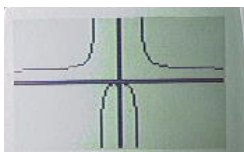


$$S = \frac{100x^2 - x}{x^2 - 10,000} = \frac{100x(x - .01)}{(x - 100)(x + 100)}$$

x-intercept = 0, .01 because
x-intercept = 0s of the numerator

```

WINDOW
Xmin=500
Xmax=500
Xscl=1
Ymin=-500
Ymax=500
Yscl=1
Xres=1
    
```



0.2 Where does the graph cross through the x-axis?

~~scribble~~ $+ 1.25 \times 10^{-8}$

$$R(p) = -250,000p^2(p - 1.25 \times 10^{-8})$$

↑
repeated once

Touches at $p=0$
because repeated twice

with a rate of 2.19% compounded continuously. With only these choices, what is the most amount of money you will have after 12 years?

① Fleet Bank
 [MATH] [0] $0 = P - Q(1 + R/N)^{NT}$
 P = *Solver* [Alpha] [Enter]
 Q = 60,000 ← guess '0'
 R = .022
 N = 12 compounded monthly
 T = 12 yrs.
 P = \$78,108.81

After 12 yrs:
 ① Fleet Bank $2.2\% = 78,108$
 Sovereign Bank $2.19\% = 78,033.9$
 ANSWER: _____

② Sovereign Bank
 [MATH] [0] $0 = P - Qe^{RT}$
 P = *Solver* [Alpha] [Enter]
 Q = 60,000 ← guess '0'
 R = .0219
 T = 12 yrs
 P = \$78,033.99

$R(p) = -250,000p^2(p - 1.25 \times 10^{-8})$
 degree: 3
 imaginary roots: 0, 2, 4, ... not to exceed the degree of the polynomial

EQUATION SOLVER
 eqn: $0 = P - Qe^{(R \cdot T)}$

alpha enter

$P - Qe^{(R \cdot T)} = 0$
 P=50
 Q=100
 R = -.0017328679...
 T=400
 bound = [-1e99, 1...
 left-rt=0

rate = -.17...%

$P - Qe^{(R \cdot T)} = 0$
 P=250
 Q=1000
 R = -.0017328679...
 T=800.00000000...
 bound = [-1e99, 1...

800

$P - Qe^{(R \cdot T)} = 0$
 P=1
 Q=1000
 R = -.0017328679...
 T=5315.0849518...

5315...

13.)⁹⁾ $\log_3(x) + \log_3(x-1) = \log_3(5^2)$ } Prop 3
 $\log_3(x) + \log_3(x-1) = 2 \log_3(5)$ } Prop 2
 $\log_3((x)(x-1)) = 2 \log_3(5)$ } algebra
 $\frac{\log_3((x)(x-1))}{\log_3(5)} = 2$ } change of base (prop 4)
 $\log_5((x)(x-1)) = 2$ } Prop 1 (definition)
 $(x)(x-1) = 25$ } algebra
 b.) 5.52 \rightarrow because logs don't like negatives

Property 4: change of base (reverse)

$$\frac{\log_b(A)}{\log_b(C)} = \log_C(A)$$

1. Choose the end behavior of the graph of each polynomial function.

<p>(a) $f(x) = 2x^5 + 6x^3 - 5x - 3$ {(a) Rises, (b) Falls} to the left and {(a) rises, (b) falls} to the right.</p>	
<p>(b) $f(x) = 4x^4 - 2x^3 + 2x - 5$ {(a) Rises, (b) Falls} to the left and {(a) rises, (b) falls} to the right.</p>	
<p>(c) $f(x) = -3x(x+1)(x-4)^2$ {(a) Rises, (b) Falls} to the left and {(a) rises, (b) falls} to the right.</p>	

disco right LC+ degree:5

happy parab

LC:4+ Degree:4(EVEN)

sad parabola

LC:-3 Degree:4 (even)

2. Divide.

$$(20x^3 + 16x^2 + 6x + 6) \div (5x - 1)$$

Your answer should give the quotient and the remainder.

Quotient: $4x^2 + 4x + 2$

Remainder: 8

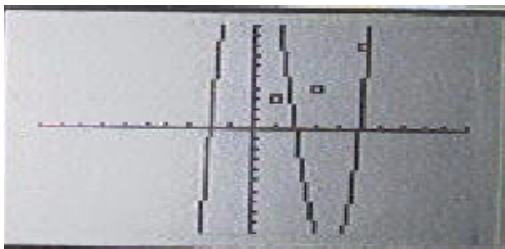
$$\begin{array}{r}
 4x^2 + 4x + 2 \quad R8 \\
 5x - 1 \overline{) 20x^3 + 16x^2 + 6x + 6} \\
 \underline{\ominus 20x^3 \oplus 4x^2} \\
 20x^2 + 6x \\
 \underline{\ominus 20x^2 \oplus 4x} \\
 10x + 6 \\
 \underline{\oplus 10x \ominus 2} \\
 8
 \end{array}$$

3. Solve the inequality.

$$x^3 - 5x^2 \geq 4x - 20$$

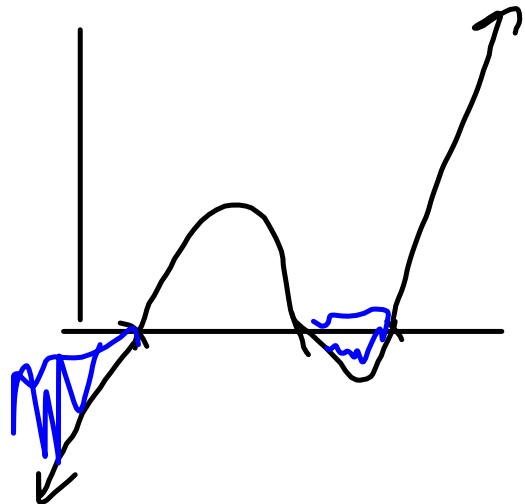
Write your answer as an interval or union of intervals.

$$y = x^3 - 5x^2 - 4x + 20$$



want mountains!

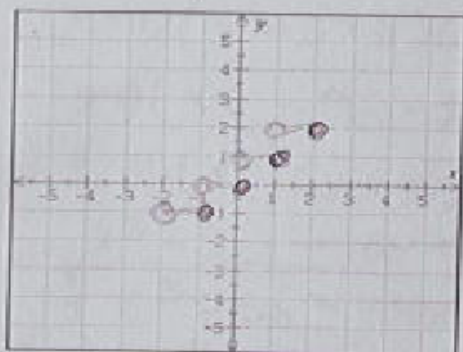
$$[-2, 2] \cup [5, \infty)$$



4. Suppose that the function f is defined on the interval $(-2, 2]$ as follows.

$$f(x) = \begin{cases} -1 & \text{if } -2 < x \leq -1 \rightarrow (-2, -1] \\ 0 & \text{if } -1 < x \leq 0 \rightarrow (-1, 0] \\ 1 & \text{if } 0 < x \leq 1 \rightarrow (0, 1] \\ 2 & \text{if } 1 < x \leq 2 \rightarrow (1, 2] \end{cases}$$

Graph the function f



5. Find all x -intercepts and y -intercepts of the graph of the function.

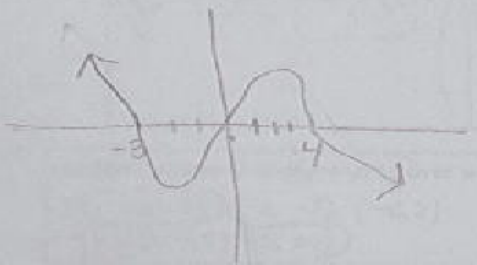
$$f(x) = -x^3 + x^2 + 12x$$

Degree: 3 (odd)
Lead: \ominus Negative
Disco Left

If there is more than one answer, separate them with commas.

x -intercept(s): $-3, 0, 4$

y -intercept(s): 0



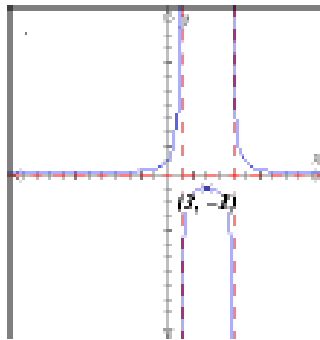
$$f(x) = -x(x^2 - x - 12)$$

$$f(x) = -x(x-4)(x+3)$$

$$\begin{array}{l} -x=0 \\ -1 \rightarrow \\ x=0 \end{array} \quad \begin{array}{l} x=4 \\ x=-3 \end{array}$$

8. The figure below shows the graph of a rational function f with vertical asymptotes $x = 1$, $x = 5$ and horizontal asymptote $y = 0$. The graph does not have an x -intercept, and it passes through the point $(3, -1)$.

The equation for $f(x)$ has one of the five forms shown below. Choose the appropriate form for $f(x)$ and then write the equation. You can assume that $f(x)$ is in simplest form.



$f(x) = \frac{a}{x - b}$

$f(x) = \frac{a(x - b)}{x - c}$

$f(x) = \frac{a}{(x - b)(x - c)}$ because NO zeros,

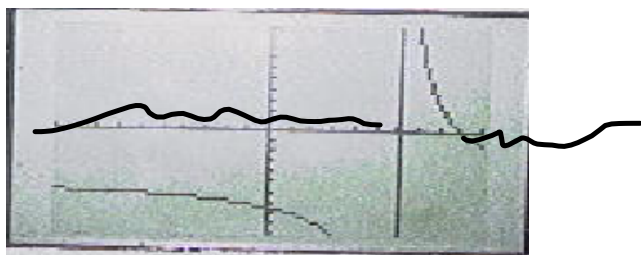
$f(x) = \frac{a(x - b)}{(x - c)(x - d)}$ but 2 VA's

$f(x) = \frac{a(x - b)(x - c)}{(x - d)(x - e)}$

$$y = \frac{a}{(x-1)(x-5)} \quad -1 = \frac{a}{(3-1)(3-5)} \quad a=4$$

$$y = \frac{4}{(x-1)(x-5)}$$

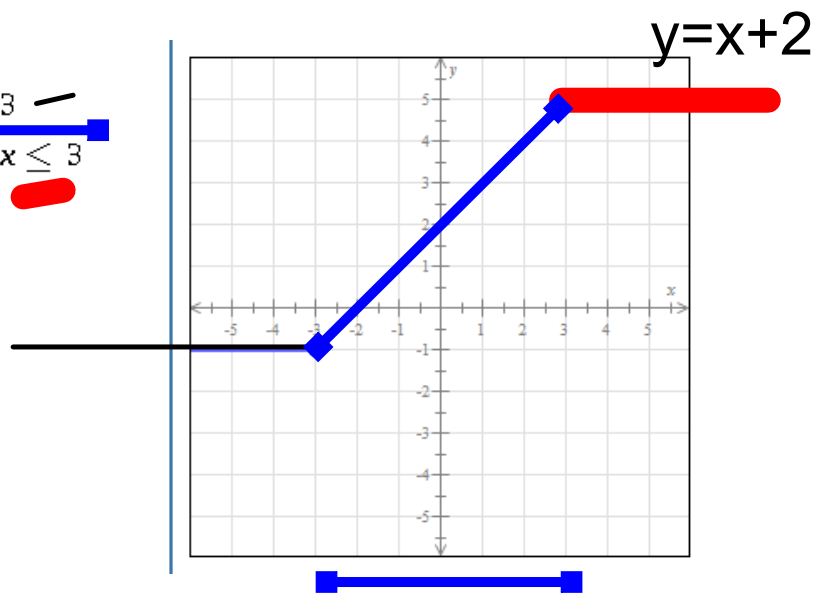
$$\frac{15}{x-6} - 5 \leq 0$$



$$(-\infty, 5) \cup [8, \infty)$$

$$(-\infty, 6) \cup [9, \infty)$$

$$f(x) = \begin{cases} -1 & \text{if } x \leq -3 \\ x+2 & \text{if } -3 < x \leq 3 \\ 5 & \text{if } x > 3 \end{cases}$$



Graphing rational functions with holes

Graph the rational function $h(x) = \frac{-3x^2 + 15x}{x^2 - 7x + 10}$.

We first factor, if possible, and note any restrictions on the value of x .

$$h(x) = \frac{-3x^2 + 15x}{x^2 - 7x + 10} = \frac{-3x(x-5)}{(x-2)(x-5)}$$

$$x \neq 2, x \neq 5$$

still true..

get a hole

