

Rational Functions

Poly Numerator Zeros (ZN) Degree DN LI
 Poly Denominator Zeros (ZD)

Zeros of Rational = ZN

Vertical Asymptote = ZD

LND Behavior

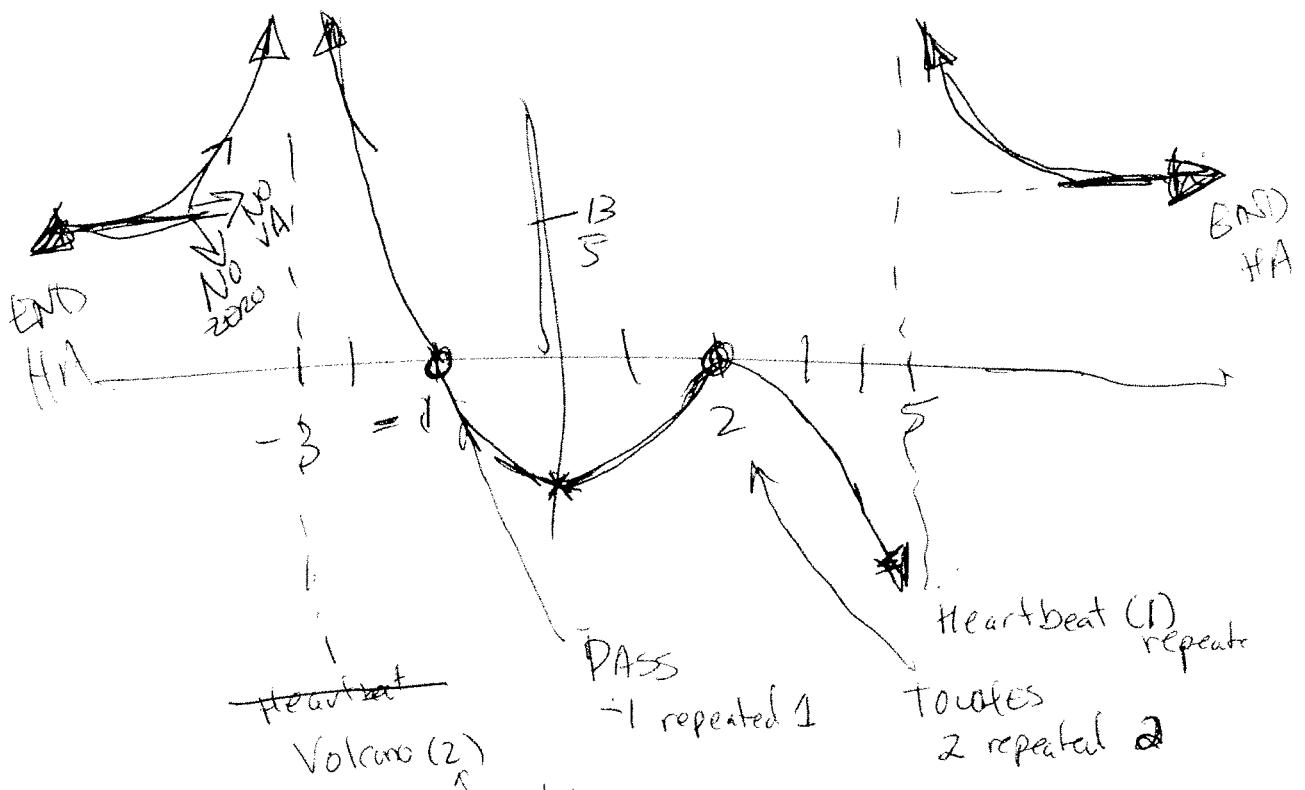
$DN = 3$
 $DD = 3$

$$HA = \frac{LN}{LD} = \frac{13}{5}$$

Ex

$$y = \frac{13(x-2)^2(x+1)}{5(x+3)^2(x-5)}$$

Zeros
 $ZN = 2, -1$
 V.A
 $ZD = -3, 5$



Ex

$$y = \frac{13(x-2)^2(x+3)^1}{5(x-7)^3(x+1)^2}$$

ZN: 2, -3
ZD: 7, -1

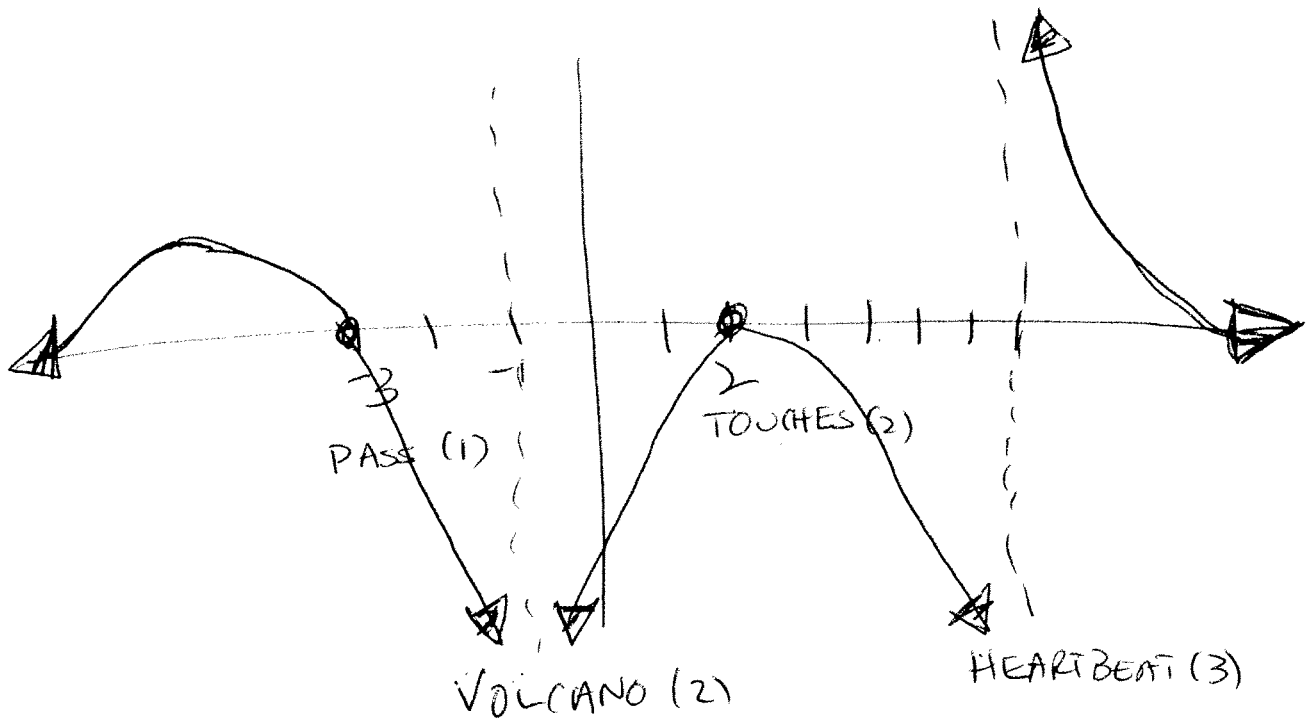
Zeros of y : 2, -3

Vertical Asym : 7, -1

END
DN: 3
DD: 5

DD > DN

$y = 0$



$$y(-4) = \frac{13(-6)^2(-1)^1}{5(-11)^3(-3)^2} = \oplus$$

Ex $y = \frac{-3(x-4)^7}{5(x+2)^3}$

$zN = 4$

$zD = -2$

Zeros of y : 4

VA: -2

END Behavior

DN: 7

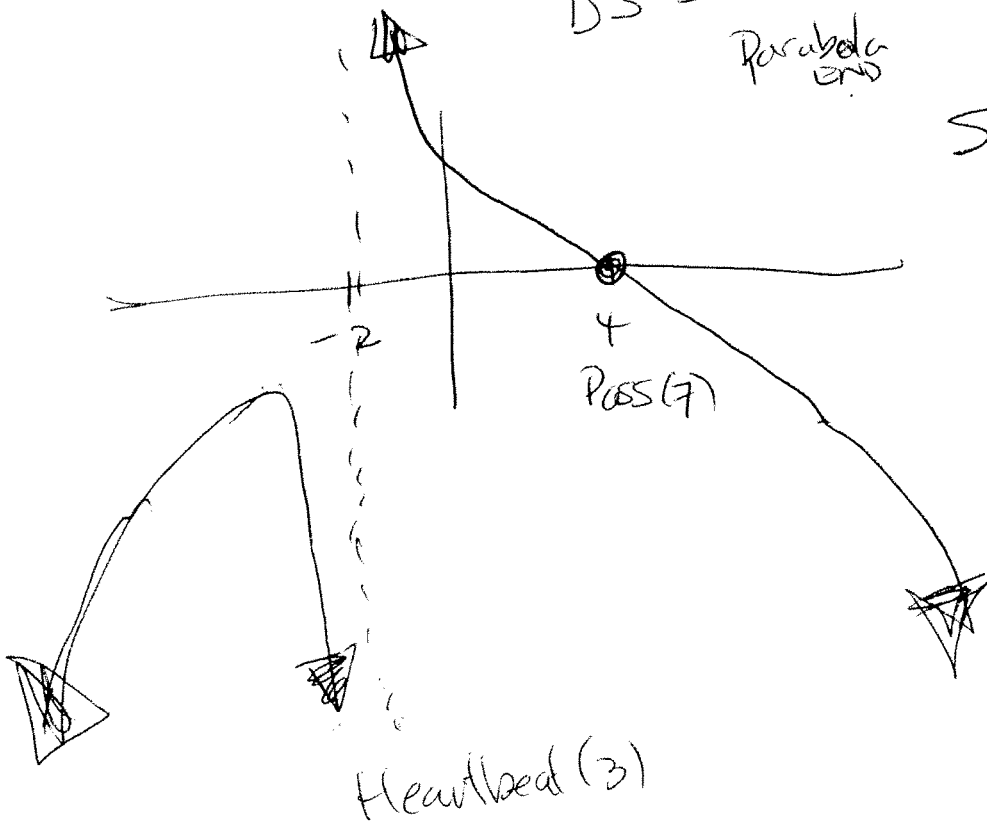
DD: 3

DS = 7 - 3 = 4

Parabola END

LS = $\frac{LN}{LD} = \frac{-3}{5}$

SAD $\rightarrow \ominus$



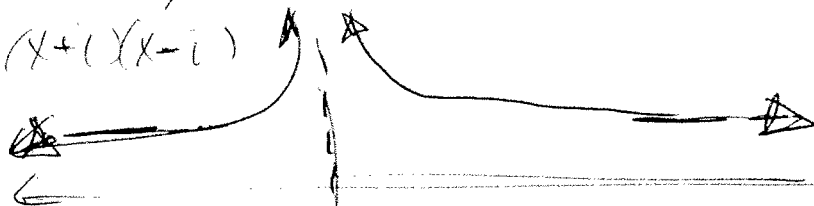
Ex

$y = \frac{x^2 + 1}{x^2}$

zN : No Real

zD : 0

$(x+i)(x-i)$



No Zeros
VA: $x = 0$

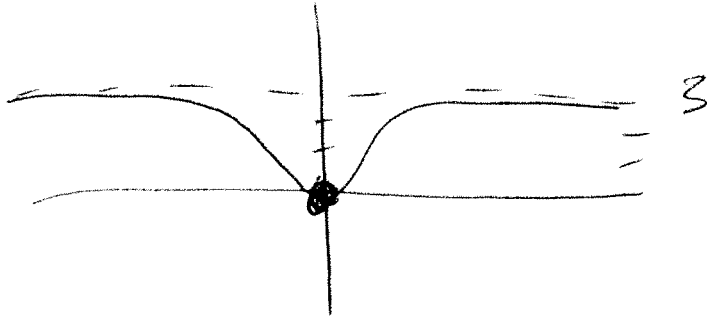
END Behavior

DN: 2

DD: 2

HA: $y = \frac{40}{40} = \frac{1}{1} = 1$

Ex



zero: $x=0$

x^2

HA: $y=3$

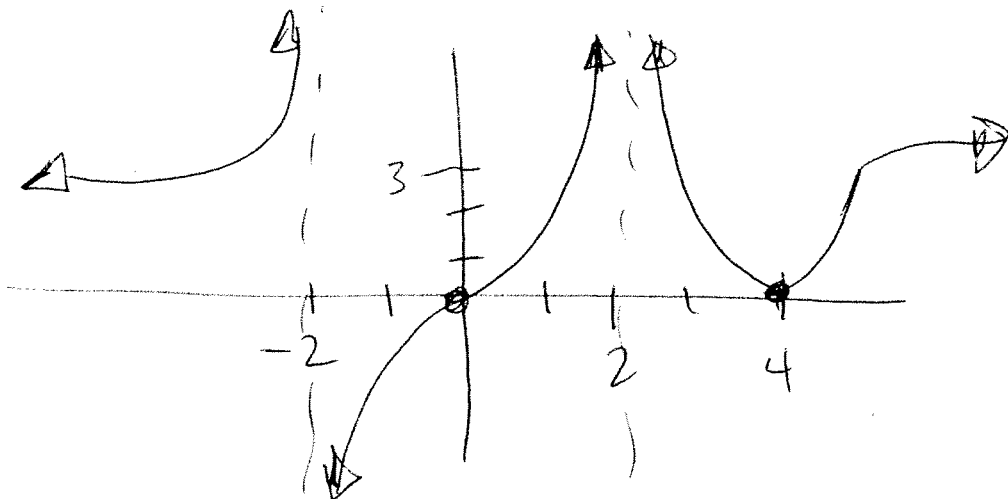
DU=DN

LN=3 LD=1

$$y = \frac{3x^2}{x^2 + 4} \quad \leftarrow \text{NO Real Zeros}$$

$(x+2i)(x-2i)$

Ex



Zeros: 0, 4

VA: $x = -2, 2$

$$y = \frac{3(x)(x-4)}{(x+2)(x-2)^2}$$

GROUP NAME: DA BROWNIES

Logo:

Date: 9-23-13

Topics:

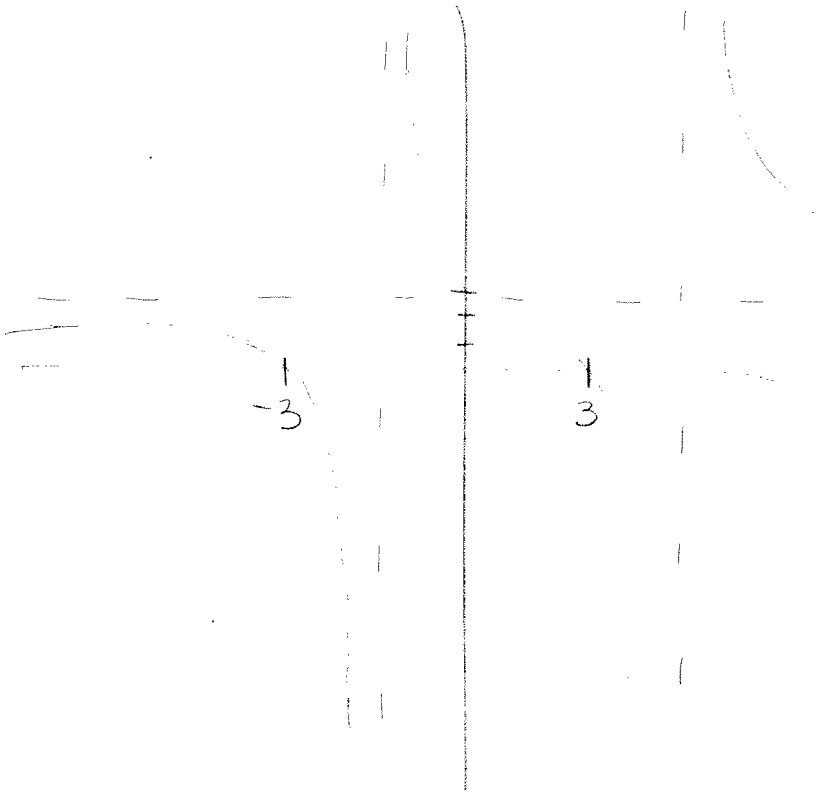
Student Names (First and Last)

Speaker/Presenter: Harrison Suelter

Writer/Prep: Vinnie Avhad

QC/Leader: Joe Korman

Instructions:



$$VA = x = -2, x = 5$$

$$HA = y = 3$$

$$\text{Zeros} = 3, -3$$

$$\text{Pass} = (-7, 2)$$

$$f(x) = \frac{a}{x-b}$$

$$f(x) = \frac{a(x-b)}{x-c}$$

$$f(x) = \frac{a}{(x-b)(x-c)}$$

$$f(x) = \frac{a(x-b)}{(x-c)(x-d)}$$

$$f(x) = \frac{a(x-b)(x-c)}{(x-d)(x-e)}$$

$$\frac{3(x-3)(x+3)}{1(x+2)(x-5)}$$

<p>GROUP NAME:</p> <p>Logo:</p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Trey</u></p>
<p>Date: _____</p> <p>Topics:</p>	<p>Writer/Prep: <u>Dominique</u></p> <p>QC/Leader: <u>Tatiana C.</u></p>

Instructions:

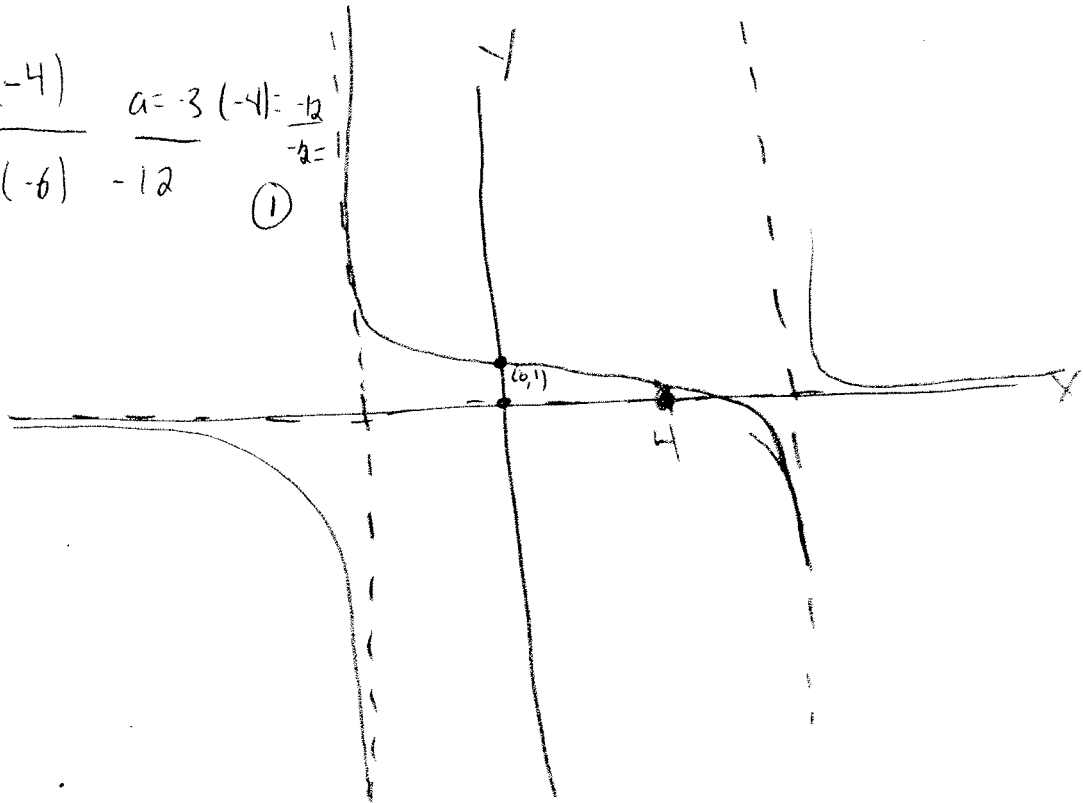
$$y = \frac{a(x-4)}{(x+2)(x-6)}$$

VA: -2, 6

y = 0 HA

$$1 = \frac{a \cdot (-4)}{(2)(-6)} \quad a = \frac{-3(-4) = 12}{-2 = 1}$$

①



Answer ✓

$$y = \frac{3(x-4)}{(x+2)(x-6)}$$

<p>GROUP NAME:</p> <p>Logo:</p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Brendan Brown</u></p>
<p>Date: _____</p> <p>Topics:</p>	<p>Writer/Prep: <u>Simon Gorman</u></p> <p>QC/Leader: <u>Paishit Janwale</u></p>

Instructions:

No zeros

VA: -4, 3

$$y = \frac{a}{(x+4)(x-3)}$$

$$y = \frac{a}{(x+4)(x-3)}$$

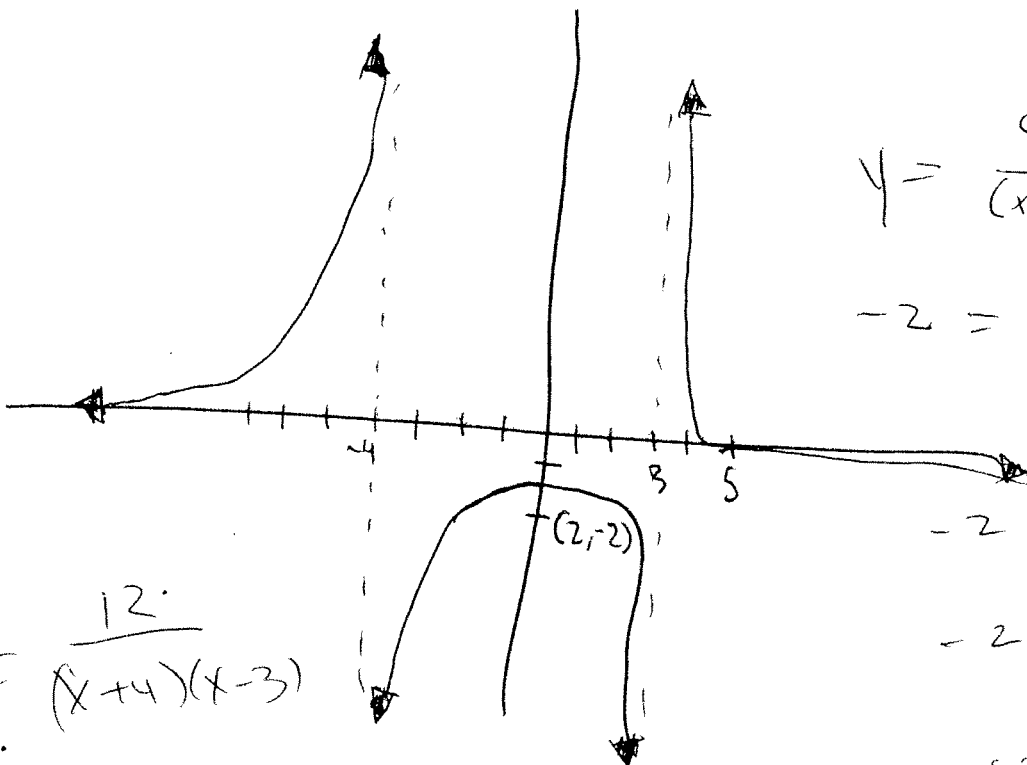
$$-2 = \frac{a}{(2+4)(2-3)}$$

$$-2 = \frac{a}{(6)(-1)}$$

$$-2 = \frac{a}{-6}$$

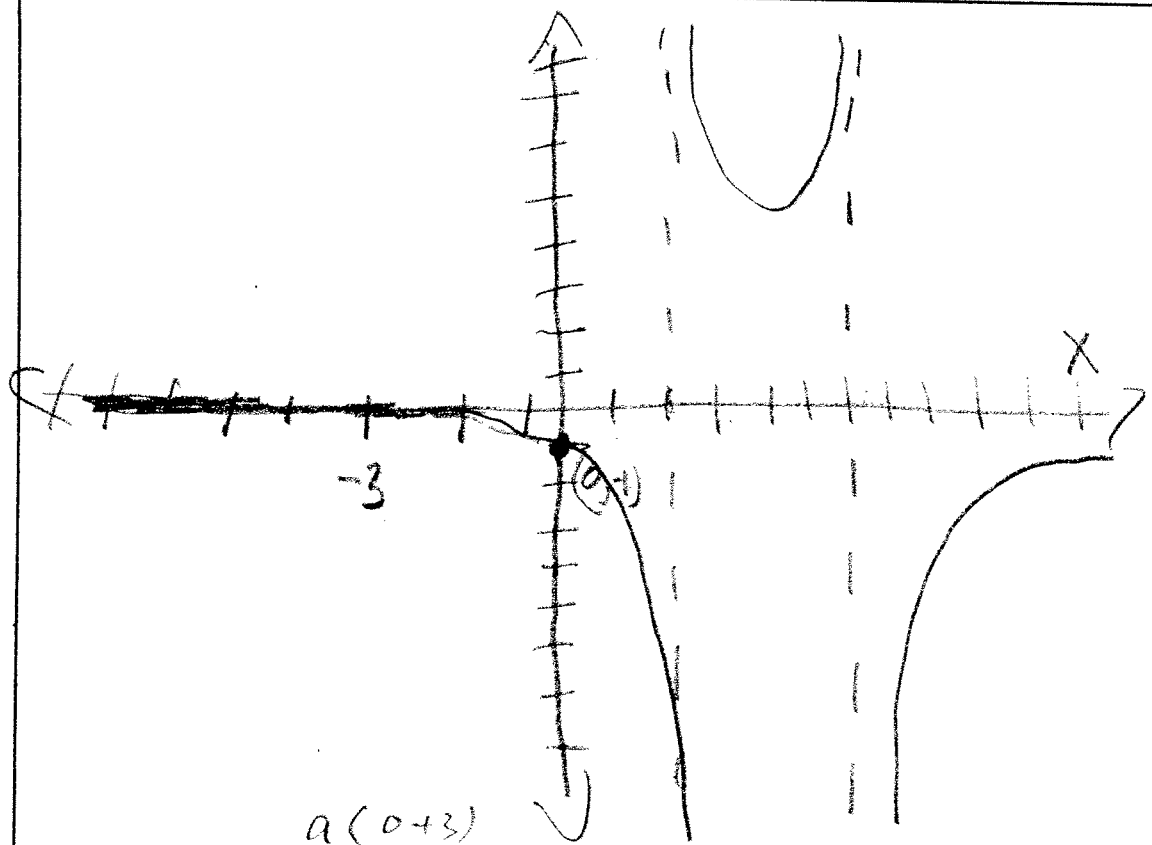
$$12 = a$$

$$y = \frac{12}{(x+4)(x-3)}$$



GROUP NAME:	Student Names (First and Last)
Logo:	Speaker/Presenter: <u>Star Kaplan</u>
Date: _____	Writer/Prep: <u>Vaisincat</u>
Topics:	QC/Leader: <u>Danyan Zhou</u>

Instructions:



$$-1 = \frac{a(0+3)}{(0-2)(0-6)}$$

$$(-1)(12) = 3a$$

$$a = \frac{-12}{3} = -4$$

$$\frac{a(x-b)}{(x-c)(x-d)} = \frac{-4(x+3)}{(x-2)(x-6)}$$

$$\frac{-1(x+3)^1}{(x-2)^1(x-6)^1}$$

GROUP NAME: ~~Future~~

Logo:

Date: _____

Topics:

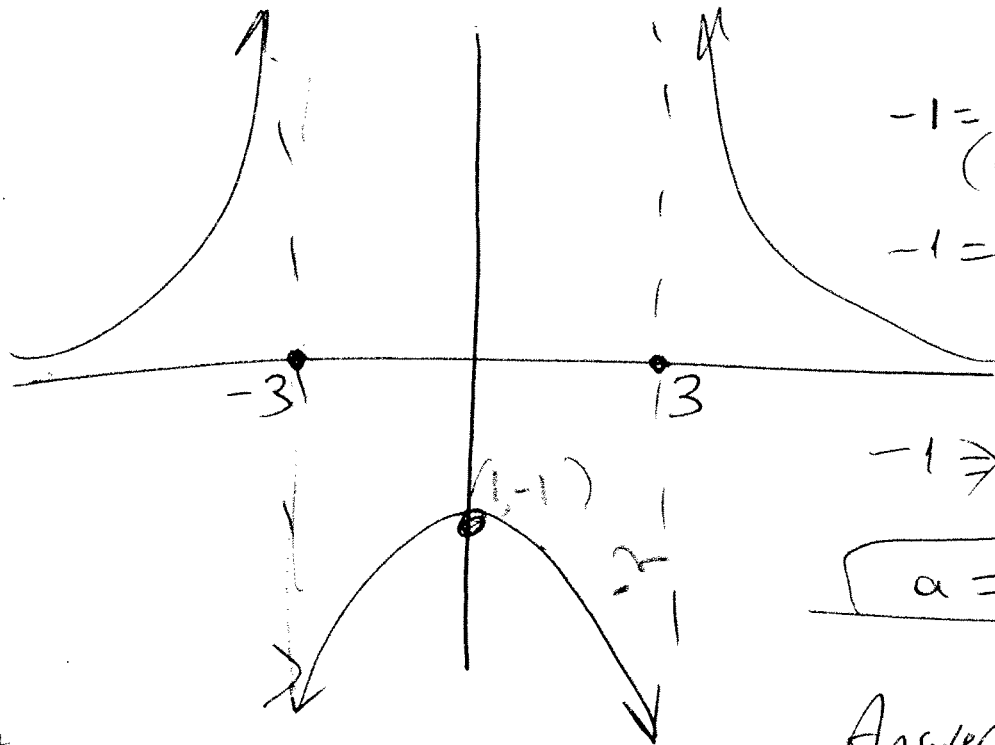
Student Names (First and Last)

Speaker/Presenter: Onur Turkcan

Writer/Prep: Kerline Simon

QC/Leader: Sharon Isoe

Instructions:



$$-1 = \frac{a}{(1+3)(1-3)}$$

$$-1 = \frac{a}{4 \cdot -2}$$

~~$$-1 = \frac{a}{-8}$$~~

$$a = 8$$

~~2D~~ HA

ZD: 3, -3

V.A: 3, -3


$$y = \frac{a}{(x+3)(x-3)}$$

x for 1 and y for -1

$$-1 = \frac{8}{4 \cdot -2} \quad \boxed{a = 8}$$

Answer $y = \frac{8}{(x+3)(x-3)}$

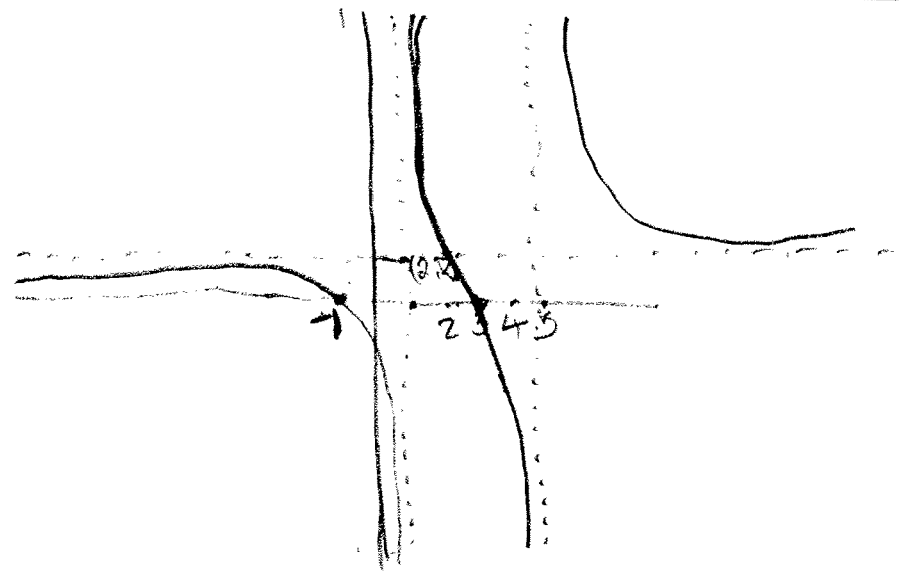
[Faint handwritten notes]

<p>GROUP NAME: <u>ILM</u></p> <p>Logo: </p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Jake Peebles</u></p>
<p>Date: <u>09/23</u></p> <p>Topics: <u>Rational function.</u></p>	<p>Writer/Prep: <u>Mikal Desai</u></p> <p>QC/Leader: _____</p>

Instructions: Find the (osined) equation

$f(x) = \frac{a}{x-b}$, $f(x) = \frac{a(x-b)}{x-c}$, $f(x) = \frac{a}{(x-b)(x-c)}$, $f(x) = \frac{a(x-b)}{(x-d)(x-e)}$

$$f(x) = \frac{a(x-b)(x-c)}{(x-d)(x-e)}$$



Answer

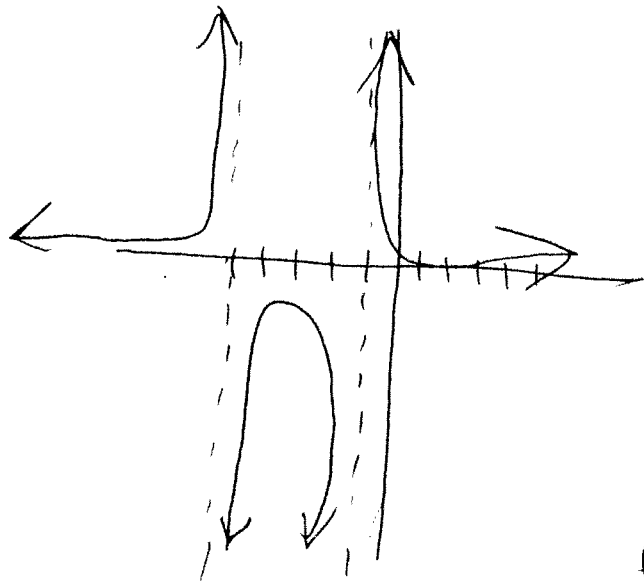
$$f(x) = \frac{a(x-b)(x-c)}{(x-d)(x-e)}$$

$$f(x) = \frac{2(x+1)(x-3)}{(x-1)(x-5)}$$

<p>GROUP NAME: Rachel Joyce, Kausalya, Alex Valerie</p>	<p>Student Names (First and Last)</p>
<p>Date: 9/23/13</p> <p>Topics:</p>	<p>Speaker/Presenter: _____</p> <p>Writer/Prep: _____</p> <p>QC/Leader: _____</p>

Instructions: With this graph decide which equation it is

$f(x) = \frac{a}{x-b}$
 $f(x) = \frac{a(x-b)}{x-c}$
 $f(x) = \frac{a}{(x-b)(x-c)}$
 $f(x) = \frac{a(x-b)}{(x-c)(x-d)}$
 $f(x) = \frac{a(x-b)(x-c)}{(x-d)(x-e)}$



$V_A = x = -5, -1$ no zeroes
 $Y=0$ $N < D$ ~~2 VAs~~
 2 heartbeats


~~$f(x) = \frac{a}{x-b}$~~

$DN = 1$
 $DD = 2$

$f(x) = \frac{a}{(x-b)(x-c)}$ $a = 15$

$f(x) = \frac{a}{(x+5)(x+1)}$

~~$f(x) = \frac{x}{(x+5)(x+1)}$~~

<p>GROUP NAME: <u>Math Lovers</u></p> <p>Logo: </p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Avik Khareja</u></p>
<p>Date: <u>9/25/13</u></p> <p>Topics:</p>	<p>Writer/Prep: <u>Avik Khareja</u></p> <p>QC/Leader: <u>Jon Sebivo</u></p>

Instructions:

VA: $x = -1$
 $x = 6$

HA: $y = 2$

x int: 5

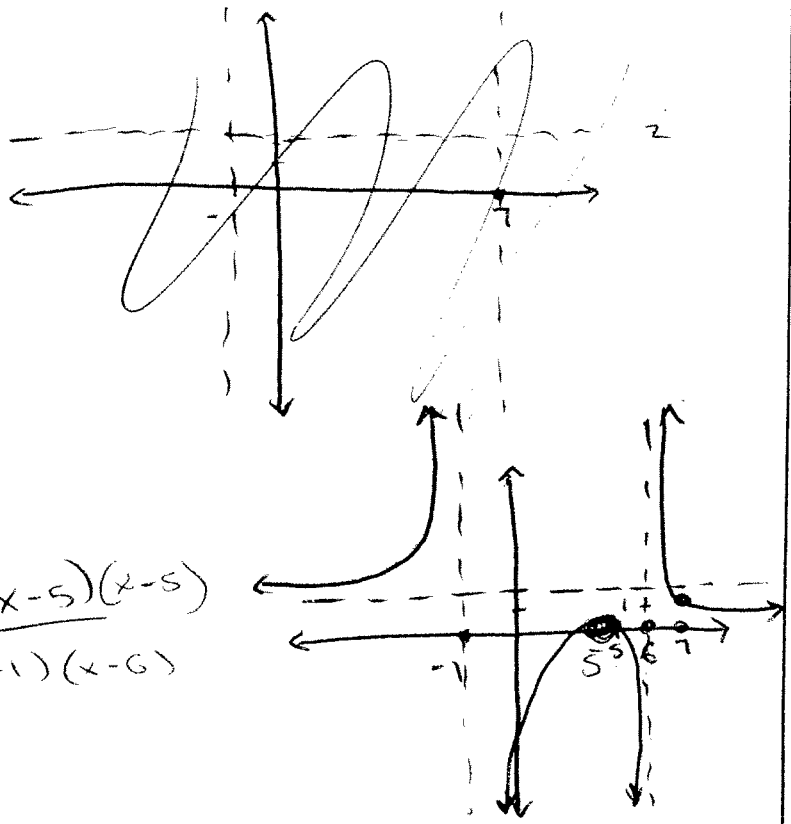
Passes through: (7, 1)

ZD: $(x+1)(x-6)$

ZN: $(x-5)(x-5)$

~~so~~ $2 \frac{(x-5)(x-5)}{(x+1)(x-6)}$

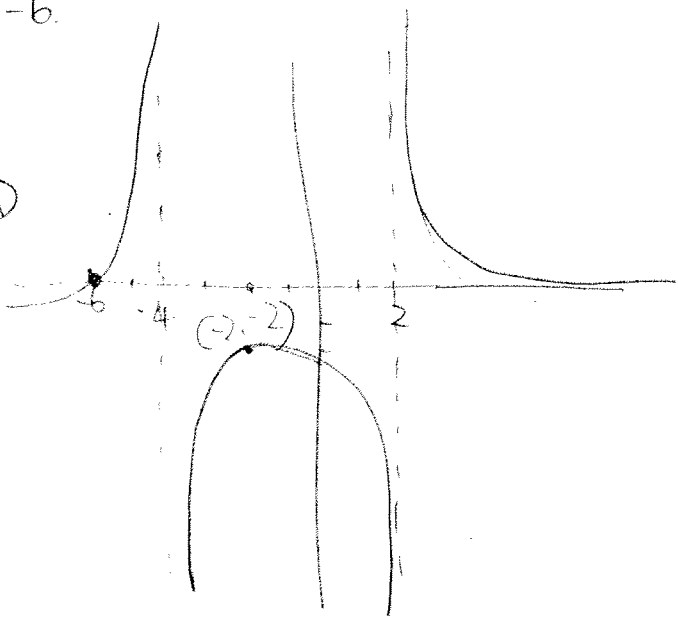
answer: $\frac{a(x-b)}{(x-c)(x-d)}$



<p>GROUP NAME:</p> <p>Logo:</p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Mengqi Guo</u></p>
<p>Date: _____</p> <p>Topics:</p>	<p>Writer/Prep: <u>Mengqi Guo</u></p> <p>QC/Leader: <u>Rex Liang</u></p>

Instructions:

$zD: 2, -4$
 $zN: -6$
 D
 $y > 0$
 $N < 0$



$$y = \frac{4(x+6)}{(x-2)(x+4)}$$

$$y = \frac{a(x+b)}{(x-2)(x+4)}$$

$$y = \frac{a(-2+b)}{(-2-2)(-2+4)}$$

$$-2 = \frac{a(4)}{-4(2)}$$

$$-2 = \frac{4a}{-8}$$

$$\frac{4a}{-8} = -2$$

$$\Delta a = 16$$

$$a = 4$$

<p>GROUP NAME:</p> <p>Logo:</p>	<p>Student Names (First and Last)</p> <p>Speaker/Presenter: <u>Natalie Cassin</u></p>
<p>Date: _____</p> <p>Topics:</p>	<p>Writer/Prep: <u>LAUREN DOBO</u></p> <p>QC/Leader: <u>Bjtn</u></p>

Instructions:

VA: $x = -1, x = 3$
 HA: $y = 0$ NKM
 x-INT: 1. ∴ ZERO @ 1
 P: (2, 1)

$$y = \frac{(x-1)}{(x+1)(x-3)}$$

$$1 = \frac{a(x-1)}{(x+1)(x-3)} = \frac{a1}{(3)(-1)} = \frac{a1}{-3} = 1 \quad \begin{matrix} a = (1) \cdot (-3) \\ a = -3 \end{matrix}$$

$$u = \frac{-3(x-1)}{(x+1)(x-3)}$$

