

GROUP NAME:

Student Names (First and Last)

Logo:

Speaker/Presenter: _____

Date: _____

Writer/Prep: Shawnee

Topics:

QC/Leader: _____

Instructions: # 1) Do Paths cross.. Do Ships hit?
Angle between the two paths

$$\vec{A} = \langle 9-0; 0-12 \rangle = \langle 9, -12 \rangle$$

$$\vec{B} = \langle 2-14, 1-10 \rangle = \langle -12, -9 \rangle$$

$$\langle 0, 12 \rangle + t \langle 9, -12 \rangle$$

$$\langle 14, 10 \rangle + s \langle -12, -9 \rangle$$

$$x = 9t \quad y = 12 - 12t$$

$$x = 14 - 12s \quad y = 10 - 9s$$

$$(9t = 14 - 12s) \cdot 4$$

$$(2 - 12t = 10 - 9s) \cdot 3$$

$$36t = 56 - 48s$$

$$36 - 36t = 30 - 27s$$

$$36 = 56 - 75s$$

$$-20 = -75s = -50$$

$$s = \frac{2}{3}$$

$$t = \frac{2}{3}$$

$$9t = 14 - 12 \left(\frac{2}{3}\right)$$

$$9t = 14 - 8$$

$$9t = 6$$

$$t = \frac{2}{3}$$

$$t = \frac{2}{3}$$

So $s = t$
they cross
and hit

$$\|\vec{A}\| = \sqrt{9^2 + (-12)^2} = \sqrt{225}$$

$$\|\vec{B}\| = \sqrt{(-12)^2 + (-9)^2} = \sqrt{225}$$

$$\cos^{-1} \frac{\langle 9, -12 \rangle \cdot \langle -12, -9 \rangle}{\sqrt{225}^2}$$

$$= \cos^{-1} \frac{(9)(-12) + (-12)(-9)}{225}$$

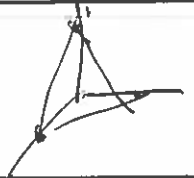
$$= \cos^{-1} \frac{-108 + 108}{225}$$

$$= \cos^{-1} 0 = 90^\circ \text{ or } \frac{\pi}{2}$$

$$|\vec{A}| = |\vec{B}| = \sqrt{9^2 + 12^2}$$

GROUP NAME: <u>Midterm</u>	Student Names (First and Last)
Logo: <u># 2 parts AB-B</u>	Speaker/Presenter: <u>Piyush</u>
Date: _____	Writer/Prep: <u>Puri</u>
Topics: _____	QC/Leader: _____

Instructions: • Eq of a plane $(1,0,0)$ $(0,4,0)$ $(0,0,2)$
 • The distance of origin from the plane?



$$\vec{AB} = \langle 0-1, 4-0, 0-0 \rangle = \langle -1, 4, 0 \rangle$$

$$\vec{BC} = \langle 0-0, 0-4, 2-0 \rangle = \langle 0, -4, 2 \rangle$$

$$\vec{AB} \times \vec{BC} = \begin{vmatrix} i & j & k \\ -1 & 4 & 0 \\ 0 & -4 & 2 \end{vmatrix} = \langle i(8-0), j(0+2), k(\cancel{4-0}) \rangle = \langle 8, 2, 4 \rangle$$

pt A. $(1,0,0)$

$$8(x-1) + 2(y-0) + 4(z-0) = 0$$

$$8x - 8 + 2y + 4z = 0$$

$$8x + 2y + 4z = 8$$

$$4x + y + 2z = 4$$

$$d = \frac{|8(0) + 2(0) + 4(0) - 8|}{\sqrt{8^2 + 2^2 + 4^2}} = \frac{8}{\sqrt{84}} = .8728\dots$$

$$= \frac{4}{\sqrt{21}}$$

GROUP NAME:

Student Names (First and Last)

Logo:

Speaker/Presenter: Kyle H.

Date: _____

Writer/Prep: _____

Topics: MIDTERM FALL 2013 #3

QC/Leader: _____

Instructions:

#3

The position of a car traveling up a spiral driveway is given by: $r(t) = 7\cos t \mathbf{i} + 7\sin t \mathbf{j} + 49t \mathbf{k}$

Find the distance travelled, the position, and the direction being faced after 30 seconds.

Arc Length \Rightarrow distance travelled

$$L = \int_0^{30} \sqrt{(-7\sin t)^2 + (7\cos t)^2 + 49^2} dt = \int_0^{30} \sqrt{2450} dt = 1484.7$$

$$r(30) = \langle 7\cos(30), 7\sin(30), 49(30) \rangle = \langle 1.08, -6.92, 1470 \rangle$$

$$r'(30) = \langle -7\sin(30), 7\cos(30), 49 \rangle = \langle 6.92, 1.08, 49 \rangle$$

Distance: 1484.7

Position: $x = 1.08, y = -6.92, z = 1470$

Direction: $\langle 6.92, 1.08, 49 \rangle$

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Speaker/Presenter: _____

Date: _____

Writer/Prep: _____

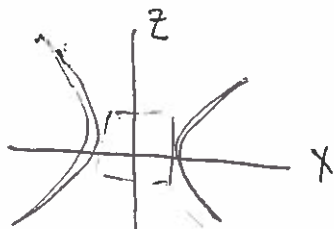
Topics:

QC/Leader: _____

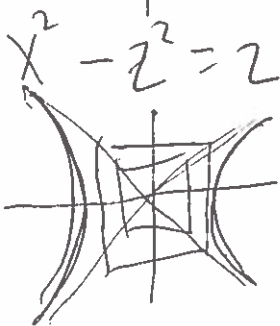
Instructions:

(4) $x^2 - y - z^2 = 1$ $y = -1, 0, 1$

$x^2 - z^2 = 1$ $y = 0$

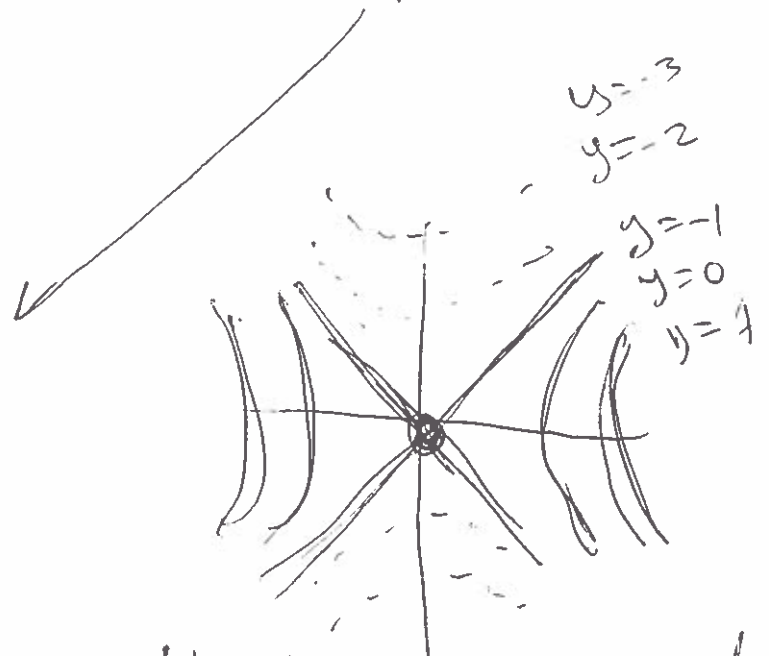
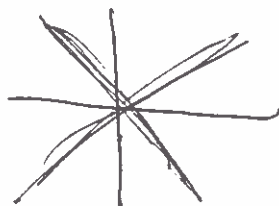


$y = 1$



$y = -1$

$x^2 - z^2 = 0$
 $x = z$



Hyperbolic Paraboloid

<p>GROUP NAME:</p> <p>Logo:</p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: _____</p>
<p>Date: _____</p> <p>Topics:</p>	<p>Writer/Prep: _____</p> <p>QC/Leader: _____</p>

Instructions: (4) Draw and label curves for $y = -1$, 0 , and 1 . Describe the shape.

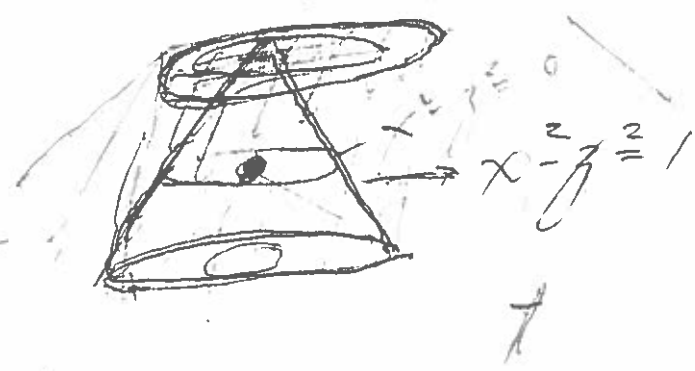
(4) $x^2 - y - z^2 = 1$ for $y = -1$

$x^2 - (-1) - z^2 = 1 \Rightarrow x^2 - z^2 = 0$

$x = 0, z = 0$
 $x = \pm 1, z = 0$

for $y = 0 \Rightarrow x^2 - z^2 = 1$

$x = \pm 1, z = 0$



The surface is a hyperboloid of one sheet.

GROUP NAME:	Student Names (First and Last)
Logo:	Speaker/Presenter: <u>Daniel Cohen</u>
Date: _____	Writer/Prep: _____
Topics:	QC/Leader: _____

Instructions:
#5: Find max, min, and saddle points.

$$f(x, y) = 900 + 3x^2 - 6xy - y^3$$

$$f_x = 6x - 6y = 0 \Rightarrow x = y$$

$$f_y = -6x - 3y^2 = 0 \Rightarrow -3y^2 = 6x$$

$$-6x - 3x^2 = 0 \quad x = \frac{-y^2}{2}$$

$$-3x(2+x) = 0$$

$$f_{xx} = 6 > 0$$

$$x = -\frac{x^2}{2}$$

$$f_{yy} = -6y = 12$$

$$x = -2, y = -2$$

$$x = 0, y = 0$$

$$f_{xy} = -6$$

$$f_{xx}f_{yy} - f_{xy}^2 = 72 - 36 = +36$$

→ min at $f(-2, -2) = 396$

$$D = f_{xx}f_{yy} - f_{xy}^2$$

$$(6)(-6y) - (-6)^2$$

$$-36y - 36$$

$$y=0 \quad D = -36$$

$$(0, 0)$$

Saddle point ($D < 0$)

$$y = -2 \quad D = +36$$

$$(-2, -2)$$

Max/Min ($D > 0$)

$$f_{xx} = 6 \oplus \underline{\underline{\text{Min}}}$$

GROUP NAME:

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Logo:

Speaker/Presenter: _____

Date: _____

Writer/Prep: _____

Topics:

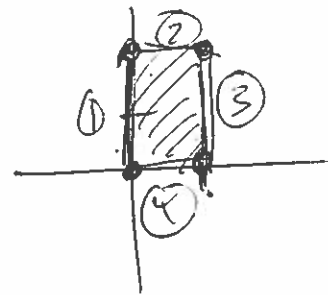
QC/Leader: _____

Instructions:

$$0 \leq x \leq 1 \quad 0 \leq y \leq 2$$

#5

$$f(x,y) = 400 + 3x^2 - 6xy - y^3$$



① $x=0 \quad 0 \leq y \leq 2$

$$z = 400 - y^3$$

$$z' = -3y^2 = 0$$

$$y = 0$$

② $y=2 \quad 0 \leq x \leq 1$

$$z = 400 + 3x^2 - 12x - 8$$

$$z' = 6x - 12 = 0$$

$$x = 2 \quad \text{None.}$$

③ $x=1 \quad 0 \leq y \leq 2$

$$z = 400 + 3 - 6y - y^3$$

$$z' = -6 - 3y^2 = 0 \quad \text{No Soln}$$

~~$x=1 \quad y^2 = y/2 \quad y = \frac{1}{2} = \frac{1}{4}$~~

④ $y=0 \quad 0 \leq x \leq 1$

$$z = 400 + 3x^2$$

$$z' = 6x = 0 = 0$$

$$f(0,0) = 400$$

$$f(0,2) = 392$$

$$f(1,2) = 400 + 3 - 12 - 8 = 383 \quad \leftarrow \text{Absolute Min.}$$

$$f(1,0) = 403 \quad \leftarrow \text{Absolute Max.}$$

GROUP NAME:	Student Names (First and Last)
Logo:	Speaker/Presenter: _____
Date: <u>12.5.13</u>	Writer/Prep: _____
Topics: <u>Midterm Review</u>	QC/Leader: <u>Olga Svitlik</u>

Instructions: #6 Height of roof given $f(x,y) = 400 + 3x^2 - 6xy - y^2$
 Find the value of the greatest slope @ $(3,5)$

$$\frac{f_x}{f_y} = \frac{6x - 6y}{-6x - 3y^2} \quad \text{at } (3,5) \quad \frac{6(3) - 6(5)}{-6(3) - 3(5)^2} = \frac{18 - 30}{-18 - 75} = \frac{-12}{-93} = 0.52$$

$$|\nabla f(3,5)| = |\langle -12, -93 \rangle| = \sqrt{(-12)^2 + (-93)^2} = \sqrt{144 + 8649} = \sqrt{8793} \approx 93.77$$

Find directional derivative from pt. $(3,5)$ towards $(0,0)$

$$\vec{v} = \langle -3, -5 \rangle, \quad \vec{u} = \frac{\vec{v}}{|\vec{v}|} = \frac{\langle -3, -5 \rangle}{\sqrt{34}}$$

$$= \left\langle \frac{-3}{\sqrt{34}}, \frac{-5}{\sqrt{34}} \right\rangle$$

$$D_u f = \nabla f \cdot \vec{u}$$

~~$$D_u f = \left\langle \frac{-3}{\sqrt{34}}, \frac{-5}{\sqrt{34}} \right\rangle \cdot \langle -12, -93 \rangle$$~~

$$\langle -12, -93 \rangle \cdot \left\langle \frac{-3}{\sqrt{34}}, \frac{-5}{\sqrt{34}} \right\rangle$$

$$\frac{36 + 465}{\sqrt{34}} = \frac{501}{\sqrt{34}} \approx 85.92$$

GROUP NAME:	Student Names (First and Last)
Logo:	Speaker/Presenter: <u>Matt Persico</u>
Date: _____	Writer/Prep: _____
Topics:	QC/Leader: _____

Instructions: #7

7) If the $f(x,y) = \frac{2x - 7y^2}{7x^2 - 2y} + 100$, find the limit as $(x,y) \rightarrow (0,0)$ along the paths $x=0$.

$$\lim_{y \rightarrow 0} \frac{2(0) - 7y^2}{7(0)^2 - 2y} + 100 = \lim_{y \rightarrow 0} \frac{-7y^2}{-2y} + 100 = \lim_{y \rightarrow 0} \frac{7y}{2} + 100$$

Along $y=x$

$$\lim_{x \rightarrow 0} \frac{2x - 7x^2 + 100}{7x^2 - 2x} = \lim_{x \rightarrow 0} \frac{-7x^2}{7x^2} = -1 + 100 = 99$$

ES it continuous at $(0,0)$?

$$f(x,y) = \frac{2x - 7y^2}{7x^2 - 2y} + 100 = \text{NO}$$

because $\lim_{(x,y) \rightarrow (0,0)} f(x,y) =$ Two different answers depending on the path

GROUP NAME:	Student Names (First and Last)
Logo:	Speaker/Presenter: _____
Date: _____	Writer/Prep: <u>Gery Greweling</u>
Topics:	QC/Leader: _____

Instructions: #8 If the error in measuring the height is $\pm .03$ and radius is $\pm .07$ cm, find an estimate for the maximum error of the volume of the cylinder using the total differential when the cylindrical rod is 5 cm in radius and 10 cm in height.

$$\text{Volume} = \pi r^2 h$$

$$\frac{\partial V}{\partial r} = 2\pi r h$$

$$\frac{\partial V}{\partial h} = \pi r^2$$

$$dV = \frac{\partial V}{\partial r} dr + \frac{\partial V}{\partial h} dh$$

$$dV = 2\pi(5)(10)(\pm .07) + \pi(5)^2(\pm .03)$$

$$\pm 24.347$$

$$V(r=5, h=10) = \pi(25) \cdot 10 = 785.39$$

$$\text{Volume} = 785.39 \pm 24.347$$

$$\% \text{ error} = \frac{24.347}{785.39} \times 100 = 3.1\%$$

GROUP NAME: わかりません

Logo: ?

Date: 12/4/13

Topics:

Student Names (First and Last)

Speaker/Presenter: _____

Writer/Prep: _____

QC/Leader: Javier Blanco

Instructions: #9 Mid-term

#9 $\int_0^3 \int_0^7 10y \, dy \, dx$

$$\int_0^3 [5y^2]_0^7 \, dx$$

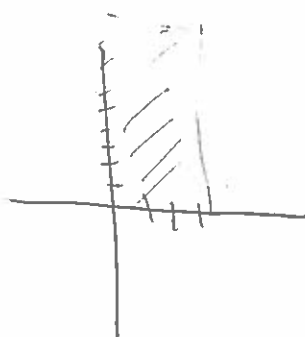
$$\int_0^3 245 \, dx$$

$$[245x]_0^3$$

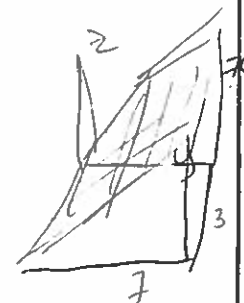
735

Le Region?

$$0 \leq x \leq 3, 0 \leq y \leq 7$$

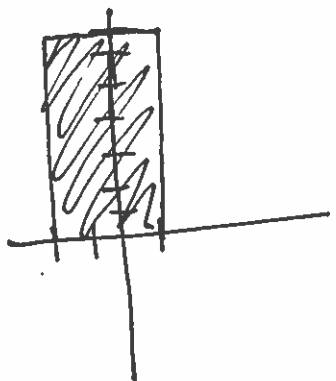


$$z = 10y$$



GROUP NAME: Logo: <u>Engineers</u>	Student Names (First and Last) Speaker/Presenter: _____ Writer/Prep: <u>Chris Sholy</u> QC/Leader: _____
Date: _____	
Topics:	

Instructions: $\iint_R (x^2 + 4xy) dA$ $-2 < x < 1$
 $0 < y < 7$
 Midterm #10



$$\int_{x=-2}^1 \int_0^7 (x^2 + 4xy) dy dx$$

$$\int_{-2}^1 \left(yx^2 + 2xy^2 \Big|_{y=0}^7 \right) dx$$

$$\int_{-2}^1 (7x^2 + 98x) dx$$

$$\frac{7x^3}{3} + 49x^2 \Big|_{-2}^1 \left[\frac{7}{3} + 49 \right]$$

$$\left[\frac{7}{3} + 49 \right] - \left[\frac{7(-2)^3}{3} + 49(-2)^2 \right] - \left[-\frac{56}{3} + 196 \right]$$

~~154~~
~~126~~

$$= \frac{63}{3} - 147$$

$$= 21 - 147$$

-126

GROUP NAME:	Student Names (First and Last)
Logo:	Speaker/Presenter: _____
Date: _____	Writer/Prep: _____
Topics:	QC/Leader: _____

Instructions:

11

$$g(x, y) = y \cdot 5^{2x}$$

$$x(u, v) = 5u + 2v$$

$$y(u, v) = 3u - v$$

$$\frac{\partial g}{\partial y} = 5^{2x}$$

$$= 5^{2(5u+2v)}$$

$$\frac{\partial g}{\partial x} = y \cdot 5^{2x} \cdot \ln 5 \cdot 2 = 2(3u-v) \ln 5 \cdot 5^{2(5u+2v)}$$


$$\frac{\partial x}{\partial u} = 5$$

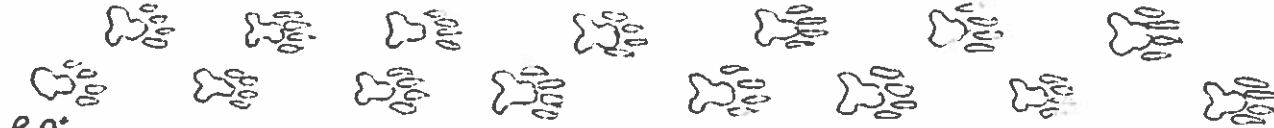
$$\frac{\partial y}{\partial u} = 3$$

$$\frac{\partial g}{\partial u} = \frac{\partial g}{\partial x} \cdot \frac{\partial x}{\partial u} + \frac{\partial g}{\partial y} \cdot \frac{\partial y}{\partial u}$$

$$= \left[5^{2(5u+2v)} \cdot 5 + 2(3u-v) \ln 5 \cdot 5^{2(5u+2v)} \cdot 3 \right]$$

~~$$\frac{\partial}{\partial u} (A \ln 5 + B) \cdot 5^{2(5u+2v)}$$~~

<p>GROUP NAME: Redacted to protect the ignorant</p> <p>Logo: </p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Face Palm</u></p>
<p>Date: <u>Ben</u></p> <p>Topics: #12 of midterm</p>	<p>Writer/Prep: <u>Derp McDerp</u></p> <p>QC/Leader: <u>AWOL, MIA</u></p>

Instructions: Print Clearly eg: 

12. a)
$$\frac{5x^2}{16} - \frac{y^2}{4.4} - \frac{7\pi z^2}{4} = 0$$

~~Hyperboloid of Two Sheets~~
Elliptical Cone

b)
$$\frac{a^2}{16} - \frac{b}{9} - \frac{c^2}{4} = 0$$

~~Elliptical Cone~~

Hyperbolic Paraboloid

c)
$$\frac{-a^2}{16} + \frac{b^2}{9} - \frac{r^2}{4} = -1$$

$$\frac{a^2}{16} + \frac{r^2}{4} - \frac{b^2}{9} = 1$$

Hyperboloid of One Sheet