

MAX / MIN PROBLEMS w/ CONSTRAINTS

1. Find Main Idea

$$D(x, y) = \sqrt{(x-5)^2 + (y-16)^2}$$

↑
Function of 2 variables

2. Identify Constraints. (-1 constraint for variables)

$$y = 16 - x^2$$

3. Made Main Idea Function of 1 variable.

$$D(x) = \sqrt{(x-5)^2 + (16-x^2-16)^2}$$

or

$$D(x) = (x-5)^2 + x^4$$

4. Use calculator or by hand.

A. $D_x = 0$ Critical points

B. Use 1st or 2nd derivative tests.

$$4x^3 + 2x - 10 = 0$$

$$x = 1.2348... \quad \leftarrow \text{critical Pt}$$

$$y = 16 - x^2 = 14.47...$$

CAN CAN

Main Idea

$$V = \pi r^2 h$$

Constraint

$$\text{Area} = 800 \text{ in}^2$$

TOP Circle

$$\pi r^2$$

Bottom

$$\pi r^2$$

Side

$$h \cdot 2\pi r = 800$$

$$2\pi r^2 + 2\pi r h = 800$$

$$h = \frac{800 - 2\pi r^2}{2\pi r}$$

Main Idea

$$V(r, h)$$

Variable

$$V(r) = \pi r^2 \left(\frac{400 - 2\pi r^2}{2\pi r} \right)$$

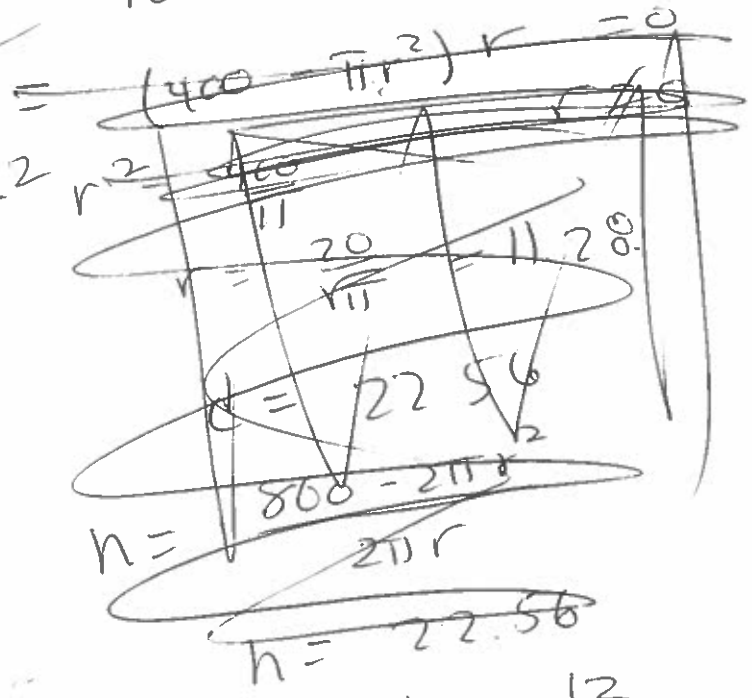
$$400r - \pi r^3 = 0$$

$$V'(r) = 400 - 3\pi r^2$$

$$r^2 = \frac{400}{3\pi}$$

$$r = \frac{200}{\sqrt{3\pi}}$$

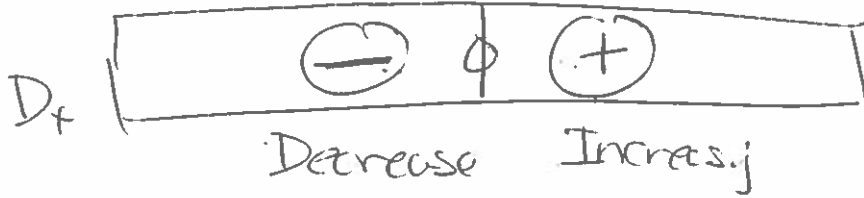
$$= 6.51$$



$$D = 13. \quad h = 13$$

1st Derivative Test

1.2348



$$D_x(1) =$$

$$4(1)^3 + 2(1) - 10 =$$
$$4 + 2 - 10 = \ominus$$

$$D_x(2) =$$

$$4(2)^3 + 2(2) - 10 = \oplus$$

2nd Derivative Test

$$D_{xx} = 12x^2 + 2$$

$$D_{xx}(1.2348) = 12(1.2348)^2 + 2 = \oplus$$

concave up \Rightarrow MIN

$$D_{xx} = \oplus$$

MIN

$$D_{xx} = \ominus$$

MAX

$$D_{xx} = 0$$

Inconclusive

EX

$$y = x^4$$

$$y' = 4x^3 = 0 \quad \text{critical } x=0$$

$$y'' = 12x^2 \quad y''(0) = 0$$

$$y'(-1) = -4 = \ominus$$

~~MIN.~~

$$y'(1) = 4 \oplus$$

1. Identify a Critical Point
to your Quartic Regression

$$\underline{\text{MAX}} \ 13.094... = X$$

2. Confirm with 1st Derivative Test

3. Confirm with 2nd Deriv. Test.

<p>GROUP NAME:</p> <p>Logo:</p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Aidan Callahan</u></p>
<p>Date: _____</p> <p>Topics:</p>	<p>Writer/Prep: <u>Logan Ackenby</u></p> <p>QC/Leader: <u>Kyle</u></p>

Instructions:

min & max

$$y_1 = \text{reg}$$

$$y_2 = \text{incline}(y_1, x, x)$$

$$y_3 = \text{incline}(y_2, x, x)$$

x	y ₁	y ₂	y ₃

GROUP NAME: <u>WOLFDACK</u>	Student Names (First and Last)
Logo:	Speaker/Presenter: <u>Jared</u>
Date: <u>11/4/13</u>	Writer/Prep: <u>DC</u>
Topics:	QC/Leader: <u>Quay</u>

Instructions:

$$Y_1 = 15.1995x^4 + 619.7057x^3 - 928390.7490x^2 + 61885436.8029x - 1554390404$$

$$Y_1' = 60.798x^3 + 18591.171x^2 - 1846781.49x + 61885436.8029$$

$$Y_1'' = 182.394x^2 + 36782.342x - 1846781.49$$

x	Y ₁	Y ₁ '	Y ₁ ''	
96.842	683.9	-4	-1500	MAX
99.654	-943.2	0	1025	MIN
105.47	10470	4	-3425	MAX

Decrease: 0, Increase ⇒ MIN

GROUP NAME: Logo:	Student Names (First and Last) Speaker/Presenter: _____
Date: _____ Topics:	Writer/Prep: _____ QC/Leader: _____

Instructions:

[Faint handwritten notes and calculations are visible in this section.]

13.7	9	176 ²	-51.61
13	7	23	-17.53
14	4	-3	-61.77

GROUP NAME: IRISH MATH BOMBS

Logo: 

Student Names (First and Last)

Speaker/Presenter: Robby O'Connell

Writer/Prep: Conner Krup Simon

QC/Leader: Buffalo Bill Smith

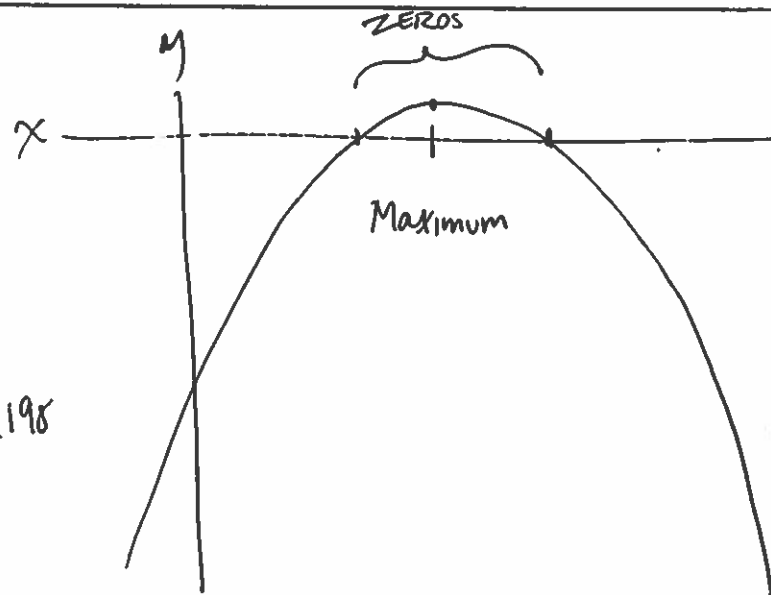
Date: _____

Topics:

Instructions:

PBR Sales (2003-2013)

x	y
3	13
5	15
7	16
9	19
11	20
13	21



$$y = -.0013x^4 + .0835x^3 - .292x^2 + 1.89x + 4.198$$

$$y_1' = nDeriv(y_1, x, x)$$

$$y_2 = nDeriv(y_2, x, x)$$

What does
the
prof say?



Wrong wrong wray wray wray

GROUP NAME: Time Is Money



Logo:

Student Names (First and Last)

Speaker/Presenter: Angelika Mazurek

Writer/Prep: Shyam Singh (Shiv)

QC/Leader: Eugenio Pelaez

Date: 11/4/13

Topics: Max & Min

Instructions:

Sale of IPhone 4S

Identifying a critical point to your Quc
 (2nd) Cot. 4: Max/min

Max $x = -.0140592, y = 755.04228$

$Y_1 = 3.7$

$Y_2 = \text{nd deriv}(Y_1, x, x)$

$Y_3 = \text{nd deriv}(Y_2, x, x)$

x	Y ₁	Y ₂	Y ₃	Max
\uparrow .0140592	755.04	-2.4	-429.2	{(increase down)}
0	755	-6	-423.8	
-1	474	649.17	-910.8	

GROUP NAME: CC

Logo:

Date: 11/4/13

Topics:

Student Names (First and Last)

Speaker/Presenter: _____

Writer/Prep: COLLEEN L. SMITH

QC/Leader: Stephen Smith

Instructions:

12	47	5629	.0032	-34
12		532.17	111.63	-138.3
13		501.02	-265.1	-672.6

Max: MUM

GROUP NAME: The factors

Student Names (First and Last)

Logo:

Speaker/Presenter: Brian Chokoy

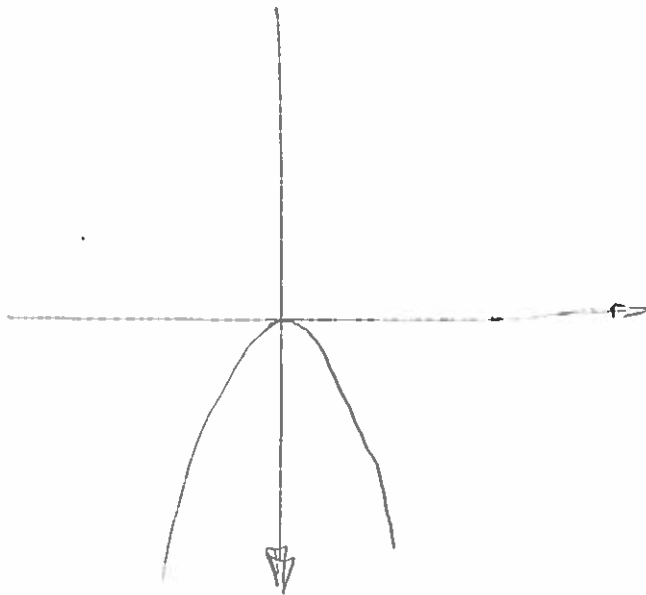
Date: 1/4/12

Writer/Prep: Ryan Elyan

Topics:

QC/Leader: Ethan Stewart

Instructions:

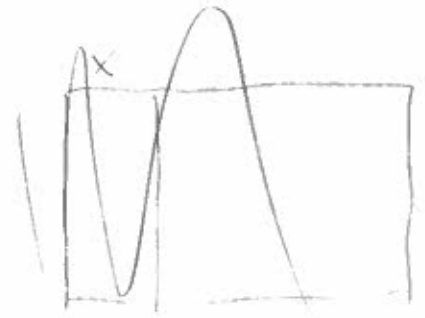


Maximum

$x = 101.0238$

$y = 9.2760527$

1st
derivative
1st



2nd
derivative
1st

— concave down
 $-0.0696 = y''$

GROUP NAME: Apples & Popples
 Logo:
 Date: 11/24/13
 Topics:

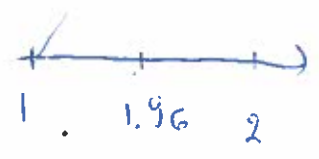
Student Names (First and Last)
 Speaker/Presenter: EMMA
 Writer/Prep: ...
 QC/Leader: THOMAS

Instructions: Find min. and max.

$y_1 = \text{reg.}$
 $y_2 = n \text{ Deriv}(y_1, x, x)$
 $y_3 = n \text{ Deriv}(y_2, x, x)$

X	y ₁	y ₂	y ₃
1.96	9.005	-0.001	4.28
1	6	7.33	-11
2	9	-0.166	-4

• MAX



$D_{xx} = \ominus = \text{max}$