

Graphing an exponential function and its asymptote: $f(x) = a(e)^{x-b} + c$

Graph the following function.

$$g(x) = \frac{1}{4}e^{x-3} - 4$$

$$g(0) = \frac{e^{-3}}{4} - 4 = \frac{1}{4e^3} - 4$$

$$g(3) = \frac{1}{4} - 4 = -3.75$$

To draw the graph, plot two points and the asymptotes (if any) of the graph. Then click on the graph icon.

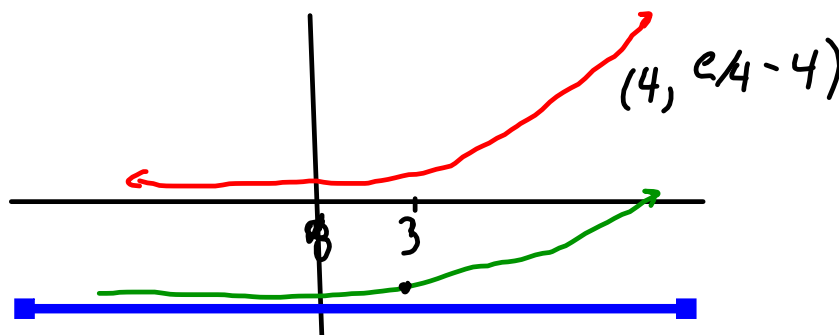
$$g(4) = \frac{e}{4} - 4 \quad (3, -3.75)$$

parent: e^x

-3 right 3

.25 shrink

-4 lower 4



Evaluating an exponential function that models a real-world situation

A species of animal is discovered on an island. Suppose that the population size $P(t)$ of the species can be modeled by the following exponential function, where time t is measured in years.

$$P(t) = \frac{550}{1 + 6e^{-0.31t}}$$

Find the initial population size of the species and the population size after 8 years. Round your answers to the nearest whole number as necessary.

initial $t = 0$ $P(0) = 550 / (1 + 6e^0)$

at 8 years $t = 8$ $P(8) = 550 / (1 + 6e^{-0.31 \cdot 8}) =$

Precalc= study of functions

function= job

domain = in

range = outbox

vertical line test for functions

inverse function = undoes a function

Inverse
Function

Switch

Domain +
Range

$$f^{-1}(x) = \frac{1}{2}x$$

$$f(x) = 2x$$

$$f^{-1}(6) = 3$$

$$f(3) = 6$$

$$g(x) = x^2 \quad (x \geq 0)$$

$$g(3) = 9$$

$$g(-3) = 9$$

$$g^{-1}(x) = \sqrt{x}$$

x	g(x)
3	9
-3	9

FAILS
Horizontal
Line
Test
pass
VLT

x	g^{-1}(x)
9	3
9	-3

FAILS
Vertical
Line
Test

How to Find

1. Solve for X
2. $x \rightarrow y^{-1}, y \rightarrow x$ (switch X & Y)

STEP 1

$$y = \frac{2x-4}{x}$$

$$xy = 2x-4$$

$$xy - 2x = -4$$

$$x(y-2) = -4$$

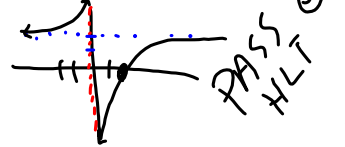
$$x = \frac{-4}{y-2}$$

STEP 2

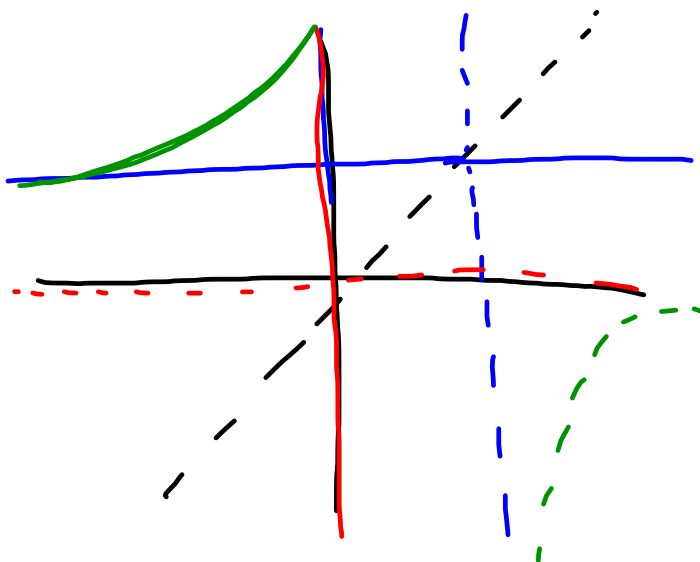
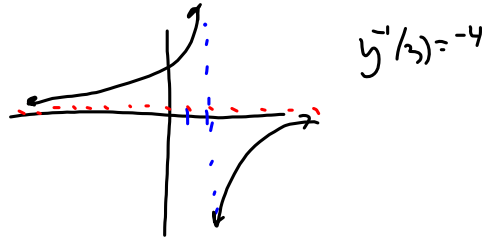
$$y^{-1} = \frac{-4}{x-2}$$

$$y = \frac{2x-4}{x}$$

Does it... PASS HIT? ☺



HAS A INVERSE!



Day 10 - Question #1;
Horizontal line test

For each function graphed below, state whether it is one-to-one.

One-to-one?	<input type="radio"/> Yes <input type="radio"/> No	<input type="radio"/> Yes <input type="radio"/> No	<input type="radio"/> Yes <input type="radio"/> No
One-to-one?	<input type="radio"/> Yes <input type="radio"/> No	<input type="radio"/> Yes <input type="radio"/> No	<input type="radio"/> Yes <input type="radio"/> No

Composite Functions $f(g(x))$

put g inside of f

$$f(x) = x + 1$$

$$g(x) = x^2$$

$$g(f(x)) = g(x+1) = (x+1)^2$$

$$f(g(x)) = f(x^2) = x^2 + 1$$

$$f(g(2)) = f(4) = 5$$

Define

$$(f \circ g)(x) = f(g(x))$$

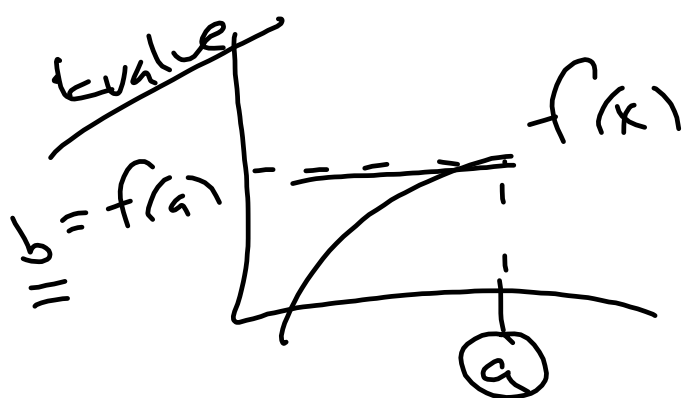
Inverse

$$(f \circ f^{-1})(x) = x$$

$$(f^{-1} \circ f)(x) = x$$

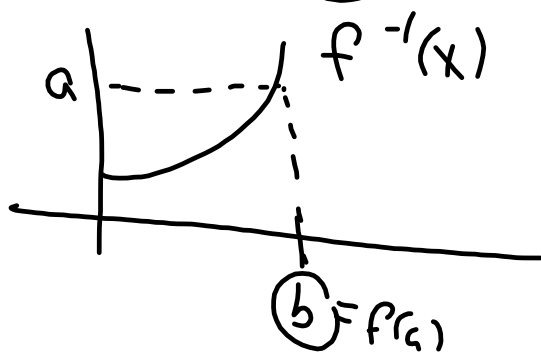
Ex $h(h^{-1}(7)) = 7$

Ex $P^{-1}(P(b)) = b$



$$b = f(a)$$

$$f^{-1}(b) = a$$



Evaluate the
Inverse inverse
To solve

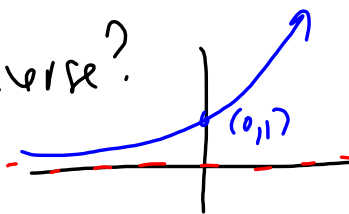
Example ???

$$y = 3^x$$

Does it have an inverse?

Exponential

Passes HLT. yes

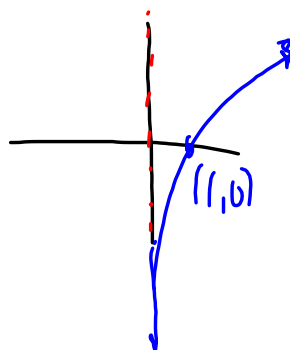


1.

$$x = \frac{\log y}{b}$$

2.

$$y^{-1} = \log_3 x$$

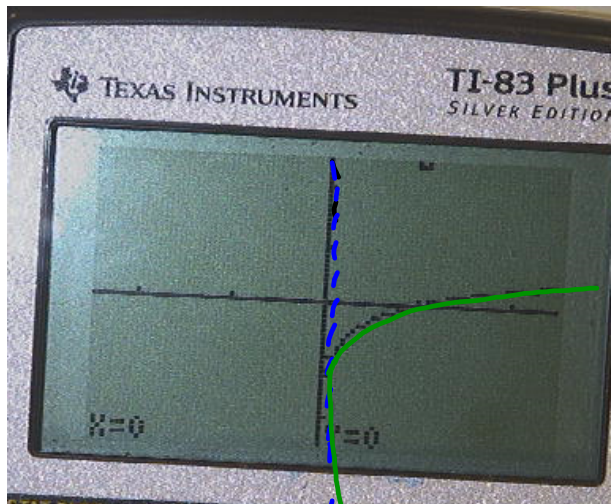


ex

$$y = 10^x$$

$$y^{-1} = \log_{10} x \equiv$$

Common
 $\log x$



$$y = 10^x$$

$$D: \mathbb{R}$$

$$R: (0, \infty)$$

$$y = \log x$$

$$D: (0, \infty)$$

$$R: \mathbb{R}$$

Natural log

$$y = e^x$$

$$y^{-1} = \ln x \quad D: (0, \infty)$$

Do a LN regression... make a prediction

put in words!!!!

To graph $\log_B X$

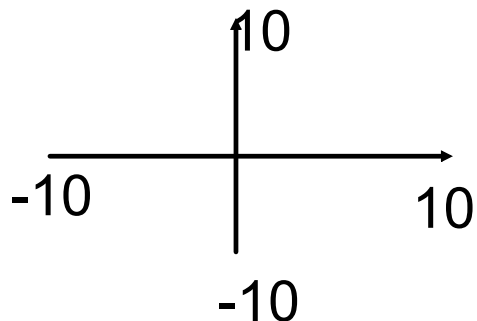
$$y_1 = \log(X) / \log(B)$$

$$\text{Ex } y = 1/2 \log_{20}(3x) + 7$$

$$y_1 = (1/2) \log_3(3x) / \log(20) + 7$$

Adjusting the Window on TI83 calculator

For ALEKS homework...try Zoom 6: standard



For DATA try ZOOM 9: stat

If you want to see a whole graph for give x values...try ZOOM 0: zoomfit